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Motion Estimation with Finite-Element Biomechanical Models and Tracking Constraints from Tagged MRI

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Abstract

Noninvasive measurements of tissue deformation provide bio-mechanical insights of an organ, which can be used as clinical functional biomarkers or experimental data for validating computational simulations. However, acquisition of 3D displacement information is susceptible to experimental inconsistency and limited scan time. In this research, we describe the process of tracking tagged magnetic resonance imaging (MRI) as enforcing harmonic phase conservation in finite-element (FE) models. This concept is demonstrated as a tool for motion estimation in a brain motion phantom, the heart, and the tongue. Our results demonstrate that the new methodology offers robustness to edge and large-displacement artifacts, and that it can be seamlessly coupled with numerical simulations for estimating fiber stretch in residually stressed tissue, or for inverse identification of muscle activation.

Introduction

Soft tissue deformation elicits vital transport processes throughout the body, and is a key determinant in widespread conditions and diseases. For example, systemic circulatory deficiencies may arise from impaired myocardial contraction, and acceleration-induced axonal overstretching has been linked to traumatic brain (Phatak et al. 2009; Wright and Ramesh 2012) and can be investigated using MRI. Thus, noninvasive motion estimation is of clinical and investigational interest. However, the acquisition and processing of tagged MRI has been problematic due to long scan times, artifacts, and challenges in obtaining accurate 3D estimates of displacement and strain. It has been shown that integration of an organ's geometry (and fiber orientations if relevant) and use of material constitutive information can increase estimation accuracy, reduce artifacts, and improve one's ability to estimate dense displacements and strains from sparsely acquired imaging data (Haber et al. 2000; Phatak et al. 2009).

Motivated by versatile contrast and unparalleled soft tissue sensitivity, several motion estimation approaches have been developed within the MRI framework, as well as dedicated motion encoding pulse sequences, image postprocessing, or both (Ibrahim 2011). Analysis of tagged MRI is one of the most well-established approaches which, from early implementations targeting the cardiovascular system, has expanded to include other organs (Bayly et al. 2012; Moerman et al. 2012; Harandi et al. 2015).

Best results in 3D motion estimation generally require consistent repetition of movement and relatively high resolution, but these are constrained by scan time (Spottiswoode et al. 2007; Knutsen et al. 2014). Traditionally, displacement information has been reconstructed in the imaging planes first and then propagated to a 3D domain with the help of interpolation methods, such as splines, or finite elements (Haber et al. 2000; Liu et al. 2012). These approaches enable preemptive reduction of artifacts via smoothing or refinement, and enforce incompressibility during the interpolation process (Liu et al. 2012). However, the imaging raster rarely aligns with the geometry or fiber structure of an organ; thus, smoothing or interpolation may introduce fictitious edge tractions, or violate other mechanical characteristics such as tissue anisotropy.

In this research, the tracking process is realized by enforcing image phase conservation in material points within the field of view (FOV), but not coincident with the spatial imaging raster. The proposed tracking kernel is based on the classic harmonic phase (HARP) analysis of tagged MRI (Osman et al. 2000), combined with hyperelastic model registration methods (Phatak et al. 2009), according to a phase conservation principle parallel to intensity conservation in optical flow (Horn and Schunck 1981). Thus, the results are *mechanically representative*, in that they are diffeomorphic, have traction free surfaces, and are otherwise consistent with continuum mechanics, but the phase vector formulation increases sensitivity in texture-free regions, and provides a more objective similarity metric.

We demonstrate our implementation in three scenarios. The first two consist of forward displacement reconstruction where the goal is to obtain deformation fields. These include: measurement of impact-induced deformation in a Sylgard™ brain phantom and quantification of fiber strain in residually stressed myocardium. The third scenario consists of displacement-based inverse parameter identification of intrinsic tongue muscle activation. Our results indicate that, in forward displacement reconstruction, the approach is robust to artifacts (edges and large-displacements) and to material stiffening due to residual stress. In the inverse problem, we show that evaluating fiber stretch enables approximation of muscle activation without the need for iterative minimization.

Background

Harmonic Phase Analysis

Tagged MRI contains artificial magnetic patterns (lines or sinusoidal profiles) that are imposed near the beginning of a CINE sequence and deform with moving tissue. HARP analysis focuses on harmonic peaks in the Fourier domain, which arise from the periodic nature of tag patterns. The harmonic phase vector, $\phi = [\phi_1 \quad \phi_2 \quad \phi_3]^T$, where each term is the phase of the inverse Fourier transform of a harmonic peak in an image whose tag

direction is orthogonal to the other two, carries information about local components of tissue motion. In particular, the phase at a reference location, $\mathbf{X}$, at $t = t_0 = 0$ will be the same as tissue moves to a new spatial location, $\mathbf{x}$, at a later time. In other words,

$$\phi(\mathbf{X}, t_0) = \phi(\mathbf{x}, t) \quad (1)$$

Thus, 3D motion estimation can be thought of as the solution of a multidimensional, nonlinear, root-finding problem: given phase distributions at two time points, find $\mathbf{x}$ for a given $\mathbf{X}$, or vice versa.

We note that a practical application of HARP analysis deals not with the true real-valued phase, but rather with the *harmonic phase* whose range is the interval $[-\pi, \pi)$. Nevertheless, it is possible to use the expressions herein without loss of generality by adopting local phase unwrapping in the final implementation (Osman et al. 2000).

Deformations in Continuum Mechanics

Tissue deformation can be modeled as a boundary problem seeking to minimize an elastic energy functional $E(\boldsymbol{\sigma})$, where the deformation map $\boldsymbol{\sigma}$ contains admissible deformations evaluated at material points i.e., $\boldsymbol{\sigma}(\mathbf{X}) = \mathbf{x} = \mathbf{X} + \mathbf{u}(\mathbf{X})$ (Phatak et al. 2009). Given an integration domain, $\mathcal{R} \in \mathbb{R}^3$, the Euler-Lagrange equations necessary to minimize are obtained by taking the directional derivative with respect to a small variation (or virtual displacement) in the spatial coordinates. This yields the weak form of the so-called virtual work equation,

$$\delta W = \int_{\mathcal{R}} \mathbf{P} : \delta \dot{\mathbf{F}} \, dV - \int_{\mathcal{R}} \mathbf{f}_0 : \delta \mathbf{v} \, dV + \int_{\mathcal{S}} \mathbf{t}_0 : \delta \mathbf{u} \, dS. \quad (2)$$

At equilibrium, $\delta W = 0$, describes a static momentum balance between body or boundary forces (respectively $\mathbf{f}_0$ and $\mathbf{t}_0$), and internal stresses defined by the material-dependent second Piola-Kirchhoff stress tensor, $\mathbf{P}(\mathbf{F})$, and the spatial gradient of the deformation map, $\mathbf{F} = \frac{d\mathbf{x}}{d\mathbf{X}}$ (Bonet and Wood 1997; Phatak et al. 2009).

One of the most popular approaches for solving the boundary problem associated with (2) is FE analysis. This process generally involves extracting discretized geometry from MRI via delineation and meshing, assigning a suitable constitutive model, and defining boundary conditions. The FE method has experienced considerable expansion in biomechanics thanks to several improvements geared to handle complex biological geometries, and nonlinear material models (Bonet and Wood 1997; Maas et al. 2012).

Tracking Tagged MRI with Deformable Models

Conservation of Harmonic Phase Vector

The basis of HARP analysis, (1), can also be described through physical conservation principles. Let ϕ represent a vectorial angular quantity (per unit mass), which is conserved. Then, the net change in phase density can be expressed as a mass transport process defined in weak form by

$$\frac{D}{Dt} \int_{\mathcal{R}} \phi \rho \, dV - \int_{\mathcal{R}} \frac{\partial(\phi \rho)}{\partial t} \, dV + \int_{\mathcal{S}} \rho \phi \otimes \mathbf{v} \cdot \mathbf{n} \, dS, \quad (3)$$

where the right hand side contains generative and advection terms dependent on mass density ρ and velocity $\mathbf{v}$ across a boundary surface with local normal $\mathbf{n}$ (Spencer 1985). Application of Gauss' theorem and the continuity equation reduces the phase conservation relationship to

$$\frac{D\phi}{Dt} = \frac{\partial\phi}{\partial t} + \nabla\phi \cdot \mathbf{v}. \quad (4)$$

The left side of the equation corresponds to the material description, which yields the deformable model tracking constraint discussed in the next section. The middle expression is equivalent to the spatial description, and is the harmonic phase equivalent of the familiar optical flow equation used in intensity-based image registration (Horn and Schunck 1981).

Nonlinear Tracking Constraint

We now focus on obtaining displacements using the material description of harmonic phase conservation noting that direct application of (1) has two key limitations: First, harmonic phase vector pairs are not unique as a consequence of phase wrapping, thus tracking may converge at erroneous locations after large displacements; second, without regularization, tracking points near edges will result in spurious displacements due to partial volume artifacts.

Definition—Using integration with respect to time, the total derivative in (4) can be formulated as a difference between two phase images, acquired at the reference and at a subsequent time, evaluated at a material point and its corresponding location in the deformed configuration i.e., $\mathbf{x} = \mathbf{x}(\mathbf{X}, t)$. This difference defines the nonlinear tracking constraint to be imposed on (2),

$$f_{\text{harp}} = \lambda(t) (\phi(\mathbf{x}(\mathbf{X}, t), t) - \phi(\mathbf{X}, t_0)), \quad (5)$$

where $\lambda(t)$ is a Lagrange multiplier that enforces phase consistency in tracking. In essence, the constraint introduces an additional body force whose purpose is to deform the model according to the temporal changes in the tag patterns.

Implementation—Given the nonlinear nature of (5), implementation within a Newton–Raphson (or similar) iterative solver requires consistent linearization of the virtual work contribution from the constraint to be applied on (2). In other words, linearizing $D\delta W_{\text{harp}}(\mathbf{x}, \delta \mathbf{v})[\mathbf{u}] = \int_{\mathcal{R}} \mathbf{f}_{\text{harp}} \cdot \delta \mathbf{v} dV$ yields the tangent stiffness aggregate to be passed along to the solver i.e.,

$$D\delta W_{\text{harp}}(\mathbf{x}, \delta \mathbf{v})[\mathbf{u}] = \int_{\mathcal{R}} \lambda(t) \nabla \phi(\mathbf{x}(\mathbf{X}, t), t) \delta \mathbf{v} \cdot \delta \mathbf{u} dV. \quad (6)$$

The tracking constraint was implemented as a plug-in extension to the FE solver within the FEBio Software Suite (Maas et al. 2012).

Image Preprocessing—In (5), it is assumed that the harmonic phase images are defined everywhere, which typically is not the case. Therefore, an image interpolation step must be built into the implementation. In fact, we propose upsampling tagged images prior to harmonic peak extraction (effective bandwidth remains limited by the original acquisition). In this experiments, we used grid-based cubic spline interpolation to achieve isotropic resolution based on the in-plane slice resolution. As with conventional HARP analysis, band-pass filtering is necessary to extract harmonic peaks. In this research, each 2D slice was filtered one image at a time, with a circular band-pass filter centered at the tagging frequency with a radius equal to half of the center frequency (Osman et al. 2000).

Solution Strategy—Two main approaches for enforcement of tracking constraints are available in this implementation. The first consists of applying a global, linearly increasing, penalty $\lambda(t)$ function (penalty method), and the second consists of using an iterative approximation to its local values to a given tolerance (augmented Lagrangian) (Guo et al. 2012). Both the maximum penalty λ_{max} , and tolerance λ_{tol} were adjusted according to a desired tracking residual $\varepsilon = \int \phi(\mathbf{x}(\mathbf{X}, t), t) - \phi(\mathbf{X}, t_0) dV$.

Experiments and Results

Measuring Impact-Induced Deformation in Brain Phantom

The goal of this experiment was to demonstrate our approach against traditional HARP analysis i.e., application of (1) with a fixed-point algorithm, for reconstructing the motion of a Sylgard™ phantom, Fig. 1(a). The phantom's base was subject to a sudden rotational acceleration and consequently imaged (3T scanner, 13 frames, 18 ms TR, 13 axial slices, 160×160 px, 1.5×1.5mm, SPAMM sequence). The FE model of the phantom consisted of 4250 linear brick elements, of a Neo-Hookean solid ($C_1 = 1.0$ kPa, $k = 120$ kPa). Tracking was performed to $\varepsilon = 0.05$ rad, with $\lambda_{\text{max}} = 0.2$, and $\lambda_{\text{tol}} = 0.1$. Both algorithms ran for 10 iterations per time frame.

Representative displacements at $t = 54$ ms appear in Figs. 1(c) and 1(d). As expected, using a fixed point algorithm results in two types of artifacts: spurious displacements near the edges, and erroneous tracking due to large displacements. In contrast, the proposed methodology results in smooth (traction-free) displacements at the boundaries, and consistent tracking of rotation.

Quantifying Fiber Stretch in Residually Stressed Myocardium

Most tissues exhibit some level of residual stress, which becomes apparent by recoil following an incision, suggesting that fibers in situ are (pre)stretched when unloaded (Genet et al. 2015). Here, we (a) demonstrate that our approach may include modeled prestretch via interstitial growth (Ateshian and Ricken 2010), and (b) evaluate changes in tracking results due to prestretch-induced stiffness variations. To this end, the left ventricle of a healthy volunteer was imaged (3T scanner, 12 long slices, 8 long slices, 256×256 , 1.25×1.25 mm, CSPAMM sequence), and images at early diastole (lowest pressure load), were used to generate an FE model consisting of 6500 linear brick elements. Simulated contraction, with parameters available in (Phatak et al. 2009; Genet et al. 2015), was used as ground truth displacements, and to create synthetic deformed images for tracking.

Two displacement results were obtained with a stress-free reference (SFR), and a prestretched reference (PSR), which included -5% mean fiber prestretch (Ateshian and Ricken 2010; Genet et al. 2015). In both, tracking was performed to $\epsilon = 0.2$ rad. Tracking from SFR terminated after 17 iterations using $\lambda_{\max} = 0.2 \times 10^{-2}$, and $\lambda_{\text{tol}} = 5 \times 10^{-2}$. The same values for PSR after 10 iterations were 1.4×10^{-2} , and 7×10^{-2} , respectively. Compared to the ground truth, the displacement residuals were 0.6 ± 0.3 mm and 0.9 ± 0.3 mm (SFR and PSF, respectively). This similarity in residuals shows that prestretch-induced variations can be compensated by tracking parameters. Thus, although the image-derived deformed configurations are similar, the PSF relates to a reference state consistent with experimental evidence of residual stress, Fig. 2(a), and results in visibly higher systolic fiber shortening, Figs. 2(b) and 2(c).

Estimating Activation of Intrinsic Tongue Muscles

In this experiment we aimed at estimating the magnitude of activation stress responsible for an observed deformation in the tongue. To this end, motion was first tracked based on a stack of images from a healthy volunteer at two time frames (3T scanner, 10 coronal slices, 8 sagittal slices, 256×256 , 1.9×1.9 mm, CSPAMM sequence) using a FE model consisting of 280 quadratic brick elements, and the tracking constraint set to $\epsilon = 0.05$ rad. To obtain contractile stress normalized to material stiffness, the tissue was modeled as a Neo-Hookean solid ($C_1 = 1.0$ kPa, $k = 120$ kPa). Fiber directionality, and muscle definitions were based on the literature (Harandi et al. 2015). Unlike previous work, which relied on numerical optimization, i.e., where multiple simulations were run to find the closest match between simulated and observed tongue deformation, our strategy was to directly approximate the contractile stresses from the image-derived fiber shortening according to the active contraction model presented in (Phatak et al. 2009) (solving for $T_{\max}$ in Eqn. 4). These approximations were applied uniformly over each of the muscles in Fig. 3(a).

Image tracking, the basis of the observed tongue deformation, terminated after 10 iterations $\lambda_{\max} = 1.0$, and $\lambda_{\text{tol}} = 0.1$. Displacement results appear on Fig. 3(b). Experimental as well as simulated fiber stretches averaged over the muscle region appear in Fig. 3(c), and show qualitative agreement. Comparison between the image-based deformation, and activation simulation allows direct estimation of contractile stress, avoiding numerical optimization, which may converge at local minima (Harandi et al. 2015). Note that both, forward simulations, and image tracking via the proposed phase tracking constraint, occur in the same geometrical model; thus, comparison between experimental and simulated behavior can be done in an element-per-element basis.

Discussion

This study extends fundamental concepts used for motion estimation based on scalar intensity images to the vectorial phase domain, which allows application of tagged images for mechanically regularized motion estimation. One immediate advantage of this type of regularization is the reduction of artifacts present at the edges where image information is affected by partial volume. The use of tagged images disambiguates similarity metrics associated with intensity in areas of low texture. This improves motion tracking, and adds robustness to material parameter uncertainty.

As shown in previous literature featuring intensity-based motion estimation in FE models (Phatak et al. 2009), displacements can be made consistent despite changes in material parameters by scaling the tracking penalty. The idea is that, within a range, a stiffer material will simply require larger forces to produce the same deformation. In the proposed method, we take advantage of the vectorial nature of phase to extract a similarity metric, ϵ , that serves as a stopping criteria for motion estimation; the tracking penalty continues to be scaled until the criteria is met. This basic principle was demonstrated when tracking deformation in residually stressed ventricular tissue, where the tracking parameters associated with the PSR were much larger than the SFR, even though the tracking metric and displacement accuracy were similar.

In terms of implementation, the proposed method effectively reduces to calculating body forces derived from phase images, i.e. the application of nodal forces where each (xyz) component is equal to scaled differences between template and target phase image in each corresponding tagging direction. The stiffness contribution, evaluated once per element, is defined similarly to the contribution of the material model but is defined as described in (6). From an image processing standpoint, upsampling of images enables the use of advantageous interpolation techniques that would be computationally expensive to evaluate along with the FE tracking constraint.

Conclusion

The main goal of this paper was to introduce and demonstrate unique features associated with this motion estimation strategy, including artifact reduction, robustness to material parameters, and interaction between observed motion and mechanical features like realistic geometry and fibers. Future research directions will focus on the relative performance of its

different components, both from an imaging standpoint (the effects of image quality, interpolation, and filtering), and from a modeling perspective (the consequences of constitutive modeling, and geometrical representation), and with respect to other motion estimation techniques.

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Fig. 1.

Acceleration-Induced Brain Phantom Deformation. As shown in the schematic (a), motion of the base causes deformation into a new configuration (b). Conventional HARP analysis (c) contains artifacts that do not appear with proposed method (d).

Fig. 2.

Comparison between SFR and PSR. A radial cut (a) on a ring-like section shows no change in the SFR, but the same cut causes separation of edges in the PSR, similar to experimental observations (Genet et al. 2015). Comparable deformed configurations exhibit different fiber stretches with respect to the SFR (a) or the PSR (c).

Fig. 3.

Motion estimation in the tongue. A FE model including five muscles (a), was used to extract deformation from MRI (b), and to simulate it via activation stresses. Measured and simulated fiber stretches (c) show qualitative agreement. key: GG=genioglossus, IL=inferior longitudinal, SL= superior longitudinal, T=transverse, V=verticalis M=mandible insertion.