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The Effect of Iron Displacement Out of the Porphyrin Plane on the Resonance Raman Spectra of Heme Proteins and Iron Porphyrins

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ABSTRACT

The causes of the strong coupling of the iron-histidine vibration to the Soret resonance in the resonance Raman spectra of deoxyhemoglobin, myoglobin, and peroxidase are explored, using the vibronic theory. It is shown that the extent of the iron displacement out of the plane of the porphyrin nitrogens is the main structural parameter controlling the Fe-N_{His} band features, such as the dependence of its frequency and intensity on the protein conformation and number of the axial ligands, time evolution after the photolysis of the diatomic complexes of the proteins under consideration, and inverse relationship between the changes Fe-N_{His} and \nu_{4} porphyrin breathing mode frequencies.

1. INTRODUCTION

The mechanism of the interaction between the active center and the protein globule in the heme proteins was subject to numerous investigations (see, for example, Gelin et al. (1983), Frauenfelder et al. (1988), Rousseau and Friedman (1988), Perutz (1989)). In hemoglobin (Hb), myoglobin (Mb), and peroxidase (PO), the bond between iron and the proximal histidine imidazole nitrogen, Fe-N_{His}, is the only covalent bond between the heme and the globule (Frauenfelder et al., 1988; Kitagawa, 1988; Rousseau and Friedman, 1988; Perutz, 1989). Therefore, any experimental technique which allows to study this bond directly, is very useful for the elucidation of the interaction under consideration.

It was previously shown (Hori and Kitagawa, 1980; Teraoka and Kitagawa, 1981; Collman et al., 1983; Kitagawa, 1988; Rousseau and Friedman, 1988), that the resonance Raman scattering spectra of Hb, Mb, and PO and their model compounds contain bands in the region of 200–250 cm\(^{-1}\) which correspond to the Fe-N_{His} vibration. The frequencies and intensities of these bands essentially depend on the nature and conformation of the protein, temperature and kind of solvent (Kitagawa, 1988; Rousseau and Friedman, 1988). It was also shown that in the heme proteins the Fe-N_{His} frequency, \nu(Fe-N_{His}), inversely correlates to the frequency of the porphyrin vibration, \nu_{4}, which is mainly the pyrrole C—N vibration. Both bands were widely used to study the dependence of the structure and conformation of the heme proteins on the temperature, allosteric effectors, etc. Particularly useful was the study of these bands in the investigation of the dynamics of the proteins in combination with the flash-photolysis technique (Rousseau and Friedman, 1988).

It was proposed (Friedman et al., 1982) that the coordination geometry (see Fig. 1) of the histidine imidazole (the extent and direction of its tilt) is the main parameter of the compound that regulates the position and intensity of the Fe-N_{His} band. This point of view was supported by the authors of the resonance Raman study of Mb and Hb (Bangchareonpaupong et al., 1984), where the Fe-N_{His} vibration was shown to be coupled directly to the Soret excitation, which corresponds to the porphyrin ring \pi \rightarrow \pi^* excitation. Such a result was not trivial, because the nature of the Fe-N_{His} bond (strength, interatomic distance, force constant, etc.) is controlled mainly by the nature and population of the \sigma(Fe-N_{His}) iron-imidazole orbital. The latter is an antibonding component of the overlapping d_{z2} iron and p_{z} imidazole nitrogen orbitals, and it is elongated in the axial direction, perpendicular to the porphyrin plane. Therefore marked intensity of the Fe-N_{His} band in the resonance Raman spectrum implies that the porphyrin and axial electronic subsystems are not orthogonal in the compounds under consideration. To explain this experimental result it was proposed (Bangchareonpaupong et al., 1984) that the tilt of the proximal imidazole reduces the D_{4h} symmetry of the heme, strongly mixing the \sigma(Fe-N_{His}) and e_{g}(\pi^*) molecular orbitals (MOs), and the extent of this mixing essentially depends on the direction of the tilt. This assumption, called below as BSC model, allowed to explain qualitatively a number of experimental data (see Section 3).

At the same time it was mentioned (Champion, 1988) that "a mixing of the a_{1u}, a_{2u} \rightarrow e_{g} porphyrin orbital transitions with spin allowed excitations involving the d_{z2} iron orbital" can lead to the coupling of the Fe-N_{His} vibration to Soret resonance. Such a mixing can take place due to the reduction of the D_{4h} symmetry of the heme to C_{4v} upon displacement of the iron out of the plane of the porphyrin nitrogens even if the axial symmetry is conserved. In this paper we will discuss in detail the influence of this displacement on the nature of the ground and excited states of heme proteins and their models, position, and intensity of the Fe-N_{His} and \nu_{4} bands and reanalyze the pool of experimental data on the structure, conformation, and dynamics of the heme proteins.
from this point of view (preliminary results of this analysis were presented by Stavrov (1992)).

2. THE ORIGIN OF THE IRON OUT-OF-PLANE DISPLACEMENT IN THE FIVE-COORDINATED METALLOPORPHIRINS AND THEIR ELECTRONIC STRUCTURE

In our previous works (Bersuker et al., 1979; Bersuker and Stavrov, 1981, 1983, 1988; Stavrov and Bersuker, 1983) the electronic causes for the iron displacement out of the plane of the porphyrin nitrogens, $q$, in the heme proteins and metalloporphins, Me(P)s, were investigated. To do this we studied the simultaneous effect of the axial-ligand “crystal field,” of $A_{2u}$ symmetry, and of the electron-nuclear (vibronic) interaction with the $q$ displacement of the same $A_{2u}$ symmetry (here and below we use notations of the $D_{4h}$ point symmetry group). For complexes with one axial ligand the second order perturbation theory in the one-electron approximation led to the following expressions for the valence MOs $\psi_i$:

$$\psi_i(q) = \psi_i^{(0)}(0) - \sum_j \frac{v_{ij}}{2\delta_j} \psi_j^{(0)}(0) - q \sum_j \frac{f_{ij}}{2\delta_j} \psi_j^{(0)}(0)$$

and their energies $\epsilon_i$

$$\epsilon_i(q) = \epsilon_i(0) - \Delta_v - q \sum_j \frac{v_{ij}}{\delta_j} - q^2 \sum \frac{f_{ij}^2}{2\delta_j}$$

where $\psi_i(0)$ is the $i$th MO of the pure imidazole or Fe(P), calculated for the iron-in-plane nuclear configuration of the latter ($q = 0$); $\epsilon_i(0)$ is its energy; $\Delta_v$, a term that describes the change in MO energy due to complex formation, and does not depend on $q$; $2\delta_{ij} = \epsilon_i(0) - \epsilon_j(0)$ is an energy gap between the $i$th and $j$th MOs, and $v_{ij}$ and $f_{ij}$ are the corresponding one-electron matrix elements of the ligand “crystal field” and vibronic operators.

We can obtain an expression for the whole electronic energy of the system by summing over the valence MO energies, multiplied by their electronic population numbers, $p_i$, and adding the term $\frac{1}{2}K_{eff}q^2$, that describes the elastic energy of inner orbitals.

$$E = E_0 - \Delta_v - q \sum p_i \frac{v_{ij}^2}{\delta_j} + \frac{1}{2} q^2 \left( K_0 - \sum p_i \frac{f_{ij}^2}{\delta_j} \right)$$

(3)

where $E_0$ is a whole energy of the pure Fe(P) and imidazole and $\Delta$ describes the energy gain due to the complex formation and does not depend on $q$. Taking advantage of Eq. 3 we can calculate a position of the energy minimum of the system in the $q$ direction, which corresponds to the electron-vibrational contribution into the iron out-of-plane displacement $q_{ev}$:

$$q_{ev} = \left( \sum p_i \frac{f_{ij}^2}{\delta_j} \right) \left( K_0 - \sum p_i \frac{f_{ij}^2}{\delta_j} \right)^{-1}$$

(4)

We must notice that the contributions of the mixing MOs with the same population numbers to the sums of Eqs 3 and 4 cancel each other. Therefore, the mixing of the iron porphyrin MOs with different $p_i$ only contributes to the dependence of the whole electronic energy on $q$, leading to the iron out-of-plane displacement in the complexes with one axial ligand.

It was shown (Bersuker et al., 1979; Bersuker and Stavrov, 1981, 1983, 1988; Stavrov and Bersuker, 1983), that the main contribution to $q_{ev}$ results from the mixing of the $a_1g(d_{xz})$ and $a_2g(d_{yz})$ orbitals, the population of the $b_1g(d_{x^2-y^2})$ metal orbital being also important for the reduction of the $K_0$ value. Using this conclusion we can estimate $q_{ev}$ value. The resulting force constant can be calculated from the experimental data on the mean-square amplitude of the iron atom at different temperatures (Parak et al., 1982). This amplitude was attributed to the low-frequency iron out-of-plane movement (Li and Zgierski, 1992), and its force field constant can be calculated in the high-temperature limit from the relationship $\frac{1}{2}K(q^2) = \frac{1}{2}k_BT$, $K \approx 1.2$ eV/Å². The value of the vibronic constant, $f_{a_1g,a_2g} \approx 0.3$ eV, was calculated previously (Bersuker et al., 1979). The corresponding “crystal field” matrix element can be calculated using the data on the electronic structure of Fe(P) complexes (Zerner and Gouterman, 1966; Roos and Sundborn, 1970), $u_{a_1g,a_2g} \approx 0.3$ eV, and $\delta_{a_1g,a_2g} \approx 0.8$ eV (Zerner and Gouterman, 1966; Eaton et al., 1978). Using all these values, we obtain $q_{ev} \approx 0.16$ Å. Note that both $f_{a_1g,a_2g}$ and $u_{a_1g,a_2g}$ are proportional to the values of the iron and imidazole nitrogen charges. In the calculation we used the charges obtained by the extended Hückel technique, which underestimates charge separation in the complexes (Case et al., 1979). It implies that the calculation underestimates values of $q_{ev}$.
This estimation unequivocally shows that the electron-vibrational mixing of the $a_{2u}(\pi)$ and $a_{1g}(d_z)$ orbitals essentially contributes to the structure of the Fe(P) complexes, steric interaction between the porphyrin and axial ligand also being important. This fact explains qualitatively and semi-quantitatively a number of the experimental data on the iron displacement of the 3d$^6$ metalloporphyrin complexes, including its dependence on the kind of the metal, its spin and oxidation state, and the number and nature of the axial ligands (Bersuker and Stavrov, 1988). For example, only electronic reasons can explain the fact that in the complex of the Mn(P) with unhindered 1-methylimidazole (1-MeIm), the metal-porphyrin distance is 0.1 Å longer than in the Fe(P) complex with hindered 2-methylimidazole (2-MeIm). We must notice also that the conclusion (Olafson and Goddard III, 1977) that electronic interactions weakly contribute to the iron out-of-plane displacement, could be a result of a usage of four NH$_2$ groups in a plane to represent the porphyrin ligand of the Fe(P) molecule. In this model the $\pi$ conjugated electronic subsystem is absent at all. Consequently, the $a_{2u}(\pi) - a_{1g}(d_z)$ mixing which was shown to control the iron out-of-plane displacement in the Fe(P) complexes, in principle could not be taken into account in the study of the Fe(NH$_2$)$_2$ model.

In this work the influence of the $a_{1g}(d_z) - a_{2u}(\pi)$ mixing upon the displacement of the iron, $q$, on the electronic structure of the compounds under consideration is of particular interest for us. Therefore, first of all, we rewrite Eqs. 2–4, separating the contribution of these two orbitals

\[
q_{ev} = \left[ F^* + (p_{a_{1g}} - p_{a_{2u}}) \int_{b_{2u}} \frac{v_{b_{2u},a_{2u}}}{\delta_{b_{2u},a_{2u}}} \right] \times \left[ K^* - (p_{b_{1g}} - p_{b_{2u}}) \int_{b_{1g}} \frac{f_{b_{2u},b_{1g}}}{\delta_{b_{1g},b_{2u}}} \right]^{-1} \tag{5}
\]

where $F^*$ and $K^*$ include contributions from all the other orbitals. It is possible to see from Eq. 5 that, other things being equal, the greater value of $p_{b_{1g}} - p_{b_{2u}}$ and the smaller that of $\delta_{b_{1g},a_{2u}}$, the greater is $q_{ev}$. From Eq. 1 we obtain that the greater is $q$, the stronger is the $a_{2u}(\pi) - a_{1g}(d_z)$ mixture

\[
\psi_1(q) = a_{2u}(\pi) - \frac{v_{b_{2u},a_{2u}}}{2\delta_{b_{2u},a_{2u}}} a_{1g}(d_z) - \frac{f_{b_{2u},b_{1g}}}{2\delta_{b_{1g},b_{2u}}} a_{1g}(d_z)
\]

\[
\psi_2(q) = a_{1g}(d_z) + \frac{v_{b_{2u},a_{2u}}}{2\delta_{b_{2u},a_{2u}}} a_{2u}(\pi) + \frac{f_{b_{2u},b_{1g}}}{2\delta_{b_{1g},b_{2u}}} a_{2u}(\pi)
\]

and the greater are the decreasing of the $\epsilon_1(q)$ and increasing of the $\epsilon_2(q)$, values

\[
\epsilon_1(q) = \epsilon_{a_{1g}}(0) - \frac{v_{b_{2u},a_{2u}}^2}{2\delta_{b_{2u},a_{2u}}} - q \frac{f_{b_{2u},b_{1g}} v_{b_{2u},a_{2u}}}{2\delta_{b_{1g},b_{2u}}} - q^2 \frac{f_{b_{2u},b_{1g}}^2}{2\delta_{b_{1g},b_{2u}}} \tag{6}
\]

\[
\epsilon_2(q) = \epsilon_{a_{1g}}(0) + \frac{v_{b_{2u},a_{2u}}^2}{2\delta_{b_{2u},a_{2u}}} + q \frac{f_{b_{2u},b_{1g}} v_{b_{2u},a_{2u}}}{2\delta_{b_{1g},b_{2u}}} + q^2 \frac{f_{b_{2u},b_{1g}}^2}{2\delta_{b_{1g},b_{2u}}}. \tag{7}
\]

The direct quantum chemical calculation of the electronic structure of four-coordinated iron porphyrins (Zerner et al., 1966) showed that the 0.49-Å iron out-of-plane displacement strongly mixes (≈25%) the $a_{1g}(d_z)$ and $a_{2u}(\pi)$ orbitals, supporting the results of our approach. The origin of the mixing under consideration is illustrated in Fig. 2, wherefrom it is possible to see that the greater is the iron out-of-plane displacement, the greater is the overlap between the iron and the porphyrin MOs.

We used above a rather crude approximation, simulating the effect of the ligand coordination by its “crystal field” only. In reality, the covalent bond between the iron and the axial ligand is also very important. In the case of the imidazole complexes this means that the imidazole binding leads to the substitution of the approximately pure iron or imidazole orbitals by the mixed iron-imidazole MOs. In particular, the interaction between the iron $d_z$ and imidazole nitrogen $p_z$ orbitals leads to the formation of the bonding, mainly imidazole, $\sigma$(NHis+Fe), and antibonding, mainly iron, $\sigma$(Fe-NHis), MOs. The energy of the bonding MO is lower than the energy of the corresponding imidazole orbital and, consequently, the energy gap between this MO and the $a_{2u}(\pi)$ one is very large. Since the value of the mixing between any MOs is inversely proportional to the energy gap between them (Eq. 1), the intermixing of the $\sigma$(NHis+Fe) and $a_{2u}(\pi)$ MOs and its contribution to $q_{ev}$ (Eq. 4) is very weak. On the other hand, the strong mixing between the $\sigma$(Fe-NHis) and $a_{2u}(\pi)$ orbitals still takes place.

On the basis of this conclusion we can write for the $\psi_1(q)$ and $\psi_2(q)$ MOs

\[
\psi_1(q) = (c_{10} - c_{1g}q)a_{2u}(\pi) - (c_{20} + c_{2g}q)\sigma$(Fe-NHis) \tag{8}
\]

\[
\psi_2(q) = (c_{10} - c_{1g}q)\sigma$(Fe-NHis) + (c_{20} + c_{2g}q)a_{2u}(\pi),
\]

where the mixing of the orbitals under consideration with other orbitals is neglected, and the $c_i$ coefficients are expanded in powers of the small $q$ displacement, and only the terms up to linear to $q$ is conserved. In this expression the $c_{10}$ describes the static low-symmetry effect of the axial ligand coordination (in the absence of the fifth ligand or in the presence of two equivalent axial ligands $c_{10} = 1$ and $c_{20} = 0$),

FIGURE 2 Illustration of the origin of the $a_{1g}(d_z) - a_{2u}(\pi)$ overlap upon the iron displacement out of the porphyrin nitrogens plane.
and $c_{i q}q$ describes the effect of the iron out-of-plane displacement (at the point $q = 0$ this term vanishes). It is also possible to show from Eq. 5, that $c_{i 0}$ and $c_{i q}q$ are of the same sign.

It must be also stressed that in the preceding discussion mainly the electronic causes for the out-of-plane displacement in the complexes with one axial ligand were discussed. It is clear that steric repulsion between the axial ligand and the porphyrin ring must increase this displacement, the latter being strongly dependent on the strength of this repulsion. In the particular case of the five-coordinated iron porphyrin complexes with different imidazole ligands, the resulting iron out-of-plane displacement, $q_{0}$, is larger for the sterically hindered imidazoles than for the unhindered ones (Jameson et al., 1980; Momenteau et al., 1988). The $R \rightarrow T$ conformation transition in the Hb also increases the values of $q_{0}$ (Perutz et al., 1987; Perutz, 1989). Steric nonbonded interactions can affect the electronic structure of the compound only indirectly through the increase of the iron out-of-plane displacement. To take into account the effect of the steric interactions on the electronic structure we must calculate the electronic structure at the nuclear configuration, corresponding to the real structure of the compound. Since all the dependence of the electronic structure on geometry is described by the Eqs. 1, 2, and 6–8 we can determine the electronic structure of the compound, considering $q$ as a parameter. As it follows from Eqs. 6 and 8, the increase of $q$ due to the steric repulsion must result in a stronger $\sigma_{(Fe-NHis)} - a_{2u}(\pi)$ mixing.

3. MANIFESTATION OF THE IRON OUT-OF-PLANE DISPLACEMENT IN THE RESONANCE RAMAN SPECTRA OF THE HEME PROTEINS AND THEIR MODELS

According to the principle of resonance Raman, the frequency of the Raman band for a given mode of vibration is given by

$$p_{\nu}(q_{0}) = p_{1} + (p_{1} - p_{2})(2c_{i 0}c_{i q}q_{0} - c_{i 0}^{2})$$

where $p_{1}$ and $p_{2}$ are the population numbers of the $\psi_{1}$ and $\psi_{2}$ MOs, respectively. In the high- and intermediate-spin ground states $p_{1} = 2$, and $p_{2} = 1$, and in the low-spin ground state $p_{2} = 0$. Therefore, in the ground state $p_{1} - p_{2} \cong 0$, and an increase of the iron out-of-plane displacement increases the population of the $\sigma_{(Fe-NHis)}$ MO. Hence, the $Fe-NHis$ frequency must decrease upon increase of the iron out-of-plane displacement. This relationship between $q_{0}$ and $\nu_{(Fe-NHis)}$ was already observed experimentally (Desbois and Lutz, 1981; Desbois et al., 1981; Aragide et al., 1984). This result is also in excellent agreement with the results of the resonance Raman and x-ray diffraction studies of the model compounds (Table 1), wherefrom one can see, that an increase of the iron out-of-plane displacement systematically decreases the $\nu_{(Fe-NHis)}$ value.

At the same time it is very difficult, if at all possible, to explain the changes of the $Fe-NHis$ frequencies taking into consideration only the $e_{g}(\pi^{*}) - \sigma_{(Fe-NHis)}$ mixing (Bangcharoenpaurpong, 1984). Indeed, an increase of the tilt angle value, $\theta$, increases the overlap between the empty $e_{g}(\pi^{*})$ and the partially populated antibonding $\sigma_{(Fe-NHis)}$ orbitals, decreasing the population of the latter, which, as it follows from the BSC model, must increase the $\nu_{(Fe-NHis)}$ value. Comparing the data of the Table 1 for the iron porphyrin complexes with 2-MeIm or 1-MeIm, we see that very pronounced opposite changes take place. In general, substitution of 2-MeIm for 1-MeIm increases the $\theta$ angle (Jameson et al. 1980; Bangcharoenpaurpong, 1984; Momenteau et al., 1988) and essentially reduces the $Fe-NHis$ frequency, for example, it equals to 227 and 215 cm$^{-1}$ in FePocPiv(1-MeIm) and FePocPiv(2-MeIm), respectively (Hori and Kitagawa, 1980; Collman et al., 1983). These data imply that in the compounds under consideration the mixing of $\sigma_{(Fe-NHis)}$ and $e_{g}(\pi^{*})$ orbitals is weaker than the mixing of $\sigma_{(Fe-NHis)}$ and $a_{2u}(\pi)$ MOs and, as a result, the features of the $Fe-NHis$
bond depend mainly on the latter mixing. This conclusion was supported by our very recent quantum chemical calculations (Stavrov and Kushkuley, 1993), which show that the strength of the Fe–N_{H} \text{His} bond is controlled mainly by the iron out-of-plane displacement, the dependence on the azimuthal angle value, $\phi$, being negligibly weak at different values of $\theta$ between 0° and 20°. The tilt also affects the Fe–N_{H} \text{His} bond but rise of $\theta$ by 10° increases the strength of this bond approximately two times weaker than rise of $q_0$ by 0.1 Å decreases it.

As far as the Fe–N_{H} \text{His} distance is considered, we can conclude from Table 1, that this distance does not depend monotonically on the $q_0$. One of the possible reasons for this complicated dependence is that the steric repulsion affects the Fe–N_{H} \text{His} bond both directly, elongating the Fe–N_{H} \text{His} distance, and indirectly, changing the iron out-of-plane displacement, which also increases the distance under consideration.

The present approach also explains the higher Fe–N_{H} \text{His} frequency in the deoxy R state than in the deoxy T state of Hb (criterion 2) as a result of the increase of the iron out-of-plane displacement in the latter due to the protein globule tension (Perutz et al., 1987; Perutz, 1989). Note, however, that one must be very careful in comparing the $\nu(\text{Fe–N}_{\text{H}} \text{His})$ values for different types of heme proteins, because other mechanisms, such as weak hydrogen bond formation, can affect this frequency very pronouncedly (Teraoka and Kitagawa, 1981; Kitagawa, 1988). For example, on the proximal side of the heme pocket of sperm whale Mb there is a serine side chain, that is absent in Hb (Lesk and Chotia, 1980), and that can form an additional hydrogen bond to the proximal histidine (Takano, 1977a, 1977b). This bond can be responsible, at least partially, for the different temperature dependence (Rousseau and Friedman, 1988) of the Fe–N_{H} \text{His} band in Mb than in Hb.

The fact, that the increase of $q_0$ reduces the Fe–N_{H} \text{His} frequency, explains also the decrease of this frequency with time after the flash-photolysis of diatomic complexes of Hb (Rousseau and Friedman, 1988) as a manifestation of the incomplete relaxation of the heme (smaller $q_0$ values, than in deoxy Hb) immediately after photolysis and the relatively slow movement of the iron atom to its stable out-of-plane position. This explanation is also consistent with the analysis of the time (Murray et al., 1988) and temperature (Nienhaus et al., 1992) evolution of the near infrared 760-nm absorption band and of the frequencies of the porphyrin vibrations of Hb after photolysis (Dasgupta and Spiro, 1986; Rousseau and Friedman, 1988).

The value of the $\nu_4$ frequency is controlled by the population of the $e_g(\pi^\ast)$ MO (Spiro, 1988). This orbital is an antibonding orbital with respect to the pyrrole C−N bond of the porphyrin ring (Gouterman, 1959, 1978; Bangcharoenpaupong, 1984; Spiro, 1988). Its depopulation increases the C−N force constant, increasing the frequency of the porphyrin ring breathing $\nu_4$ vibration (Spiro, 1988). The displacement of the iron out of the porphyrin plane reduces the overlap between the iron $e_g(d_{z^\ast})$ and the porphyrin $e_g(\pi^\ast)$ MOs, reducing the charge transfer to the porphyrin $e_g(\pi^\ast)$ orbital and, consequently, increasing the $\nu_4$ frequency. Therefore, any change of the iron out-of-plane displacement per se must lead to the inverse relationship between changes of the frequencies of this mode and of the Fe–N_{H} \text{His} one (criterion 3). However, the maximal absolute value of the admixing of the $e_g(d_{z^\ast})$ MO to the $e_g(\pi^\ast)$ one is extremely small, $\approx 0.02$ (Zerner and Gouterman, 1966), and, consequently, its reduction upon the iron out-of-plane displacement cannot be strong. Therefore, the imidazole tilt, considered in the BSC model, can affect the $\nu_4$ frequency more pronouncedly. Because of small $e_g(\pi^\ast) - e_g(d_{z^\ast})$ mixing even weak charge transfer from $\sigma(\text{Fe–N}_{\text{H}} \text{His})$ to $e_g(\pi^\ast)$ must increase significantly the population of the $e_g(\pi^\ast)$ MO, reducing the $\nu_4$ value relatively strongly. It is the increase of the $\sigma(\text{Fe–N}_{\text{H}} \text{His}) \rightarrow e_g(\pi^\ast)$ charge transfer on going from Fe(TPivPP)(1-MeIm), $\theta \approx 5^\circ$, to Fe(TPivPP)-(1,2-Me_{2}Im), $\theta \approx 10^\circ$, that may explain the reduction of the $\nu_4$ frequency from 1355 to 1345 cm$^{-1}$ in these compounds (Hori and Kitagawa, 1980). In the model compounds under consideration the increase of the steric repulsion due to the substitution of 2-MeIm for 1-MeIm increases both the iron out-of-plane displacement and the imidazole tilt (Jameson et al., 1980; Momenteau et al., 1988), decreasing both the $\nu(\text{Fe–N}_{\text{H}} \text{His})$ and $\nu_4$ frequencies.

The protein can affect the histidine coordination geometry in another way, by changing mainly $q_0$, and only slightly the tilt angle, $\theta$. This must lead to the inverse relationship between the changes of the $\nu(\text{Fe–N}_{\text{H}} \text{His})$ and $\nu_4$ frequencies, the changing of the $\nu_4$ frequency being much smaller, than
in the methylimidazole containing model compounds. The dependence of these frequencies on several parameters can explain also their different relaxation kinetics in the photolyzed carbon monoxide complex of Hb (Rousseau and Friedman, 1988; Dasgupta and Spiro, 1986). Note also, that the \( \sigma(\text{Fe-NHis}) \rightarrow e_g(\pi^*) \) charge transfer can take place only in the compounds with populated \( \sigma(\text{Fe-NHis}) \) MO. Therefore, we can expect lower \( \nu_4 \) values in the high-spin iron compounds (\( \sigma(\text{Fe-NHis}) \) orbital is populated), than in the low-spin ones (\( \sigma(\text{Fe-NHis}) \) MO is empty), this conclusion being in agreement with the experimental results (Spiro, 1983).

All the results on the dependence of the Fe-NHis frequency on the heme structure prove that the iron displacement out of the porphyrin plane is the parameter which mainly controls this frequency (provided, obviously, that the protonation of the imidazole is not changed). Taking advantage from this result, we can use the data from the Table 1 to find an approximate (without taking into account of the effect of the simultaneous tilt of the imidazole) correlation between the \( \nu_0 \) and \( \nu(\text{Fe-NHis}) \) values:

\[
\nu (\text{cm}^{-1}) = 209.4 - 184.0[\nu_0(\text{Å}) - 0.4] \quad (10)
\]

Coordination of the second axial ligand dramatically increases the energy gap between the \( \sigma(\text{Fe-NHis}) \) and \( a_{2u}(\pi) \) orbitals (Eaton et al., 1978; Gouterman, 1978; Bersuker and Stavrov, 1988) and essentially reduces the low-symmetry axial “crystal field,” causing the iron to move closer to the porphyrin plane (Bersuker and Stavrov, 1988). All these effects strongly reduce the mixing between the \( a_{2u}(\pi) \) and \( \sigma \) orbitals, the latter now carrying contributions of the \( d_z^2 \) iron orbital and the \( \sigma \) orbitals of both axial ligands. Therefore in the hexacoordinated compounds the nature of the \( \sigma \) orbital is controlled mainly by the iron-axial ligand distance, which in proteins weakly depends on their conformation (Liddington et al., 1988), and in model compounds on the steric interaction with the fifth ligand (Jameson et al., 1980; Momenteau et al., 1988). That is why the trans-effect of the fifth ligand coordination geometry depends only weakly on the protein conformation, which can explain the weakness or absence of change of the Fe-O2 vibrational frequency upon the changing the protein conformation (criterion 6).

**Intensities**

The first, fourth, and fifth criteria mentioned above deal with the intensity of the Fe-NHis band upon excitation in the Soret band region. The considerable intensity of the Fe-NHis band implies that the characteristics of the adiabatic surfaces (the iron-imidazole distance, force field constant, etc.) of the ground state, GS, and the corresponding excited B state, must be different. This means, in turn, that in the B state the electronic population of the \( \sigma(\text{Fe-NHis}) \) orbital is notably changed. The necessary condition for this, is a participation of the \( \sigma(\text{Fe-NHis}) \) orbital in the excitation. Such a participation really takes place in the compounds with one axial ligand due to the mixing of the \( a_{2u}(\pi) \) and \( \sigma(\text{Fe-NHis}) \) orbitals. Coordination of the second axial ligand, as it was mentioned, strongly reduces the mixing between these orbitals, leading to the weak or vanishing coupling of the Fe-NHis mode to the Soret resonance (criterion 5).

To prove, that in the five-coordinated compounds the intensity of the Fe-NHis band is strong enough to be observable, we must show, that the electronic populations of the \( \sigma(\text{Fe-NHis}) \) orbital in the ground and the B states are essentially different. According to the four-orbital model (Gouterman, 1959, 1978) any component of the doubly degenerated B state of the iron-porphyrin complex can be written as the sum of two determinants

\[
B_{\alpha(\beta)} = \frac{1}{2} \left[ |\psi_1^{(1)} e^{(1)}_{\alpha(\beta)}| + |\psi_2^{(1)} e^{(1)}_{\alpha(\beta)}| \right] \quad (11)
\]

where only the MOs whose populations change upon the excitation are listed and the mixing between the \( a_{2u}(\pi) \) and \( \sigma(\text{Fe-NHis}) \) orbitals is already taken into account. It is simple to see from Eq. 11 that in the B state the \( \psi_1 \) electronic population, \( p_1 \), equals to 1.5 instead of 2 in the ground state, the \( p_2 \) value remaining the same, \( p_2 = 1 \). Keeping this in mind and using Eq. 9 we can write for the \( \Delta p_\sigma = p_B(\sigma) - p_G(\sigma) \):

\[
\Delta p_\sigma = -0.5[2c_{10}c_{14}(q_G^0 - q_B^0) - c_{10}^2] \quad (12)
\]

where \( q_{1a}^{(1)} \) and \( q_{1b}^{(1)} \) are the iron out-of-plane displacement in the ground and B states. Assuming that these displacements are equal \( q_{1a}^{GS} = q_{1b}^0 = q_0 \) we can rewrite Eq. 12

\[
\Delta p_\sigma = -0.5(2c_{10}c_{14}q_0 - c_{10}^2). \quad (13)
\]

Using results (Zerner et al., 1966) it is possible to estimate the population values for \( q_0 = 0.49 \) Å; \( p_\sigma(\mathrm{GS}) \approx 1.25 \), \( p_\sigma(B) \approx 1.12 \), and \( \Delta p_\sigma \approx -0.13 \). We see that the population of the \( \sigma(\text{Fe-NHis}) \) MO is reduced essentially by the Soret excitation, which causes the reduction of the Fe-NHis distance and force field constant, leading to the strong coupling of the Fe-NHis vibration to the Soret resonance (criterion 1).

It also follows from Eq. 13, that the greater is \( q_0 \) in the ground state, the greater is \( \Delta p_\sigma \) and, consequently, the greater must be the Fe-NHis band intensity. It means that the smaller is the frequency of the Fe-NHis band, the greater must be its intensity. Experimental data, however, show no monotonic dependence between the frequency and intensity of the Fe-NHis band (Nagai and Kitagawa, 1980; Nagai et al., 1980; Sassaroli et al., 1986; Rousseau and Friedman, 1988; Friedman et al., 1990; Ahmed et al., 1991; Bosenbeck et al. 1992). In general this experimental fact means, that the frequency and intensity of the Fe-NHis band are governed not only by the ground state \( q_0 \) value but by other factors, too. It was mentioned above, that the hydrogen bond between the proximal histidine and the protein globule can affect the Fe-NHis frequency: the stronger the bond, the higher is the frequency. Therefore, if upon the out-of-plane iron movement a strengthening of the hydrogen bond takes place, it can compensate the reduction of the Fe-NHis frequency and only
weakly affect the corresponding intensity, leading to the apparent absence of relationship between the frequency and intensity. A tilt of the imidazole can be considered as another parameter, which increases both the frequency and the intensity. From this point of view a lack of dependence between the position and the intensity of the Fe-NH$_3$ band in different heme proteins (Friedman et al., 1990) can be caused by a simultaneous change of the iron out-of-plane displacement and the histidine tilt. In this case we still must assume, that the histidine tilt is changed significantly more, or the iron displacement is changed significantly less, than in the model compounds, where a reduction of the Fe-NH$_3$ frequency due to the increase of $q_0$ strongly exceeds its decrease due to the tilt (see Table 1). This hypothesis, however, does not agree with the inverse relationship between the Fe-NH$_3$ and $v_4$ frequencies, discussed above. Friedman et al., 1990 proposed an azimuthal angle $\phi$ (Fig. 1) controlling the overlap between the iron $4p_{\pi}$ and imidazole $\pi_m$ orbitals as a parameter, governing the intensity and not the frequency. This assumption does not look well-founded, because the change of the $4p_{\pi}$-$\pi_m$ overlap population upon the $\phi$ change from 0° to 45° is very small itself being less than 0.01 e$^-$(Scheidt and Chipman, 1986). The Fe-NH$_3$ band intensity is affected by the mixing of the porphyrin and iron-imidazole electron sub-systems and, consequently, the intensity is governed by the change of overlap population between the imidazole $\pi_m$ and porphyrin $\pi$ orbitals. This population depends on $\phi$ even weaker than the $4p_{\pi}$-$\pi_m$ overlap population, because it is proportional to the latter one multiplied by the very weak overlap between the iron $4p_{\pi}$ and the porphyrin $e_g(\pi^*)$ orbitals.

All the parameters discussed above are the ground state parameters of the compounds under consideration. At the same time there is one more possible reason for the complicated relationship between the Fe-NH$_3$ frequency and intensity. We must recall, that the expression (Eq. 13) was obtained under the assumption that $q_0$ is the same in the ground and B states. To test this assumption we must consider the expression (Eq. 5) for the B state. Using Eq. 11 for the iron-in-plane nuclear configuration we can easy show, that in this state the effective population of the $a_{2u}(\pi)$ MO is 1.5, instead of 2 in the ground state. Since $q_{ev}$ decreases upon a decrease in the $p_{a_{2u}} - p_{a_{1g}}$ value (Eq. 5), it follows that due to the electronic causes the $q_{ev}^{GS} > q_{ev}^{FS}$. If the $q_0$ had been controlled only by electronic effects this difference could only increase $\Delta p_{\alpha}$, increasing the Fe-NH$_3$ band intensity. However, it was noted in Section 2 that the steric repulsion or/and protein tension can considerably increase the $q_0$ value comparing to the $q_{ev}$ one. These interactions reduce the approaching of the iron atom to the porphyrin plane in the excited state and, consequently, reduce the Fe-NH$_3$ band intensity. Thus, in compounds where the steric interactions play an important role, the intensity under consideration can be smaller than in compounds where the steric interactions are weak enough.

This conclusion can be proved using Eq. 12. Let us consider first the compounds where the steric interactions between the axial ligand and the porphyrin are weak enough to be neglected, $r$ compounds. For the sake of simplicity we will take into account only a contribution of mixing the $a_{1g}(d_z)$ and $a_{2u}(\pi)$ orbitals into the $q_{ev}$ value, $F^* = 0$ (5). In this case the iron out-of-plane displacement is controlled only by the electronic interactions, $q_{a_{2u}} = q_{ev}$, and is proportional to $p_{a_{1g}} - p_{a_{1u}}$. Consequently, $q_{a_{2u}} = 1/2 q_{ev}^{GS}$, and we obtain from Eq. 12

$$\Delta p_{\alpha, r} = -0.5(3c_{10}c_{14}q_{ev}^{GS} - c_{10}^2).$$

(14)

In the opposite situation ($t$ compounds) when the steric interactions are much stronger than the electronic ones, the change of the iron out-of-plane displacement upon the excitation of the system into the B state is negligibly small. In this case the value of $\Delta p_{\alpha, r}$ is determined by Eq. 13. An expression for the difference between the absolute values of the $\Delta p_{\alpha, r}$ and $\Delta p_{\alpha, t}$ can be obtained from Eqs. 13 and 14,

$$|\Delta p_{\alpha, t} - \Delta p_{\alpha, r}| = c_{10}c_{14}(2q_{ev}^{GS} - q_{ev}^{GS}).$$

(15)

and can be positive even if $q_{ev}^{GS} > q_{ev}^{FS}$. Consequently, the intensity of the Fe-NH$_3$ band can be greater in the $r$ compound than in the $t$ one even if $q_{ev}^{GS} > q_{ev}^{FS}$. If in both compounds the steric interactions are strong (both compounds are of $t$ type (Eq. 13)) or weak (both compounds are of $r$ type (Eq. 14)) the larger $q_{ev}^{GS}$ is the stronger must be the Fe-NH$_3$ intensity. Certainly, upon the elaboration of the expressions (Eqs. 12–15) a quit crude approximation was used. In real complexes the intermediate situation takes place and the relationship between the $q_0^{GS}$ and the intensity and, consequently, between the Fe-NH$_3$ frequency and intensity, can be very complicated.

The contribution of the steric and electronic interactions to the value in the different protein conformations can be estimated from the comparison of the ground state Fe-NH$_3$ vibrational frequencies. The small reduction of $\nu(\text{Fe-NH}_3)$ upon the $R \rightarrow T$ conformational transition implies that the protein tension is weak in both conformations. Consequently, the electronic effects prevail in both T and R conformations (both compounds are of the $r$ type) and the Fe-NH$_3$ band intensity must be greater in the T conformation, than in the R one. Significant reduction of $\nu(\text{Fe-NH}_3)$ upon the $R \rightarrow T$ conformational transition means that the opposite situation occurs, the protein tension in the T conformation is strong and essentially contributes to the iron out-of-plane displacement (t type compound), in the R conformation the $q_0$ still being mainly controlled by the electronic effects ($r$ type compound). In this case the Fe-NH$_3$ intensity can be stronger in the R conformation than in the T one. For example, the R conformation of the valency hybrid Hb $\alpha^\text{CN}$ can be changed to the T one by decreasing the $p$H value from 9.0 to 6.5 and addition of inositol hexaphosphate (Nagai and Kitagawa, 1980). This conformational transition slightly reduces the $\nu(\text{Fe-NH}_3)$ value from 224 to 220 cm$^{-1}$, implying that the protein tension in the T conformation is weak, the electronic effects prevail (both conformations belong to the $r$ type compounds) and the Fe-NH$_3$ band intensity must be
stronger in the T conformation of the protein: this is really the case (Nagai and Kitagawa, 1980). The opposite situation takes place in another valency hybrid Hb, $\alpha^2_2\beta^2_2\alpha^+CN$, which shows a strong shift of the $\nu$(Fe-NHis) from 222 to 207 cm$^{-1}$ on going from the R to T conformation. This means that in the T conformation the protein tension is rather strong (t compound), the R conformation being of the r type. This conclusion explains the higher intensity of the Fe-NHis band in the R conformation of the protein than in the T one (Nagai and Kitagawa, 1980).

In general the complicated dependence of the Fe-NHis band intensities on the protein conformation can be explained as the result of the interplay between the electronic and steric (or protein tension) effects in the systems under consideration. From this point of view the extent and direction of the imidazole tilt can be very important, because they can change dramatically the steric interaction between the histidine and the porphyrin plane, essentially affecting the Fe-NHis band intensity.

It follows also from Eq. 7 that an increase of $q$ lowers $\epsilon_1$ energy of the $\psi_1$ orbital. At the same time the Q and Soret absorption bands of metalloporphyrins correspond to the $\psi_1$, $a_{1u}(\pi) \rightarrow e_g(\pi^*)$ excitations strongly mixed by the configuration interaction (Gouterman, 1959, 1978). Therefore, if the $e_g(\pi^*)$ energy weakly depends on $q$, the decrease of the $\epsilon_1$ must lead to the blue shift of both bands. The imidazole tilt increases the energy of the $e_g(\pi^*)$ MO also leading to the blue shift of the B and Q bands (Bangcharoenapuropong, et al., 1984). Such a blue shift was indeed observed in the Fe-(PocPiv)(Im) complexes upon the substitution of 2-Melm for 1-Melm (Collman et al., 1983), and on the R $\rightarrow$ T conformational transition of Hb (Perutz et al., 1974).

4. CONCLUSION

In this paper the influence of the iron displacement out of the plane of the porphyrin nitrogen in heme proteins and iron porphyrin complexes on their electronic structure was studied using the vibronic theory. It was shown that this displacement crucially mixes the iron-imidazole and porphyrin electronic subsystems, leading to the strong coupling of the Fe-NHis vibration to the porphyrin $\pi \rightarrow \pi^*$ excitations. The spectroscopic and structural manifestations of the theoretical results, obtained in this work, are in a good agreement with a number of experimental data, which stresses the crucial role of the iron out-of-plane displacement for the understanding of the features of the systems under consideration.

It also follows from our analysis that the tilt of the imidazole ligand itself can not explain a very important piece of the experimental data: the relationship between the Fe-NHis frequency and the geometry of the model compounds. Therefore we can state that, as far as the heme geometry is considered, the features of the resonance Raman Fe-NHis band of the compounds of interest depend mainly on the value of the iron out-of-plane displacement, the imidazole tilt being able to modulate this dependence mostly indirectly, changing the iron displacement. Thus, the position of the resonance Raman Fe-NHis band of heme proteins in different conformations contains mainly information on the dependence of the iron out-of-plane displacement on the conformation of the protein, which was shown to be very important for the understanding of the binding of small molecules to heme proteins (Perutz et al., 1987; Liddington et al., 1988; Šrajer et al., 1988).

All the obtained results are qualitative or semiquantitative. The direct quantum chemical calculations of the dependence of the electronic structure and vibrational frequencies on the iron out-of-plane displacement and geometry of the imidazole coordination in the compounds under consideration, are now in progress.

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REFERENCES


