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Mixture models for undiagnosed prevalent disease and interval-censored incident disease: Applications to a cohort assembled from electronic health records

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Abstract

For cost-effectiveness and efficiency, many large-scale general-purpose cohort studies are being assembled within large health-care providers who use electronic health records. Two key features of such data are that incident disease is interval-censored between irregular visits and there can be pre-existing (prevalent) disease. Because prevalent disease is not always immediately diagnosed, some disease diagnosed at later visits are actually undiagnosed prevalent disease. We consider prevalent disease as a point mass at time zero for clinical applications where there is no interest in time of prevalent disease onset. We demonstrate that the naive Kaplan-Meier cumulative risk estimator underestimates risks at early time points and overestimates later risks. We propose a general family of mixture models for undiagnosed prevalent disease and interval-censored incident disease that we call prevalence-incidence models. Parameters for parametric prevalence-incidence models, such as the logistic regression and Weibull survival (logistic-Weibull) model, are estimated by direct likelihood maximization or by EM algorithm. Non-parametric methods are proposed to calculate cumulative risks for cases without covariates. We compare naive Kaplan-Meier, logistic-Weibull, and non-parametric estimates of cumulative risk in the cervical cancer screening program at Kaiser Permanente Northern California. Kaplan-Meier provided poor estimates while the logistic-Weibull model was a close fit to the non-parametric. Our findings support our use of logistic-Weibull models to develop the risk estimates that underlie current U.S. risk-based cervical cancer screening guidelines.

Keywords

cervical cancer; cumulative risk estimation; HPV; Kaplan-Meier; prevalence-incidence models

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1. Introduction

Screening is used to identify individuals with asymptomatic disease or disease precursors for effective early intervention. A goal of “precision medicine” is to develop screening guidelines that are based on the risk of disease, given an individual’s risk factors and screening test results [1]. To inform screening guidelines, many large-scale general-purpose epidemiologic cohort studies are being organized within large health-care providers who use electronic health records [2]. These providers have the benefit of having large patients populations to recruit from, pre-existing infrastructure to support longitudinal visits, and electronic health records to facilitate data collection. Although potentially cost-effective and efficient, such cohorts present many challenges for analysis [3]. We consider two key features of such data that make it inappropriate to calculate risk using standard methods, such as Kaplan-Meier methods [4] or Cox models [5].

First, the exact time of disease onset for an individual is unobserved and only the partial information of the occurrence falling between the last time observed to be disease-free and the time of diagnosis, ie. mixed cases interval censoring [6], is available. For approximately regular intervals, which can be enforced in controlled trials, discrete time or Kaplan-Meier methods could be applied as approximations. However, researchers working with data from health providers typically cannot influence the timing of visits, and patients return at intervals that are quite irregular, which render discrete-time or Kaplan-Meier methods inappropriate to use [7].

Second, people can enter the screening program with prevalent disease at baseline that is not always immediately diagnosed. In particular, people with missing or negative screening test results generally do not undergo definitive disease ascertainment, such as biopsies. Consequently, among those for whom prevalent disease was not ascertained but disease is diagnosed at future screens, it is not possible to determine whether the disease is undiagnosed prevalent disease that occurred prior to enrollment into the screening program or incident disease that occurred over the course of screening. Accurately estimating risk of prevalent disease is important because clinicians are primarily concerned with the risk that disease is present. Guidelines for referring women for immediate biopsies should be based on the prevalent disease risk [8].

In our application, it suffices to consider prevalent disease as a left-censored point mass at time zero, because a clinician takes little interest on the time in the past when a cancer detected today might have arisen. Standard approaches to mixed cases interval censoring [9, 10, 11] do not handle a point mass at time zero for prevalent disease. One could either set aside those with ascertained prevalent disease or approximate ascertained prevalent disease by offsetting to a small time just after zero, and then apply traditional interval-censoring approaches. However, both of these methods would treat unascertained prevalent disease that are diagnosed at future screens as incident disease and would result in underestimating prevalent disease risks while inflating incident disease risks. For covariates, a Cox model cannot properly separate covariate effects on prevalent disease from those for incident disease. Furthermore, applying Kaplan-Meier and Cox model methods by ignoring the interval censoring and using time of diagnosis to approximate time of disease onset results in

biased estimates [12, 13]. In section 2, we demonstrate that there is an interesting pattern to this bias: the Kaplan-Meier cumulative risk estimator generally underestimates early risks and overestimates later risks.

In this article, we propose a general family of mixture models, which we call prevalence-incidence survival models, for estimating the cumulative risk and assessing covariate effects using data from screening cohorts assembled from electronic health records (Section 3). Prevalence-incidence models are akin to cure mixture models [14, 15, 16], but the point mass is at zero rather than infinity. Prevalent disease is observed for some individuals, mitigating identifiability issues that can affect cure mixture models [17]. Identifiability of prevalence-incidence models is considered in the Web Appendix A. Moreover, in prevalence-incidence survival models, accurately identifying those at high risk of prevalent disease and in need of immediate intervention is of primary importance, whereas, in cure models, it is not often crucial for clinicians to differentiate long-term survivors from those who are cured.

We employed the expectation-maximization (EM) algorithm [18] for inference in parametric prevalence-incidence survival models. All details are presented for the useful special case where prevalent disease is modelled with logistic regression and incident disease is modelled with a Weibull survival model, which is supported by the multi-stage theory of carcinogenesis [19]. We also present a non-parametric cumulative risk estimator for the marginal model that has no covariates; this can be used to check the distribution assumptions of the parametric prevalence-incidence survival models. Our R package, PIMixture (<http://dceg.cancer.gov/tools/analysis/PIMixture>), provides the non-parametric estimator, the logistic-Weibull model, and various other parametric prevalence-incidence models. We use simulations to examine the robustness of our cumulative risk estimators when the logistic-Weibull model is misspecified (Section 4).

In section 5, we use the Kaiser Permanente Northern California (KPNC) cervical cancer screening cohort to estimate the cumulative risk of cervical precancer and cancer following HPV-positive/Pap-negative baseline screening results. The KPNC cohort consists of 1.4 million women screened from 2003-2013 and was assembled by linking various electronic records of patient information, test results, and disease outcomes [20]. Not all women with HPV-positive/Pap-negative results underwent definitive disease ascertainment at baseline, so while only 0.18% of these women had precancer/cancer diagnosed at baseline, precancer/cancer could have been present at baseline for another 2.05% of these women. Compared to the non-parametric estimates, the Kaplan-Meier estimates show the expected under/over estimation. Estimates from the logistic-Weibull model agree with the non-parametric estimates and demonstrates that the logistic-Weibull model can estimate prevalent disease risk even when disease is rarely ascertained at baseline. We illustrate how we used the risk estimates from the logistic-Weibull model to inform the current U.S. cervical cancer screening guidelines [21, 22]. In section 6, some useful extensions of prevalence-incidence models are discussed.

2. The behavior of the Kaplan-Meier estimator in screening data

While originally proposed for analysis of mortality data, Kaplan-Meier methods are often used to estimate disease-free survival by using the time of diagnosis to approximate time of disease onset [13]. This approximation is reasonable for symptomatic disease, as the diagnosis time is close to the time of disease onset. However, for asymptomatic disease, the difference between time of diagnosis and time of onset depends on the density of screening visits and the sensitivity of screening tests. In cervical screening, women who test negative usually have long-term (3-year) intervals [21]. Consequently, diagnosis of cervical precancer/cancer may lag onset by years, and Kaplan-Meier estimates based on diagnosis time may be biased for the cumulative risk of disease onset.

Consider this simple example. For n subjects disease-free at baseline, denote the cumulative distribution of time of disease onset as F . Suppose these subjects randomly return for a single follow-up visit with definitive disease ascertainment at one of two time points: θn subjects are seen at t_1 and the remaining $(1 - \theta)n$ subjects are seen at time t_2 , where $\theta \in (0, 1)$ and $0 < t_1 < t_2$. From Table 1, we see that Kaplan-Meier methods using time of diagnosis will underestimate the cumulative risk at t_1 by the fraction of people, θ , who return at the early time point. Intuitively, disease with early onset is not detected until later, and thus, Kaplan-Meier methods underestimates early disease risk. This underestimation can be substantial; if for example, people are asked to return at t_1 and 70% do return, then the cumulative risk at t_1 is underestimated by 30%. A numerical example is presented in Web Appendix B.

Interestingly, at the later time point, t_2 , Kaplan-Meier methods treating diagnosis time as occurrence time overestimates the cumulative risk when $\theta F(t_1) > 0$. From table 1, it is easily seen that the amount of overestimation is given as $\theta F(t_1)\{1 + F(t_2)\}$. Intuitively, we not only have the extra disease from those whose disease onset was earlier, but also the risk set contains fewer people than at the earlier time, leading to overestimation. The amount of overestimation at t_2 increases as:

1. θ increases to one. When θ is close to zero, bias is small at time t_2 as almost all subjects return for the first time at time t_2 . As θ increases to one, the bias in the cumulative risk at t_1 shrinks while the bias at t_2 increases.
2. $F(t_1)$ increases to one. When $F(t_1)$ is zero, no events have occurred among the n subjects by t_1 . Thus for the $(1 - \theta)n$ who return at time t_2 , time t_1 can be seen as renewal of the survival process with all subjects returning at time t_2 .

Note that t_1 can be arbitrarily close to t_2 , but the Kaplan-Meier estimate at t_1 and t_2 can differ considerably with biases in opposite directions. This is because the Kaplan-Meier estimator sees $(1 - \theta)nF(t_2)$ events occurring in the very short time period between t_1 and t_2 , with a smaller population at risk, $(1 - \theta)n$ instead of n , and thus estimates very large hazards for t_2 .

The bias in the Kaplan-Meier estimator does not depend on n but only on the proportions returning at each of the two time points, so increasing the sample size to infinity does not remove the bias. This pattern of the Kaplan-Meier cumulative risk estimator underestimating

at earlier times and overestimating at later times persists for screening data with more than two return time points.

3. Prevalence-Incidence Survival Models

We propose a general family of mixture models, which we call prevalence-incidence survival models. For subjects $i = 1, 2, \dots, n$, let T_i be the time of disease onset, which is never directly observed. Let $c_i = I(T_i = 0)$, which is the subject-specific indicator variable for (prevalent) disease present at the baseline visit (time zero). Let L_i be the last time the i th subject is observed to be disease-free, which is defined only when c_i is known to be zero. Let R_i be the first time that the i th subject is diagnosed with the disease. For many subjects, c_i is unobserved, and we know only that $T_i \leq R_i$. We allow $R_i = \infty$ to include cases of right-censoring or when subjects with unobserved c_i provide no information regarding T_i . Let x_i and z_i be subject-specific vectors of covariates for prevalent and incident disease respectively.

Let θ_1 and θ_2 be disjoint vectors of parameters. Given covariates x and z , let $P(T = 0; x, z) = P(c = 1; x) = \pi(x; \theta_1)$ be the probability of prevalent baseline disease (prevalence model) and $P(T > t | c = 0, x, z) = P(T > t | c = 0, z) = S(t; \theta_2 | c = 0, z)$ be the conditional survival function of time to disease onset given that the disease is not present at baseline (incidence model). The cumulative risk can be modelled as

$$P(T \leq t; x, z, \theta) = \pi(x; \theta_1) + \{1 - \pi(x; \theta_1)\} \{1 - S(t; \theta_2 | c = 0, z)\}, \quad t \geq 0, \quad (1)$$

where $\theta = \theta_1 \cup \theta_2$. Thus the cumulative risk, $P(T \leq t; x, z, \theta)$, can be seen as a mixture distribution having mixing proportions $\pi(x; \theta_1)$ and $1 - \pi(x; \theta_1)$ with component distributions $P(T \leq t | c = 1) = 1$, a degenerate distribution among those with prevalent disease at baseline, and $P(T \leq t; \theta_2 | c = 0, z) = 1 - S(t; \theta_2 | c = 0, z)$, the conditional failure time distribution among those without prevalent disease at baseline.

3.1. Non-parametric estimator of the cumulative risk

In this subsection, we show how to obtain the non-parametric maximum likelihood estimate (NPMLE) of the cumulative risk. In addition to its intrinsic value, the NPMLE can be used to assess the distribution assumptions of parametric prevalence-incidence models with no covariates.

The NPMLE of the cumulative risk can be obtained by applying the EM-ICM algorithm [23] after mapping (c_i, L_i, R_i) to new intervals (L'_i, R'_i) in three steps as followed:

1. if $c_i = 1$, set (L'_i, R'_i) to the interval $(0, \varepsilon]$;
2. if $c_i = 0$, set (L'_i, R'_i) to intervals $(\max(\varepsilon, L_i), R_i]$;
3. if c_i is unknown, set (L'_i, R'_i) to intervals $(0, R_i]$,

where ε is half of the value of the smallest positive L_i in the data set.

Because the NPMLE assumes that the survival function is one at time zero, we approximate prevalent disease by assuming known prevalent disease occurs in the small time interval $(0, \varepsilon]$ immediately after time zero (step 1). The estimated risk of disease prevalent at time zero is then the NPMLE cumulative risk estimate at ε . Known incident disease is mapped to time intervals after ε (step 2). We set ε to half of the value of the smallest positive L_i in the data set; however, ε can take any value between zero and the smallest positive L_i . The intuition is to use ε to assign separate time intervals to known prevalent disease and known incident disease, as bias will ensue if the intervals overlap. The third step assigns time intervals that span the prevalent and incident disease intervals when it is unknown whether the disease is prevalent or incident.

We cannot directly extend methods for the NPMLE to include covariates because such an approach assumes that the size and relationship (eg. proportional hazards or additive risks) of the covariate effects for incident disease also applies to prevalent disease. Instead we suggest using prevalence-incidence survival models when incorporating covariates.

3.2. Likelihood for prevalence-incidence survival models

Let K_1 and K_0 be partitions of subjects into observed and missing c_i , respectively. We assume that c_i is missing at random (MAR).

When $c_i = 1$, the subject contributes $\log \{ \pi(x_i; \theta_1) \}$ to the log-likelihood. When $c_i = 0$, the subject contributes $\log \{ 1 - \pi(x_i; \theta_1) \} + \log \{ S(L_i; \theta_2 | c_i = 0, z_i) - S(R_i; \theta_2 | c_i = 0, z_i) \}$ to the log-likelihood. Finally, when c_i is unobserved, the subject contributes $\log [\pi(x_i; \theta_1) + \{ 1 - \pi(x_i; \theta_1) \} \{ 1 - S(R_i; \theta_2 | c_i = 0, z_i) \}]$. Let y^{obs} and y^{mis} denotes the observed and missing data, respectively, contained in $y_i = \{ x_i, z_i, L_i, R_i, c_i \}$, for $i = 1, 2, \dots, n$. Then the observed log-likelihood is given as:

$$\begin{aligned}
 l(y^{obs}; \theta) = & \sum_{i \in K_1} [c_i \log \{ \pi(x_i; \theta_1) \} + (1 - c_i) \{ \log(1 - \pi(x_i; \theta_1)) + \log(S(L_i; \theta_2 | c_i = 0, z_i) - S(R_i; \theta_2 | c_i = 0, z_i)) \}] \\
 & + \sum_{i \in K_0} \log [\pi(x_i; \theta_1) + \{ 1 - \pi(x_i; \theta_1) \} \{ 1 - S(R_i; \theta_2 | c_i = 0, z_i) \}].
 \end{aligned}
 \tag{2}$$

A full derivation of the observed log-likelihood from the complete data joint likelihood is given in Web Appendix C.

3.3. Inference for parametric prevalence-incidence survival models

When parametric forms are chosen for both $\pi(x; \theta_1)$ and $S(t; \theta_2 | c = 0, z)$ in (1), the likelihood (2) can be directly maximized by Newton-Raphson method [24]. However, Newton-Raphson method does not converge for KPNC data analyses that have a large proportion of subjects (greater than 99%) with right-censored event times, which is a situation that is not uncommon for population-based cancer screening. For those analyses, we employ the EM algorithm [18] as followed:

Initialization—Set initial values for the parameters $\theta^{(0)}$. Two useful sets of initial values are the parameter values that maximize (2) after assuming that disease diagnosed in K_0 are either all prevalent disease, ($c_i = 1$) or all incident disease ($c_i = 0$). When the EM algorithm based on these two extreme starting values converge to the same set of parameter values, that provides additional confidence that the EM algorithm is converging to a global maximum.

Alternate between the expectation (E) step and the maximization (M) step until convergence:

E-step—Use $\theta^{(l)}$ to compute the expected log-likelihood given by

$$Q(\theta|\theta^{(l)}) = \sum_{i=1}^n [E(c_i|y_i^{\text{obs}}; \theta^{(l)}) \log\{\pi(x_i; \theta_1)\} + \{1 - E(c_i|y_i^{\text{obs}}; \theta^{(l)})\} \{\log(1 - \pi(x_i; \theta_1)) + \log(S(L_i; \theta_2|c_i=0, z_i) - S(R_i; \theta_2|c_i=0, z_i))\}], \quad (3)$$

where $S(L_i; \theta_2|c_i=0, z_i) = 1$ when $i \in K_0$ and

$$E(c_i|y_i^{\text{obs}}; \theta^{(l)}) = \begin{cases} c_i & : i \in K_1 \\ \frac{\pi(x_i; \theta_1^{(l)})}{\pi(x_i; \theta_1^{(l)}) + \{1 - \pi(x_i; \theta_1^{(l)})\} \{1 - S(R_i; \theta_2^{(l)}|c_i=0, z_i)\}} & : i \in K_0. \end{cases} \quad (4)$$

For subjects in K_0 , as R_i approaches zero, $E(c_i|y_i^{\text{obs}}; \theta^{(l)})$ approaches one, reflecting the fact that the detected disease is more likely to have been prevalent at baseline. When $R_i = \infty$, then there is no information regarding the subject's time of disease onset and the conditional expectation of c_i equals the average probability of prevalence.

M-step—The updated MLE, $\theta^{(l+1)}$, are the values of θ that maximizes the expected log-likelihood (3), which can be separated into terms containing only $\pi(x_i; \theta_1)$ and only $S(t; \theta_2|c_i=0, z_i)$ as followed:

$$\begin{aligned} Q(\theta|\theta^{(l)}) &= \sum_{i=1}^n [E(c_i|y_i^{\text{obs}}; \theta^{(l)}) \log\{\pi(x_i; \theta_1)\} + \{1 - E(c_i|y_i^{\text{obs}}; \theta^{(l)})\} \{\log(1 - \pi(x_i; \theta_1))\}] \\ &\quad + \sum_{i=1}^n \{1 - E(c_i|y_i^{\text{obs}}; \theta^{(l)})\} \{\log(S(L_i; \theta_2|c_i=0, z_i) - S(R_i; \theta_2|c_i=0, z_i))\}. \end{aligned}$$

This allows $\theta_1^{(l+1)}$ and $\theta_2^{(l+1)}$ to be estimated separately.

The variance of $\hat{\theta}$ is the inverse of the observed Fisher information. The variance of the cumulative risk can be derived using the delta method:

$$\widehat{\text{Var}}\{P(T \leq t; x, z, \hat{\theta})\} = \nabla P(T \leq t; x, z, \hat{\theta})^T \cdot \text{Var}(\hat{\theta}) \cdot \nabla P(T \leq t; x, z, \hat{\theta}),$$

where $\nabla P(T \leq t; x, z, \hat{\theta})$ is the gradient of $P(T \leq t; x, z, \hat{\theta})$.

The complementary log-log of the cumulative risk can be shown to be asymptotically normal via the multivariate delta method (Web Appendix D). Confidence limits for the cumulative risk can be constructed on the complementary log-log scale and then converted to the cumulative risk scale.

3.4 logistic-Weibull model

A parametric prevalence-incidence survival model that is relevant to cancer screening is a mixture of logistic regression prevalence model and Weibull regression incidence model. The prevalence and incidence models are parameterized as

$$\pi(x; \theta_1) = \frac{\exp(x_i^T \beta)}{1 + \exp(x_i^T \beta)}$$

and

$$S(t; \theta_2 | c=0, z_i) = \exp \left[- \left\{ \frac{t}{\exp(z_i^T \gamma)} \right\}^{\frac{1}{\tau}} \right]$$

respectively, where $\beta = (\beta_0, \beta_1, \dots, \beta_{m_1-1})$ and $\gamma = (\gamma_0, \gamma_1, \dots, \gamma_{m_2-1})$ are vectors of regression coefficients and $\tau > 0$ governs the shape of the Weibull distribution. Note that $\theta_1 = \beta$ and $\theta_2 = (\gamma, \tau)$. Inference for parameters, cumulative risk, odds ratios, and hazard ratios for the logistic-Weibull models are presented in Web Appendix E. The M-step is solved using just one iteration of Newton's method. This EM gradient algorithm [25] is locally equivalent to the EM algorithm, but converges more quickly.

The Weibull survival model is supported by the multi-stage theory of carcinogenesis [19], which suggests that cancer incidence has a Weibull distribution. The time of follow-up for most cancer studies are relatively short, in the sense that time to cancer incidence is right-censored for most subjects. Given that we expect the hazard of cancer to be monotonic over this short time scale, the Weibull incidence model can be an adequate working model for cancer screening.

In the special case of no undiagnosed baseline disease (i.e. everyone at baseline undergoes definitive disease ascertainment), then the likelihood (2) can be factored into prevalence and incidence model parts, and thus parameters in each model can be estimated separately. For the logistic-Weibull model, this means that the logistic regression and Weibull regression can be conducted separately to obtain their own parameter estimates.

4. Performance of the logistic-Weibull model

We evaluated the performance of the logistic-Weibull prevalence-incidence survival model for cases when the model was correctly specified and for cases when it was misspecified. Within each set-up, 1,000 simulation data sets, each containing 10,000 patients were used. Because most applications will use the same covariates for both the prevalence and incidence models, we set $x_i = z_i = (x_{1i}, x_{2i})$, where x_{1i} and x_{2i} were drawn from independent Bernoulli(0.5) and Uniform(0,1) distributions, respectively. Using different sets of covariates did not change the overall conclusions of the simulations.

For simulations under a correctly specified logistic-Weibull model, prevalent disease followed a logistic regression model and time to onset of incident disease followed a Weibull regression model:

$$\pi(x; \theta_1) = \frac{\exp(-3.5 + .5x_{1i} + x_{2i})}{1 + \exp(-3.5 + .5x_{1i} + x_{2i})}$$

and

$$S(t; \theta_2 | c=0, z) = \exp\left\{-\left(\frac{t}{\exp(3.5 - .5x_{1i} - .5x_{2i})}\right)^2\right\}.$$

For simulations under a misspecified logistic-Weibull model, prevalent disease followed a probit regression model and time to onset of incident disease followed a log-logistic survival model:

$$\pi(x; \theta_1) = \Phi(-2 + .35x_{1i} + .5x_{2i})$$

and

$$S(t; \theta_2 | c=0, z_i) = \frac{1}{1 + t^2 \exp\{-(4.3 + 1.5x_{1i} + 2x_{2i})\}}.$$

For each subject, an indicator variable for whether disease was ascertained at baseline was drawn from an independent Bernoulli distribution. We examined the performance of the prevalence-incidence model while varying the levels of disease ascertainment at baseline: 90% - high ascertainment, 50% - moderate ascertainment, and 10% - low ascertainment. Following baseline, time to each subsequent disease ascertainment followed a Gamma(3,1) distribution, with no disease ascertainment after time 20. The amount of right-censoring in the data varied from 63% to 69% for each of the simulation set-ups. Confidence intervals for the cumulative risks were obtained by constructing confidence limits on the asymptotically normal complementary log-log cumulative risk scale and converting those confidence limits to the cumulative risk scale.

When correctly specified, the logistic-Weibull prevalence-incidence model performed well regardless of the level of disease ascertainment at baseline, with unbiased parameter and cumulative risk estimates and good coverage. Table 2 gives the results of the logistic-Weibull model under low disease ascertainment at baseline.

Table 3 shows the result of fitting a misspecified logistic-Weibull prevalence-incidence survival model to a population where prevalent baseline disease followed a probit regression model and time to onset of incident disease followed a log-logistic survival model. While coverage can be poor, the bias in the cumulative risk was below 9% at all time points. Under high baseline disease ascertainment, there was virtually no bias at early time points as logit and probit link functions often yield very similar outputs. The misspecified survival model resulted in biased cumulative risks at later times, with the greatest amount of overestimation at time 5.6 (6.76%). When there was less data on the baseline disease status, as in the case of low baseline disease ascertainment, the misspecified survival model had a greater effect on bias at early time points, with the baseline disease risk underestimated by 8.3%. At later times, the misspecified survival model resulted in overestimating the cumulative risk, with the greatest amount of overestimation at time 6.9 (5.4%).

We also applied the methods described in section 3.1 to the simulation data to show that the bias for the NPMLE cumulative risk estimator was less than 1%, regardless of the level of disease ascertainment. These results are presented in Table 4.

5. Application to women who test HPV-positive/Pap-negative

The most common abnormal screening result at Kaiser Permanente Northern California (KPNC) is HPV-positive but Papnegative [22]. It is the most challenging abnormality to manage because the Pap test might have missed precancer/cancer, but more likely, the HPV infection might naturally clear without intervention. Accurately estimating the cumulative risk of cervical intraepithelial neoplasia grade 3 and cancer (CIN3+), ie. precancer/cancer, is an important step in developing appropriate management guidelines. We compared the cumulative risk estimates of CIN3+ obtained using different methods. We compared the overall and age-stratified risk curve of HPV-positive/Pap-negative women to the risk curves of other abnormal results for which management strategies are well established. We assumed prevalent disease status was missing at random given the baseline cotest result, because whether women have definitive disease ascertainment at baseline depended primarily on the KPNC protocols for their baseline cotest result.

From 2003–2013, 34,261 women age 30–65, with no prior history of screening abnormalities, precancers, or treatments, tested HPV-positive/Pap-negative at their first “cotesting” (testing with both HPV and Pap) screen. According to KPNC protocols, these women would have been told to forgo immediate colposcopy and undergo a repeat cotesting screen in one year, where if they tested either HPV-positive or Pap-positive, they would be referred to colposcopy for definitive disease ascertainment. However, only 12,058 (35.2%) of women had repeat cotesting one year later; 1,249 (3.6%) opted for immediate colposcopy, while others either returned late for repeat cotesting (the largest return time was over 10 years later) or did not return at all.

Among the population of HPV-positive/Pap-negative women, 1,056 CIN3+ were diagnosed, of which 61 (8.8%) were classified as cancers. Because early cervical cancers and precancers usually have no symptoms, we treated censoring as uninformative. We applied an algorithm to patients' longitudinal history of cotesting and colposcopy results so that the intervals (L_i, R_i) reflect medical opinion of the smallest reasonable interval in which disease onset can occur. For example, we accepted negative cotesting results as a surrogate for ascertaining that a woman did not have precancer/cancer ($<$ CIN3), because HPV-positivity is a necessary precursor to cervical cancer and negative cotesting results have a very low false positive rate [26]. Among the 34,261 women testing HPV-positive/Pap-negative at their first cotesting screen, 61 (0.18%) were diagnosed with CIN3+ at an immediate colposcopy visit. 995 (2.90%) were diagnosed with CIN3+ in follow-up, of which we could rule out prevalent CIN3+ for only 292 (0.85%). 24,282 (70.87%) were right-censored, while 8,923 (26.0%) did not have sufficient history to classify as either CIN3+ or $<$ CIN3 at any time point. The percentage risk of a prevalent CIN3+ in the sample is then between $100 \times 61 / (24,282 + 61 + 995) \% = 0.24\%$ and $100 \times (61 + 995 - 292) / (24,282 + 61 + 995) \% = 3.02\%$.

5.1 Comparison of cumulative risk estimates

For women testing HPV-positive/Pap-negative, we estimated the cumulative risk of CIN3+ using our non-parametric risk estimator, the Kaplan-Meier estimator treating time of diagnosis as occurrence time, and various parametric prevalence incidence models fitted without covariates. For parametric prevalence incidence models, we modelled prevalent disease using an intercept-only logistic regression and considered the Weibull, exponential, loglogistic, lognormal, generalized gamma, and gamma distributions for the incidence model. Confidence intervals were obtained by estimating confidence limits on the asymptotically normal complementary log-log scale and converting those confidence limits to the cumulative risk scale. Figure 1 shows the cumulative risk curve of CIN3+ from the non-parametric risk estimator, the Kaplan-Meier estimator, the logistic-Weibull model, and the logistic-generalized-gamma model, which is the best fitting parametric prevalence-incidence model according to the Bayesian Information Criterion (BIC).

The non-parametric cumulative risk curve was a step function that is constant for long intervals followed by large jumps, reflecting the clustering in the times that women return for further screening. For example, both the non-parametric prevalent and one-year cumulative risk of CIN3+ were 1.99%, but the non-parametric cumulative risk jumped to 2.79% at 14 months. The non-parametric risk curve was flat in the first year because few women returned early for screening, and the jump at 14 months reflects the large clustering of diagnoses from those who returned at one year, tested HPV- positive or Pap-positive at that visit, and were referred to colposcopy visits for definitive disease ascertainment. Because decision frameworks for action are based on risks at specific time points [8], the non-parametric estimator cannot be directly used for determining guidelines. However, the non-parametric cumulative risk can be used to assess fit of other estimators. The non-parametric estimator estimated 1.99% prevalent CIN3+ risk and 5.68% seven-year cumulative risk of CIN3+. In contrast, Kaplan-Meier methods estimated merely 0.18% prevalent CIN3+ risk, reflecting the proportion of HPV-positive/Pap-negative women who were diagnosed with CIN3+ at immediate colposcopy visits. Kaplan-Meier methods

presumed that all CIN3+ diagnosed at future times were truly incident disease and overestimated the hazard of incident CIN3+, leading to a 7.31% seven-year cumulative risk estimate.

The logistic-Weibull model estimate of 1.87% prevalent CIN3+ risk was close to the non-parametric estimate of 1.99%, showing that prevalence-incidence models can estimate prevalent disease risk even when baseline disease is rarely ascertained. Confidence intervals for the logistic-Weibull model were tighter than that of the bootstrap confidence intervals for the non-parametric estimator (Table 5). The parametric assumption resulted in a 74% reduction in confidence interval for the baseline cumulative risk, and a smaller reduction at later time points. The reduction in confidence interval lengths can be considered a positive or a negative feature, depending on how much one believes the parametric assumptions.

The logistic-generalized gamma model (BIC=10,106) was a better fit to the data than the logistic-Weibull model (BIC=10,117). However, the logistic-generalized gamma model estimated zero hazards for the first 7 months following the initial HPV-positive/Pap-negative cotesting result; even though there was little data within this time period, zero hazards for HPV-infected women is unrealistic [27] and more likely a result of overfitting. Regardless of which distribution (Weibull, exponential, loglogistic, lognormal, generalized gamma, or gamma) was used for the incidence model, the cumulative risk curves were similar to one another in respect to the resulting recommendations for guidelines and were close fits to the non-parametric risk curve. We favor using the logistic-Weibull model over other parametric prevalence-incidence models, as it allows covariate effects to be described in terms of odds ratios for prevalent disease and hazard ratios for incident disease.

5.2 Implications for screening guidelines

Management of abnormal Pap screening results in the absence of an HPV test is well established. Women with atypical cells of undetermined significance (ASC-US) Pap results are asked to return for repeat screening in one year, while women with low-grade squamous intraepithelial lesion (LSIL) or worse Pap results are referred to immediate colposcopy [22]. We fitted the logistic-Weibull model to KPNC data and compared the cumulative risk curves for these groups of women to women with HPV-positive/Pap-negative cotesting results (Figure 2). For HPV-positive/Pap-negative women, the estimated baseline CIN3+ risk of 1.87% (95% CI: 1.59-2.19%) was lower than the 1.99% (95% CI: 1.24-3.17%) baseline CIN3+ risk estimated for women with ASC-US Pap results and much lower than the 3.87% (95% CI: 3.49-4.29%) baseline CIN3+ risk estimated for women with LSIL Pap results. Applying an equal management of equal risk principle [8], the baseline CIN3+ risk estimates suggest that women with HPV-positive/Pap-negative cotesting results should not be referred to immediate colposcopy.

The 1-year CIN3+ risk among women with HPV-positive/Pap-negative results (2.56%, 95% CI: 2.36-2.78%) was similar to the 1-year CIN3+ risk among women with ASC-US Pap results (2.50%, 95% CI: 1.97-3.17%). However, the hazards of incident CIN3+ was greater among women with HPV-positive/Pap-negative cotesting results than women with ASC-US Pap results, so that at 5 years, the cumulative risks of CIN3+ were 4.81% (95% CI: 4.53-5.11%) and 3.37% (95% CI: 2.84-4.00%) for women with HPV-positive/Pap-negative

and ASC-US Pap results, respectively. These risk estimates suggest that women with HPV-positive/Pap-negative results, like women with ASC-US Pap results, should return for a repeat cotesting screen in one year. However, for HPV-positive/Pap-negative results, clinicians will need to be especially cautious that women do not skip their return visits.

Women with HPV-positive/Pap-negative cotesting result may consist of sub-populations with distinctly different risk profiles [28]; additional information can be used to further personalize management. We considered how risk profiles may differ for women of different ages by fitting age as a categorical covariate in the logistic-Weibull model (Table 6). No age group had risks of prevalent CIN3+ high enough to warrant referral to immediate colposcopy. The two-year cumulative risks of CIN3+ among women of ages 45–49, 50–54, and 55–65 were 2.38% (95% CI: 1.89%-3.00%), 1.75% (95% CI: 1.30%-2.36%), and 2.41% (95% CI: 1.94%-2.99%), respectively. Compared to the 2.50% implicit cumulative risk threshold for returning women for repeat screening in 1-year that is implied by women with ASC-US Pap results, these risks suggest that a longer return time may be reasonably safe with older women. Further analysis that consider the benefits (eg. potential reduction in overtreatment) would need to be considered before recommending an extended screening interval for these age groups.

6. Discussion

Cohorts assembled from electronic health records at health providers can have irregularly interval-censored outcomes, and prevalent left-censored disease is undetermined when disease ascertainment is not conducted at the first available visit. We demonstrated that Kaplan-Meier methods are inappropriate and proposed a general family of mixture models, called prevalence-incidence survival models. We presented an EM algorithm to fit parametric prevalence-incidence models with covariates and obtained a non-parametric estimate (no covariates) by adapting standard NPMLE methods. The non-parametric estimate can be used to assess the fit of parametric prevalence-incidence models such as the logistic-Weibull. For a cohort undergoing cervical cancer screening at KPNC, Kaplan-Meier yielded poor risk estimates and the non-parametric cumulative risk is a step function with large jumps. In contrast, the logistic-Weibull yielded a smooth risk curve and agreed with the non-parametric estimates. The logistic-Weibull allows for covariate effects to be described in terms of odds ratios for prevalent disease and hazard ratios for incident disease and the Weibull distribution has previously been suggested for modeling cancer [19]. The ability to separate out the risk of disease present at baseline versus disease that occurs during follow-up is important for informing clinical decisions on whether to intervene with a surgical procedure at the initial screening visit (baseline). These findings support the choice of the logistic-Weibull model to estimate risks that underlie current U.S. risk-based cervical cancer screening guidelines [21].

Kaplan-Meier is biased under interval-censoring, even with ad hoc schemes to impute event onset within intervals [29]. We demonstrated that the bias has an interesting pattern: underestimation of risks at early times and overestimation of risks at later times. This bias is exacerbated by the presence of prevalent left-censored outcomes. Most work on left-censoring involves inference on the past time of onset and assumes it is known a priori

whether outcomes are left-censored (prevalent) or interval-censored (incident) [30]. For clinical use, a simple estimate of the total amount of prevalent disease as a point-mass at zero can suffice. Definitive disease ascertainment may not be conducted at the first available visit, so that some disease diagnosed during follow-up are also pre-existing disease.

The proposed mixture model is particularly applicable to our data, because women who test HPV-positive/Pap-negative at the first available screen consist of two populations: (1) women with long-term HPV infections who, may already have CIN3+, and (2) women with recently acquired HPV infections, most of whom will clear their infections, but can have future CIN3+ if the infection persists [28]. We believe that Kaplan-Meier methods should be avoided. The non-parametric estimate is robust, but constant for long intervals followed by large jumps, and loses efficiency due to the slow $n^{1/3}$ asymptotic convergence rate [31]. The best methodology is to fit a parametric model, such as the logistic-Weibull, and check that it is a good fit to the non-parametric estimate. Our findings support the choice of using logistic-Weibull models for KPNC data to estimate the risks that underlie current US cervical screening guidelines.

Two extensions of prevalence-incidence models would be useful. The first is to develop semi-parametric versions of the prevalence-incidence models that incorporate covariates. Fitting a Cox model to interval-censored data has previously been studied [32, 33, 34]. These methods might be adapted to prevalence-incidence survival models. The second is to develop methodology to fit prevalence-incidence models to general epidemiologic study designs, such as case-control studies, while accounting for complex sampling.

Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

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Figure 1. Cumulative Risk of CIN3+ for HPV+/Pap- in a Screened Population
 % cumulative risk of cervical intraepithelial neoplasia grade 3 and cancer (CIN3+) following a HPV-positive/Pap-negative result at the initial screen

Figure 2. Comparing CIN3+ Cumulative Risk for HPV+/Pap- to that of ASC - US and LSIL Pap
Curves showing the % cumulative risk of cervical intraepithelial neoplasia grade 3 and cancer (CIN3+) following (1) HPV-positive/Pap-negative cotesting results, (2) Pap result of atypical cells of undetermined significance (ASC-US), and (3) Pap result of low-grade squamous intraepithelial lesion (LSIL).

Table 1

Performance of the Kaplan-Meier (KM) cumulative risk estimator using time of diagnosis to approximate time of disease onset. N subjects whose time of disease onset have cumulative distribution function, F , are randomly seen at one of two times: θn are seen at time t_1 and $(1 - \theta)n$ are seen at time t_2 .

Time	At Risk	Diagnosed	KM Cumulative Risk Estimate	True Cumulative Risk
t_1	n	$n\theta R(t_1)$	$\theta R(t_1)$	$R(t_1)$
t_2	$(1 - \theta)n$	$(1 - \theta)nR(t_2)$	$1 - (1 - \theta R(t_1))(1 - R(t_2))$	$R(t_2)$

Table 2

Performance of the logistic-Weibull prevalence-incidence model when the model is not misspecified and with low disease ascertainment at baseline. β_0 , β_1 , and β_2 are coefficients for the logistic regression portion of the model; γ_0 , γ_1 , and γ_2 are regression coefficients for the Weibull scale and τ is the inverse of the Weibull shape. $R(T=t)$ is the cumulative risk at time t for those with a specific set of covariates. % Bias is negative to denote underestimation and positive to denote overestimation. ASE is the asymptotic standard error. ESE is the empirical standard error. CP is the coverage probability.

Parameter	True	% Bias	ASE	ESE	CP
β_0	-3.5	-0.25	0.13	0.13	0.952
β_1	0.5	0.86	0.10	0.10	0.943
β_2	1.0	0.26	0.18	0.18	0.952
γ_0	3.5	0.06	0.028	0.028	0.951
γ_1	-0.5	0.08	0.021	0.022	0.942
γ_2	-0.5	-0.11	0.034	0.034	0.960
τ	0.5	0.38	0.0082	0.010	0.956
$R(T=0)$	0.076	-0.12	0.0049	0.0048	0.954
$R(T=1)$	0.080	0.02	0.0048	0.0047	0.952
$R(T=3)$	0.109	0.19	0.0045	0.0046	0.949
$R(T=5)$	0.166	0.17	0.0050	0.0051	0.946
$R(T=10)$	0.386	-0.08	0.0069	0.0069	0.949

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Table 3

Performance of the misspecified logistic-Weibull prevalence-incidence model under high and low disease ascertainment at baseline. $P(T = t)$ is the cumulative risk at time t for those with a specific set of covariates. % Bias is negative to denote underestimation and positive to denote overestimation. ASE is the asymptotic standard error. ESE is the empirical standard error. CP is the coverage probability.

Parameter	High Ascertainment					Low Ascertainment				
	True	% Bias	ASE	ESE	CP	% Bias	ASE	ESE	CP	
$P(T=0)$	0.081	-0.9	0.0039	0.0038	0.952	-8.3	0.0045	0.0044	0.726	
$P(T=1)$	0.082	0.7	0.0039	0.0038	0.949	-5.9	0.0045	0.0043	0.830	
$P(T=3)$	0.090	4.8	0.0039	0.0039	0.815	0.5	0.0043	0.0042	0.963	
$P(T=5)$	0.106	6.7	0.0041	0.0040	0.563	4.5	0.0044	0.0042	0.812	
$P(T=10)$	0.173	3.8	0.0051	0.0049	0.748	3.9	0.0053	0.0051	0.748	

Table 4

Percent bias and coverage probability (CP) for the non-parametric cumulative risk estimate under different levels of disease ascertainment at baseline: high (H), moderate (M), and low (L). % Bias is negative to denote underestimation and positive to denote overestimation.

Parameter	True	% Bias (H)	% Bias (M)	% Bias (L)
$P(T=0)$	0.076	0.08	-0.03	-0.55
$P(T=1)$	0.078	0.05	-0.11	-0.10
$P(T=3)$	0.096	0.11	0.03	0.01
$P(T=5)$	0.130	0.03	0.15	0.12
$P(T=10)$	0.280	-0.06	-0.05	0.05

% cumulative risk and 95% confidence intervals of acquiring cervical intraepithelial neoplasia grade 3 or cancer (CIN3+) following a HPV-positive/Pap-negative result at the initial screen as estimated by the non-parametric estimator and by logistic-Weibull prevalence incidence models. The % interval reduction (IR) is the percent reduction in confidence interval length from the parametric assumptions.

Table 5

Year	Non-parametric			Logistic-Weibull			% IR
	Est.	LCL	UCL	Est.	LCL	UCL	
0	1.99	0.00	2.30	1.87	1.59	2.19	74
1	1.99	1.70	2.30	2.56	2.36	2.78	30
2	3.28	2.90	3.55	3.17	2.95	3.39	32
3	3.81	3.47	4.11	3.73	3.51	3.98	27
4	4.49	4.12	4.80	4.28	4.03	4.55	24
5	5.31	4.60	5.67	4.81	4.53	5.11	46
6	5.31	5.03	5.83	5.33	5.01	5.67	60
7	5.68	5.25	6.12	5.84	5.47	6.24	11

Table 6

Result of fitting a logistic-Weibull model with categorical age to women with an initial HPV-positive/Pap-negative cotesting result at Kaiser Permanente Northern California. % Sample is the percentage of women with HPV-positive/Pap-negative cotesting result in that age category. OR are odds ratio of having CIN3+ prevalent at the initial cotesting screen for that age group compared to the reference group (age 30–34). HR are hazard ratios of acquiring incident CIN3+ after the initial cotesting screen for that age group compared to the reference group (age 30–34). % Prevalent Risk refers to the percent risk of having CIN3+ prevalent at the initial cotesting screen. 1 Year, 2 Years, and 3 Years % CR refers to the percent cumulative risk of having CIN3+ 1 year, 2 years, and 3 years after the initial cotesting screen, respectively.

Age category	% Sample	OR	HR	% Prevalent Risk	1 Year % CR	2 Years % CR	3 Years % CR
30–34	37.7	1.00	1.00	1.91	2.88	3.75	4.57
35–39	18.4	1.13	0.63	2.14	2.76	3.30	3.83
40–44	13.7	1.38	0.59	2.61	3.17	3.68	4.16
45–49	10.6	0.88	0.38	1.67	2.05	2.38	2.71
50–54	8.4	0.55	0.37	1.06	1.42	1.75	2.06
55–65	11.2	0.63	0.64	1.21	1.85	2.41	2.94