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Energy accommodation coefficient extracted from acoustic resonator experiments

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Abstract

We review values of the temperature jump coefficient ζ_T determined from measurements of the acoustic resonance frequencies f_{acoust} of helium-filled and argon-filled, spherical cavities near ambient temperature. We combine these values of ζ_T with literature data for tangential momentum accommodation coefficient (TMAC) and the Cercignani-Lampis model of the gas-surface interaction to obtain measurement-derived values of the normal energy accommodation coefficient (NEAC). We found that NEAC ranges from 0 to 0.1 for helium and from 0.61 to 0.85 for argon at ambient temperature for several different surfaces. We suggest that measurements of f_{acoust} of gas-filled, cylindrical cavities and of the non-radial modes of quasi-spherical cavities might separately determine TMAC and NEAC. Alternatively, TMAC and NEAC could be determined by measuring the heat transfer and momentum transfer between parallel rotating discs at low pressure.

Keywords

Acoustic resonator; temperature jump coefficient; tangential momentum accommodation coefficient; normal energy accommodation coefficient; rarefied gas

I. INTRODUCTION

Accommodation coefficients (ACs) play an important role in description of rarefied gas flows^{1–3}. They represent particular integrals of the gas-surface interactions allowing us to avoid a detailed descriptions of these complex interactions and, at the same time, to predict more precisely the behavior of gases in vacuum systems, microfluidics, around space vehicles and in other situations when rarefied gas flows encounter solid surfaces. Usually, ACs are not measured directly; instead, they are extracted from experiments using specific models for the gas-solid interaction, such as the simple diffuse-specular scattering or the Cercignani-Lampis (CL) model⁴. The latter will be used here. If ACs determined in one experiment are used to describe another experiment, both experiments must have similar solid surfaces, both must use the same gas, and both must be interpreted using the same model for the gas-solid interaction.

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Today, there is extensive literature providing values of the tangential momentum accommodation coefficient (TMAC) extracted from diverse experiments^{5–7}. However, reliable values of the normal energy accommodation coefficient (NEAC) are rare because of the difficulty of measuring the quantities used to extract NEAC. In the present work, we extract the NEAC from the literature of measurements of the acoustic resonance frequencies of gas-filled, quasi-spherical, metal-walled cavities. These well-documented measurements were performed to determine the Boltzmann constant and the thermodynamic temperature with small uncertainties using different kinds of acoustic resonators^{8–24}. To attain low uncertainties, the temperature jump at the gas-surface interface is taken into account by using the model for radially-symmetric, acoustic standing waves in the cavity. Moreover, the NEAC is extracted from experimental data on heat transfer^{25,26}. In general, the temperature jump and heat transfer are determined by both the TMAC and NEAC so that the diffuse-specular model containing only one parameter is not appropriate for our purpose; instead, the CL model⁴ providing more complete description of the gas-solid interaction will be used here.

The paper is organized as follows: Accommodation coefficients are defined in Section II. The temperature jump coefficient and its application to acoustic resonance are described in Section III. Values of ACs extracted from various experiments are given in Section IV. Discussions and recommendations of new experiments to measure the ACs are presented in Section V.

II. DEFINITION OF ACCOMMODATION COEFFICIENTS

The AC of some property ψ is defined as^{1–3}

$$\alpha(\psi) = \frac{J(\psi)}{J_{\text{diff}}(\psi)}, \quad J(\psi) = \int v_n \psi(v) f(v) dv, \quad (1)$$

where $\mathbf{v}$ is the molecular velocity, v_n is its component normal to a surface element where the AC is calculated, f is the velocity distribution function, J is the actual flux of the property ψ normal to the surface, and J_{diff} is the same flux assuming the complete accommodation (diffuse scattering) of gaseous particles on the surface. For example, if we assume $\psi = mv_t$, where m is the particle mass and v_t is its tangential velocity, then α will be the TMAC denoted as α_t . In another example, if $\psi = mv^2/2$ then α is the AC of the total kinetic energy. It is common to consider only the part of the kinetic energy corresponding to the normal molecular velocity, i.e., $\psi = mv_n^2/2$. The coefficient corresponding to this property is the NEAC further denoted as α_n . The use of the ACs simplifies interpretations of experimental data, but some issues pointed out below should be considered in such interpretations.

The diffuse-specular scattering model assumes that a fraction h of incident particles is scattered diffusely, while the remaining fraction $(1-h)$ is reflected specularly. If we employ this model to calculate the accommodation coefficient α based on Eq. (1), it will be equal to the fraction h for any property ψ and for any incident distribution function. However, the

values of α_t extracted from various experiments on gas flows⁵⁻⁷ are quite different from the values of α_n extracted from experiments on heat transfer^{25,27}. Moreover, the diffuse-specular model is inconsistent with experimental data on the thermomolecular pressure difference^{28,29}.

In contrast to this model, the CL gas-surface interaction kernel⁴ contains two independent parameters α_t and α_n . This model is consistent with measurements of the thermomolecular pressure differences. The CL kernel was constructed so that the TMAC α_t and NEAC α_n calculated by Eq. (1) on the basis of the CL model do not vary for different distribution functions of incident particles so that it is expected that their values will be not sensitive to the type of gas flow. Thus, the CL model is a more versatile description of the gas-surface interaction than the widely used diffuse-specular law.

In the free-molecular regime, some quantities can be expressed analytically in terms of the ACs by applying the CL model. For instance, in case of heat transfer through a gas confined between two parallel plates having a small temperature difference T , the heat flux reads³⁰

$$q = \frac{pv_m \Delta T}{2\sqrt{\pi}T} \left[\frac{\alpha_n}{2-\alpha_n} + \frac{\alpha_t(2-\alpha_t)}{2-\alpha_t(2-\alpha_t)} \right], \quad (2)$$

where p is the gas pressure, T is the average temperature of the plates, v_m is the most probable speed of gaseous particles given by

$$v_m = \sqrt{2k_B T/m}, \quad (3)$$

and k_B is the Boltzmann constant.

III. TEMPERATURE JUMP AND ACOUSTIC RESONANCE

As is well known, in a non-equilibrium state, the gas temperature T_g near a surface is not equal to the surface temperature T_s ; instead, there is a temperature jump which is proportional to the normal temperature gradient in the gas. Let x be a coordinate normal to a flat surface with the origin at the surface and directed toward the gas. Then the temperature jump can be written as^{2,3}

$$T_g - T_s = \zeta_T \ell \frac{dT_g}{dx} \quad \text{at} \quad x=0, \quad (4)$$

where ζ_T is the temperature jump coefficient, ℓ is the equivalent free path defined as

$$\ell = \frac{\mu v_m}{p}, \quad (5)$$

p is the local pressure of the gas, μ is the gas viscosity and v_m is calculated by Eq. (3) using the surface temperature T_s . Considering the Fourier law, Eq. (4) can be also written in term of the normal heat flux q_x

$$T_g - T_s = -\zeta_T \ell \frac{q_x}{\kappa}, \quad q_x = -\kappa \frac{dT_g}{dx}, \quad (6)$$

where κ is the heat conductivity of the gas. Note that the jump condition (4) or (6) is applied to any surface with a curvature radius R_c significantly larger than the equivalent free path, $R_c \gg \ell$. Under this condition, the curvature is negligible and the surface can be considered flat.

During last decades, the temperature jump coefficient was calculated by many researchers starting with the kinetic Boltzmann equation^{5,31–34}. An extensive list of the corresponding publications and critical analysis of numerical data on the jump coefficient can be found in the review⁷. Application of the temperature jump condition, Eqs. (4) or (6), allows us to obtain analytical solutions of some classical problems of heat transfer. For instance, the radial heat transfer q_r between two coaxial cylinder having a small temperature difference T is given by⁷

$$q_r = \kappa \frac{\Delta T}{r} \left[\ln \frac{b}{a} + \frac{\zeta_T}{\delta} \left(1 + \frac{a}{b} \right) \right]^{-1}, \quad (7)$$

where κ is the gas heat conductivity, a and b are inner and outer cylinder radii, respectively, and δ is the gas rarefaction parameter

$$\delta = pa / (\mu v_m). \quad (8)$$

Note that, the expression (7) is valid for large values of the rarefaction parameter $\delta \gg 1$.

Another form of the temperature jump is used in the papers^{9,10,15–17,21,22}, namely,

$$T_g - T_s = -l_a \frac{q_x}{\kappa}, \quad (9)$$

where l_a is the thermal accommodation length defined as

$$l_a = \frac{\kappa}{p} \left(\frac{\pi m T_s}{2k_B} \right)^{1/2} \frac{1}{c_V/k_B + 1/2} \frac{2-h}{h}, \quad (10)$$

and c_V is the specific heat per particle at constant volume. The definition given by Eqs. (9) and (10) is based on the Maxwell theory of the velocity slip and temperature jump phenomena³⁵. The main assumption of this theory is that the stream of molecules approaching to a solid surface is the same as it is in the midst of the gas. In other words, the velocity distribution function in the Knudsen layer is not obtained; instead, its approximate expression is used to calculate macroscopic quantities. Moreover, the diffuse-specular gas-interaction model was applied to obtain Eq. (10) assuming h to be the fraction of diffusely scattered particles. In spite this quantity is frequently referred as thermal AC, the scattering model applied to derive (10) does not relate h to some specific molecular property ψ .

Ewing *et al.*⁹ calculated the effects of the temperature jump on the frequencies of the radially-symmetric acoustic modes of gas-filled spherical cavities surrounded by metal walls. For these modes, the acoustic velocity is perpendicular to the solid walls. As the gas acoustic pressure oscillates, the gas temperature oscillates too. During each acoustic cycle, heat is exchanged between the gas and the solid within thermal boundary layers at the gas-solid interface. Ewing *et al.*⁹ concluded that a temperature jump at the gas-solid boundary increases the resonance frequencies and leaves the half-widths of the resonances unchanged. For a low-density, monatomic gas, the frequency f_i of the i^{th} radially symmetric acoustic mode increases by Δf_i according to

$$\frac{\Delta f_i}{f_i} = \frac{(\gamma-1)l_a}{a} \equiv \frac{A_{-1}p^{-1}}{2u_0^2}, \quad (11)$$

where a is the radius of the spherical cavity, $\gamma = c_p/c_V = 5/3$ is the heat-capacity ratio, p is the pressure, u_0 is the speed of sound in the limit $p \rightarrow 0$, and A_{-1} is a parameter that is fitted to $f_i(p)$. Several groups (Table I) measured the pressure dependence of the acoustic resonance frequencies $f_i(p)$ and corrected the data for well-understood perturbations^{9,10,20}. Then, they determined A_{-1} and l_a in Eq. (11).

A combination of Eqs. (6), (9), and (10) leads to the following relation of the temperature jump coefficient to h

$$\zeta_T = \frac{5\sqrt{\pi}}{4Pr} \frac{1}{c_V/k_B + 1/2} \frac{2-h}{h}, \quad (12)$$

where Pr is the Prandtl number determined by viscosity μ and heat conductivity κ . Using the numerical values of μ and κ based on ab initio potential^{36,37}, we verify that for low-density gases near ambient temperatures, Pr is 0.25% and 0.06% less than 2/3 for helium and argon,

respectively. For these monatomic gases $c_V \approx (3/2)k_B$ and $Pr \approx 2/3$; therefore, Eq. (12) becomes

$$\zeta_T = 1.662 \frac{2-h}{h}. \quad (13)$$

From this expression, we conclude that the minimum value of the temperature jump coefficient calculated from the elementary kinetic theory³⁵ is 1.662 when $h = 1$. However, the jump coefficient ζ_T calculated from the kinetic Boltzmann equation assuming $h = 1$ is significantly larger and equal to

$$\zeta_T = 1.954, \quad (14)$$

according to the review⁷. Thus, the approach to obtain Eq. (12) based on the elementary kinetic theory leads to a significantly smaller value of the temperature jump coefficient in comparison to that obtained from the Boltzmann equation, Eq. (14), even when the same boundary conditions are applied.

In Table I, we list the most precise values of h determined by acoustic resonator experiments and analyzed by their authors using the expressions (9) and (10). As mentioned above, the relationship between the temperature jump and the ACs depends on the model of the gas surface interaction. To avoid this dependence, we recommend reporting experimental results in terms of the temperature jump coefficient ζ_T using Eq. (4). The fifth column of Table I contains the values of the jump coefficient ζ_T that we extracted from the experimental data^{9,10,15–17,21,22} using the relation (13).

The second column in Table I identifies the metals surrounding the gas-filled cavities. Within the resolution of the measurements, the values of ζ_T are independent of which metal comprises the walls of the cavities; however, ζ_T for helium and argon differ significantly from each other. We have no certain explanation for this remarkable independence of the wall metal. We note that the resonators were not baked out under high vacuum conditions; instead, they were exposed for many days to flows of highly purified gases. We speculate that the metal surfaces were covered with oil or water layers, perhaps only a few molecules thick, that hid the differences between the metal substrates. The oil comprising such a layer may originate in vacuum pumps.

Besides the rigorous kinetic equation describing the intermolecular collisions, a reliable model of the gas-surface interaction should be applied. The widely used diffuse-specular model contains only one parameter and does not allow description of a wide range of experiments. That is why the CL model is more suitable for our purpose and will be used below. Numerical values of the jump coefficient ζ_T for various values of α_t and α_n were reported in Refs.^{5,34}. In contrast to the common opinion that the temperature jump coefficient is determined only by the NEAC and independent of the TMAC, it was shown

that the jump coefficient is sensitive to both ACs α_t and α_n ^{5,34}. Thus, if both α_t and α_n are known then the jump coefficient can be calculated applying the methodology described in Refs. 5 and 34.

IV. EXPERIMENTAL VALUES OF ACCOMMODATION COEFFICIENTS

A. Resonators

In this section, we combine the resonator values of the temperature jump coefficient ζ_T with flow-derived values of α_t to estimate TMAC and NEAC for machined metal surfaces. To do this, we assume that metal surfaces of the resonators and of the flow apparatus are equivalent.

To determine the constraints on TMAC and NEAC from the experimental values of ζ_T listed in Table I we need a relation of ζ_T to α_t and α_n obtained from numerical solution of the Boltzmann kinetic equation subject to the CL boundary condition. A method to solve such a problem based on Shakhov's model^{3,39} is described in details previously⁵ and omitted here. Following the method, we calculated the jump coefficient ζ_T with a numerical error below 0.1 % for several values of the ACs α_t and α_n in the ranges $0 \leq \alpha_n \leq 1$ and $0.6 \leq \alpha_t \leq 1$ with the step 0.1. These ranges span all possible in practice values of α_t and α_n for any gas. A convenient representation of the numerical results for $\zeta_T(\alpha_n, \alpha_t)$ within the tolerance of 0.1 % is given by the following interpolating formula

$$\zeta_T = \frac{95.68 - 35.23\alpha_n + 3.55\alpha_n^2 - 25.27\alpha_t + 12.82\alpha_t^2}{1 + 13.4\alpha_n + 23.96\alpha_t - 11.97\alpha_t^2}, \quad (15)$$

which was obtained using the commercial software package TableCurve 3D, Version 4.0.⁴⁰ In the diffuse scattering limit, $\alpha_t = 1$ and $\alpha_n = 1$, Eq. (15) provides the value given by Eq. (14).

According to this relation, not only one pair of ACs provides some specific value of the jump coefficient ζ_T , but a continuous set of values of α_t and α_n leads to the same jump coefficient. Figure 1 displays shaded regions that are consistent with the temperature jump data from resonators listed in Table I. For the helium, the shaded region nominated "He resonance" spans the range $6.35 \leq \zeta_T \leq 7.0$; for argon, the shaded region "Ar resonance" spans the range $2.05 \leq \zeta_T \leq 2.7$. Using additional information about the TMAC, we can reduce the regions of ACs corresponding the experimental values of the jump coefficient given in Table I.

The TMAC has been measured previously by many other methods different from the acoustic resonance. Its values extracted from experimental data on the velocity slip coefficient are given in Table 6 of Ref. 7. Some values extracted from measurements of mass flow rate of gases through long pipes are reported in Ref. 6. Summarizing these data, it can be said that for smooth solid surfaces the TMAC α_t varies in the ranges $0.84 \leq \alpha_t \leq 0.91$ for helium and $0.80 \leq \alpha_t \leq 0.97$ for argon. If a surface is atomically clean, the TMAC for helium

can be as small as 0.71⁴¹. Figure 1 displays the values of TMAC from the papers^{6,7} as horizontal bands nominated as “Ar flow” and “He flow”. If the surfaces of the resonators are comparable to the surfaces of the flow channels, the intersection of the domains “He flow” and “He resonance” in Figure 1 puts tight constraints on the values of α_t and α_n at ambient temperature for helium. The intersection of “Ar flow” and “Ar resonance” in Figure 1 indicates the set of possible ACs for argon. Some pairs of α_t and α_n from these sets related to the experimental values of the jump coefficient ζ_T by Eq. (15) are given in the sixth and seventh columns of Table I.

B. Heat transfer between coaxial cylinders

Previously, the NEAC was estimated²⁷ using experimental data on heat transfer between two coaxial cylinders²⁵. The estimation points out that the NEAC α_n is not larger than 0.1 for helium and it is close to unity for argon. Here, a more detailed analysis of these experimental data is done, i.e. the heat flux is calculated for more pairs of the ACs and hence more accurate values of the NEAC are extracted. For this purpose, the dimensionless heat flux defined as

$$\tilde{q} = \frac{q}{pv_m} \frac{T}{\Delta T} \quad (16)$$

will be used. Here, q is actual heat flux, p is the gas pressure, T is its average temperature and ΔT is the temperature difference between the cylinders.

The experimental data for helium²⁵ are given in the range of the rarefaction parameter δ from 0.009 to 0.18, which practically represents the free-molecular regime. To extract the ACs from these data, the dimensionless heat flux $\tilde{q}$ was calculated by the method described in Ref. 27 for four combinations of the ACs (α_b, α_n): (0.9, 0.0), (0.9, 0.1), (0.7, 0.0), and (0.7, 0.1). A comparison of the experimental data²⁵ with the numerical values of $\tilde{q}$ presented in Figure 2 shows a good agreement between the theory and experiment for the combinations (0.9, 0.0) and (0.7, 0.1). Thus, we conclude that the NEAC α_n is certainly smaller than 0.1, which is consistent with its values extracted from the acoustic resonator data given in Table I. If we assume that the ACs for helium varies in the ranges $0.7 < \alpha_t < 0.9$ and $0 < \alpha_n < 0.1$, the jump coefficient ζ_T will vary from 5.6 to 7.1 according to Eq. (15).

The experimental values of the heat flux through argon²⁵ span the rarefaction parameter δ range from 0.06 to 4. The data for larger values of δ have smaller uncertainty since the heat flux is larger in this regime. A comparison of these data with Eq. (7) allows us to extract the temperature jump coefficient. Combining Eqs.(7) and (16), the dimensionless heat flux in the temperature jump regime is obtained as

$$\tilde{q} = \frac{15}{8\delta} \left[\ln \frac{b}{a} + \frac{\zeta_T}{\delta} \left(1 + \frac{a}{b} \right) \right]^{-1} \quad \text{at } r=a, \quad (17)$$

where the value $Pr = 2/3$ has been used. The curves corresponding to three values of the jump coefficient $\zeta_T = 1.954, 3$ and 5 are plotted in Figure 3 along with the experimental values of the heat flux²⁵. Note that, the first value corresponds to the diffuse scattering, Eq. (14), and it is the lowest among all the other values. The comparison shows that the best agreement between the theory and experiment is reached at $\zeta_T = 3$. The most realistic combination of ACs corresponding to this value of the jump coefficient is $\alpha_t = 0.92$ and $\alpha_n = 0.61$. The value 0.92 of α_t was extracted from the Poiseuille flow, see Table 6 of Ref. 7. The value 0.61 of α_n obtained using Eq. (15) is 20% smaller than the average value $\alpha_n = 0.78$ extracted from the acoustic resonator experiments and given in Table I. Considering that the jump coefficient extracted from any kind of experiment has a relatively large uncertainty, the discrepancy of 20% for two completely different experiments can be considered reasonable. The conclusion about the variation in the range of the temperature jump coefficient of argon can be made from the data given in Table I and the value extracted from the experiments²⁵, that is, $2.3 \leq \zeta_T \leq 3.0$. This range of ζ_T corresponds to the ACs variation in the ranges $0.8 \leq \alpha_t \leq 0.9$ and $0.61 \leq \alpha_n \leq 0.85$.

Thus, the values of the NEAC α_n for both helium and argon extracted from the experimental results on cylindrical heat transfer²⁵ are consistent with those based on the acoustic resonance experiments and given in Table I.

C. Heat transfer between two planar plates

Experimental results on heat transfer between two parallel planar plates made from various kinds of materials were reported in Ref. 26, where the diffuse-specular model was used to extract the AC. The measurements were carried out in a wide range of the gas rarefaction parameter. Since the influence of the gas-surface interaction on the heat flux is maximum in the free-molecular limit ($\delta \rightarrow 0$), it is reasonable to use the data in this limit to extract the TMAC and NEAC. Trott *et al.*²⁶ did not report the heat flux values; instead, they presented their results in term of the AC h . In the free-molecular limit, the heat flux between two plates under the diffuse-specular scattering reads

$$\tilde{q} = \frac{1}{\sqrt{\pi}} \frac{h}{2-h} \quad \text{at} \quad \delta \rightarrow 0, \quad (18)$$

where $\tilde{q}$ is defined by Eq. (16). If we replace the diffuse-specular scattering by the CL model, then the same quantity takes the form

$$\tilde{q} = \frac{1}{2\sqrt{\pi}} \left[\frac{\alpha_n}{2-\alpha_n} + \frac{\alpha_t(2-\alpha_t)}{2-\alpha_t(2-\alpha_t)} \right] \quad \text{at} \quad \delta \rightarrow 0, \quad (19)$$

where Eqs.(2) and (16) have been combined.

Table II shows values of h reported in Ref. 26, the corresponding dimensionless heat flux $\tilde{q}$ calculated by Eq. (18) and possible pairs of α_t and α_n providing the same value of the heat

flux when calculated by Eq. (19). Again, these data show that the NEAC for helium is very small, i.e. $\alpha_n = 0.01$, while for argon it is close to unity, i.e. $0.84 < \alpha_n < 0.93$. These results also suggest that a treatment of metal surfaces by plasma reduces both the TMAC and NEAC.

V. DISCUSSION AND CONCLUSIONS

Recently, measurements of the acoustic resonance frequencies f_{acoustic} of the longitudinal modes of argon-filled cylindrical cavities have been used to determine the Boltzmann constant k_B ¹⁸ and they will be used to determine the thermodynamic temperature T , particularly at its high values^{19,23}. For the lowest possible uncertainties, these measurements must consider the effects of both the temperature jump and the velocity slip at the gas-solid interface. Suppose the cylinder's axis is coincident with the z -coordinate axis and one end of the cylinder is located at $z = 0$. For the longitudinal modes, the acoustic velocity has only a z -component $v_z \propto \sin(z)$. Furthermore, v_z is independent of the x - and y -coordinates, except near the solid, stationary wall that bounds the cavity. At the gas-wall boundary, momentum and heat are exchanged between the oscillating gas and the wall during each acoustic cycle. In response to the momentum exchange, a viscous boundary layer extends from the wall into the cylinder. In this layer, v_z grows from zero at the wall (ignoring slip) to v_z with the characteristic length $\delta_v = [\mu(\pi \rho f_{\text{acoustic}})]^{1/2}$, where ρ is the mass density of the gas. According to Moldover *et al.*²⁰, the boundary layer adds a measurable term to f_{acoustic} that varies as $-p^{1/2}$ at low gas pressures because under such conditions $p \propto \rho$.

In principle, measurements of f_{acoustic} of several modes of a cylindrical cavity can be analyzed to determine values of α_t and α_n . In practice, the resulting uncertainties of α_t and α_n will be larger than those in Table I because the acoustic modes of a cylindrical cavity have lower signal-to-noise ratios for measuring f_{acoustic} than the modes of quasi-spherical cavities of equal volume. Even with large uncertainties, resonator-derived values of α_t would be of interest to better understand gas-surface interactions. For the most accurate measurements of thermodynamic temperatures, it may be useful to conduct slip-sensitive flow measurements to determine α_t for argon-solid interfaces similar to those used in high-temperature resonators.

We pointed out that presentations of experimental results for gas-surface interactions in terms of ACs are model-dependent and should be avoided. Therefore, we recommend that future presentations of resonator results use the well-defined temperature jump coefficient. In addition, future results on a heat flux between two surfaces will be more valuable when experimental values of the heat flux itself are presented instead of data on extracted ACs. We note that a derivation of ACs from any kind of experimental data is not a trivial task requiring a numerical calculation of the kinetic equation together with a reliable model of the gas-surface interaction.

We reviewed the temperature jump coefficients determined by experimental data from spherical acoustic resonators. First, this coefficient has been calculated applying the CL model of the gas-surface interaction for the whole range of the NEAC, while only those values of the TMAC that are usually observed in practice have been considered. These data

have been used to extract the NEAC from the experimental values of the temperature jump coefficient for helium and argon. To check the consistency of these data, the same coefficients were extracted from experimental data on heat transfer between two coaxial cylinders and two parallel plates. Analyzing all these data, it was found that the NEAC of helium varies in the range $0 < a_n < 0.1$. The same coefficient for argon varies in the range $0.61 < a_n < 0.93$. The variations of the temperature jump coefficient are $5.6 < \zeta_T < 7.1$ and $2.3 < \zeta_T < 3.0$ for helium and argon, respectively. These values span all most types of smooth metallic surfaces.

Since the temperature jump coefficient is sensitive to both the TMAC and NEAC, their values can be extracted more precisely from different types of experiments made with the same surface and gas. For instance, two rotating discs can be used to measure the shear stress and subsequently to calculate the TMAC. The same discs having different temperatures can be employed to measure the heat flux between them, which can then be used to calculate the NEAC. Similar experiments can be performed with two coaxial cylinders.

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FIG. 1.
(Color online) Shaded areas are values of α_t and α_n consistent with resonance data from Table I and with flow data^{6,7}.

FIG. 2.
(Color online) Experimental data²⁵ (symbols) of heat flux through helium between two coaxial cylinders and its numerical values (curves) based on the theory²⁷.

FIG. 3.
(Color online) Experimental data (symbols) reported in²⁵ of heat flux through argon between two coaxial cylinders and analytical solution (curves) based on Eq. (7)

TABLE I

Experimental values of accommodation coefficient h near 273.16 K, corresponding values of temperature jump coefficient ζ_T calculated by Eq. (13), and combinations of α_l and α_n providing the same value of ζ_T according to Eq. (15).

gas	surface	Ref.	h	ζ_T	α_l	α_n
He	ETP-Cu ^a	22 ^b	0.399±0.15 ^c	6.67±0.32 ^d	0.7	0.037
	ETP-Cu	21	0.3926±0.0010	6.805±0.022	0.7	0.027
	OFHC-Cu ^e	16	0.38±0.01	7.1±0.2	0.7	0.007
	SS ^f	14	0.38±0.05	7.1±1.3	0.7	0.007
Ar	Al ^g	9	0.84±0.05	2.30±0.25	0.9	0.85
	ETP-Cu	15	0.80±0.03	2.55±0.16	0.9	0.76
	ETP-Cu	17	0.777±0.013	2.62±0.07	0.9	0.74

^aElectrolytic-Tough-Pitch Copper

^bPreliminary results using helium in this resonator are consistent with $h=0.40 \pm 0.02$ in the range 235 K to 362 K³⁸.

^cThe uncertainties for h are those provided by the original authors and correspond to one standard uncertainty

^dThe uncertainties for the temperature jump coefficient are propagated from the uncertainty of h

^eOxygen-Free-High-Conductivity Copper

^fStainless Steel

^gAluminum alloy

TABLE II

Experimental values²⁶ of accommodation coefficient h , dimensionless heat flux calculated by Eq. (18) and ACs extracted by Eq. (19).

gas	surface	h	$\bar{q}$	α_i	α_n
He	SS ^a	0.46±0.02 ^b	0.168 ±0.010 ^c	0.49	0.01
	Al ^d	0.47±0.02	0.173 ±0.010	0.51	0.01
	Pl ^e	0.58±0.02	0.230 ±0.011	0.68	0.01
	SS-pl ^f	0.38±0.02	0.132 ±0.009	0.40	0.01
	Al-pl ^g	0.38±0.02	0.132 ±0.009	0.40	0.01
	Pl-pl ^h	0.52±0.02	0.198 ±0.010	0.58	0.01
Ar	SS	0.95±0.02	0.510±0.021	0.95	0.92
	Al	0.96±0.02	0.521±0.021	1.0	0.93
	Pl	0.96±0.02	0.521±0.021	1.0	0.93
	SS-pl	0.90±0.02	0.462±0.019	0.9	0.84
	Al-pl	0.91±0.02	0.471±0.019	0.9	0.85
	Pl-pl	0.94±0.02	0.500±0.020	0.95	0.90

^aMachined Stainless Steel

^bUncertainty declared in Ref.²⁶ and based only on repeatability in measurements.

^cUncertainties propagated from the uncertainty of h

^dMachined Aluminum

^eMachined Platinum

^fMachined Stainless Steel treated by plasma

^gMachined Aluminum treated by plasma

^hMachined Platinum treated by plasma