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Size and Charge Dependence of Ion Transport in Human Nail Plate

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Abstract

The electrical properties of human nail plate are poorly characterized, yet are a key determinate of the potential to treat nail diseases such as onychomycosis using iontophoresis. In order to address this deficiency, molar conductivities of 17 electrolytes comprising 12 ionic species were determined in hydrated human nail plate *in vitro*. Cation transport numbers across the nail for 11 of these electrolytes were determined by the electromotive force method. Effective ionic mobilities and diffusivities at infinite dilution for all ionic species were determined by regression analysis. The ratios of diffusivities in nail to those in solution were found to correlate inversely with the hydrodynamic radii of the ions according to a power law relationship having an exponent of -1.75 ± 0.27 , a substantially steeper size dependence than observed for similar experiments in skin. Effective diffusivities of cations in nail were three-fold higher than those of comparably sized anions. These results reflect the strong size and charge selectivity of the nail plate for ionic conduction and diffusion. The analysis implies that efficient transungual iontophoretic delivery of ionized drugs having radii upwards of 5 Å (approximately MW 340 Da) will require chemical or mechanical alteration of the nail plate.

Keywords

Diffusion; Iontophoresis; Membrane transport; Mobility; Nail; Permeability; Structure-transport relationship

INTRODUCTION

Onychomycosis accounts for nearly 50% of all nail disorders and affects 2–18% or more of world's population.^{1–6} Although the condition is treatable, the current therapeutic options are limited due to efficacy and safety issues. Oral therapy for the treatment of onychomycosis is recommended by only 35–65% of the physicians due to the associated side effects such as headache, risk of hepatotoxicity and potential drug–drug interactions.⁵ The clinical significance of formulations such as medicated nail lacquers, patches and

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creams for topical treatment of onychomycosis is debatable. New techniques such as use of chemical penetration enhancers,^{7–10} micro-drilling,¹¹ nail abrasion,^{12–14} acid etching¹⁵ and iontophoresis^{16–24} are also being evaluated as potential treatment methods for onychomycosis. The drug-device combination which uses iontophoresis to deliver high concentrations of medication directly to the site of action has considerable potential to improve the treatment of onychomycosis.^{16–24} Although significant efforts have been made to evaluate and enhance transungual iontophoretic drug delivery, little has been done to systematically characterize ion transport across the nail plate. It is fair to say that work to date on transungual ion transport has been largely phenomenological, with little guidance from electrotransport theory.

The main objective of this research was to evaluate the impact of ionic size and charge on transungual transport of both organic and inorganic ions. Transport parameters including ionic conductance at infinite dilution, ionic mobility and diffusion coefficient of 12 ionic species in hydrated nail plate were obtained by performing conductivity and transport number studies using *in vitro* electrochemical and radiochemical methods. Also, gravimetric experiments were performed to determine the extent of hydration and keratin fiber volume fraction of the nail plate. Results are compared to similar information obtained recently for charged solutes in human stratum corneum²⁵ as amended²⁶ and to passive diffusion data for uncharged solutes in human nail plate.²⁷ A procedure for using the conductivity results to predict transungual iontophoretic drug delivery is proposed.

MATERIALS AND METHODS

Materials

Sodium chloride (NaCl), potassium chloride (KCl), calcium chloride (CaCl₂) and potassium bromide (KBr) were obtained from Fischer Scientific (Pittsburgh, PA); sodium bromide (NaBr), sodium sulfate (Na₂SO₄), tetraethylammonium bromide (TEABr), tetraethylammonium chloride (TEACl), sodium acetate (Na-Ac), tetraethylammonium acetate (TEA-Ac), tetraphenylphosphonium bromide (TPPBr), tetraethylammonium benzoate (TEA-Bz) and olamine hydrochloride (Olam-Cl) from Sigma-Aldrich (St. Louis, MO); calcium bromide (CaBr₂) and potassium sulfate (K₂SO₄) from GFS Chemicals (Powell, Ohio); sodium benzoate (Na-Bz) from Alfa Aesar (Ward Hill, MA) and methyltriphenylphosphonium bromide (MTPPBr) from StremChemicals (Newburyport, MA). CaCl₂ and CaBr₂ had stated purity of 96%, TPPBr 97%, MTPPBr 98% and rest of the chemicals were 99% pure. KCl conductivity standard solutions (1,000 μ mho/cm and 10,000 μ mho/cm at 25°C) were obtained from LabChem Inc. (Pittsburgh, PA). All aqueous solutions were prepared in deionized water (18.2 M Ω -cm at 25°C, U.S. Filter). Dialysis membranes (MWCO 6000Da) were obtained from Bel-Art Products (Wayne, NJ). Optically clear silicone elastomer MED-6033 was obtained from NuSil Technology LLC (Carpinteria, CA). ²²NaCl (100–2000Ci/g) and ¹⁴C-TEABr (3.5mCi/mmol) were purchased from Perkin Elmer Life and Analytical Sciences (Boston, MA). Ag-AgCl electrodes, E215 and E252P were obtained from In-Vivo Metric (Healdsburg, CA).

Nail Sample Preparation

Frozen, human cadaver fingernails (Caucasian male, age 26 – 86) were obtained from Science Care Anatomical (Phoenix, AZ). A total of 75 index, middle and ring fingernails from both left and right hands of 13 donors were selected for the experiments. The frozen nail plates were thawed at room temperature ($25 \pm 2^\circ\text{C}$) in DI water and cleaned by removing adhering tissues with forceps and cotton swabs. The nails were then rinsed with DI water and inspected for any visual deformities such as cracks or hairline fractures. The thickness of nail plates, ranging from 0.21 to 0.85 mm, was measured by using a point micrometer (Mitutoyo, Kawasaki, Kanagawa, Japan). The use of human cadaver nails was approved by the Institutional Review Board at the University of Cincinnati, Cincinnati, OH.

Nail Adapter Preparation

The nail adapters were fabricated from a thermally curable silicone elastomer MED-6033 which was comprised of two parts. These materials were mixed together in equal proportions by volume and allowed to stand for 2–3 hours to remove air bubbles formed during the mixing process, prior to pouring into the molds. The silicone mix within the molds was then cured for 30 minutes at $60 \pm 2^\circ\text{C}$ to form sturdy, but flexible nail adapter halves. A circular hole, 9 mm in diameter (0.64 cm^2) was punched in the center of both halves of the silicone nail adapter. The shape and design of these custom-made silicone nail adapters were similar to Teflon nail adapters made by PermeGear Inc. (Bethlehem, PA); however they had an additional advantage of not requiring adhesive glue, which is used to seal the gaps between the nail and Teflon nail adapters. These custom-made silicone nail adapters accommodated the nail curvature better than Teflon adapters and demonstrated no inter-compartmental leakage in preliminary experiments.

Nail Hydration Studies

Hydration experiments were performed on six finger nails selected randomly from different donor sets. Nail plates were immersed in DI water in a glass vial and placed in a water bath ($32.0 \pm 0.1^\circ\text{C}$) for 24 h. The nail samples were removed after 24 h, excess water was wiped off with Kimwipes® and cotton swabs, and then wet mass (m_{wet}) of the nail plate was measured on an analytical balance (Mettler Toledo AB-135SP®) reading to $\pm 0.01\text{ mg}$. The nail samples were then dried at 60°C overnight or until constant weight was achieved (m_{dry}). The water content w (wt%) in hydrated nail plate was determined by Eq. 1. The water uptake capacity of dry nail plate (ν') was determined by using Eq. 2.

$$w(\text{wt}\%) = \frac{m_{\text{wet}} - m_{\text{dry}}}{m_{\text{wet}}} \times 100\% \quad (1)$$

$$\nu'(\text{gH}_2\text{O/g dry nail}) = \frac{m_{\text{wet}} - m_{\text{dry}}}{m_{\text{dry}}} \quad (2)$$

Assuming nail plate to be comprised only of keratin and water, the fiber volume fraction (ϕ_f) is given by:²⁸

$$\varphi_f = 1 - \frac{\rho_m \nu'}{\rho_1 + \rho_m \nu'} \quad (3)$$

where ρ_m is the density of dry nail (keratin density $\sim 1.3 \text{ g}\cdot\text{cm}^{-3}$)²⁹ and ρ_1 is the density of water ($\sim 1.0 \text{ g}\cdot\text{cm}^{-3}$).

Conductivity Measurements

The molar conductivities of all the electrolyte solutions and of human nail plate immersed therein were determined by a four terminal resistance method^{25,30,31} in side-by-side diffusion cells (PermeGear Inc., Bethlehem, PA). The method was that used in Franz diffusion cells by LaCount and Kasting²⁵ except for variations as described below. Commercially available cylindrical Ag-AgCl electrodes, E215 and E252P (In-Vivo Metric, Healdsburg, CA), were used for all electrolytes except for those containing bromide. For the latter, homemade Ag-AgBr electrodes were employed, as Ag-AgCl electrodes are fouled by bromide ions.³² Ag-AgBr electrodes were constructed from a 1.0 mm diameter silver wire (99.999% - Alfa Aesar, Ward Hill, MA) electrolyzed in 0.1M KBr solution and were stored in the dark prior to use due to its sensitivity to light. Electrodes were placed as shown in Fig. 1. The 98.28 k Ω standard resistor described previously²⁵ was replaced by a 10.01 k Ω ($\pm 0.02\%$) precision standard resistor (Ohm-labs Inc., Pittsburgh, PA) in order to better match the 3– 10 K Ω resistance of the hydrated nail plate immersed in physiological saline solution.³³ A 10 V peak-to-peak, 20 Hz sinusoidal signal was applied across a 1 M Ω current-limiting resistor using a waveform generator (Agilent 33220A) to yield a 6.5–6.9 μA root-mean-square AC current across the nail plate. The AC potential generated across the nail plate (maximum of 0.5 V peak-to-peak) was measured by the inner pair of electrodes using a sensitive multimeter (Agilent 34410A). The multimeter was alternatively connected to the 10 k Ω standard resistor by a double pole double throw toggle switch (represented by broken lines in Fig. 1) which facilitated the measurement of potential drop across the standard. The use of low magnitude, low frequency AC signals ensures that the treatment has little impact on tissue electrical properties and that the impedance is primarily resistive rather than capacitive in nature.³⁴

Solution-only measurements were made at 25°C with the nail adapter in place, but without the nail plate. Cell constants K (cm^{-1}), corresponding to the effective ratio of path length ℓ to cross sectional area A , were determined by a two point calibration using KCl standards (1,000 $\mu\text{mho}/\text{cm}$ and 10,000 $\mu\text{mho}/\text{cm}$ at 25°C). The average distance ℓ between the sensing electrodes was 2.7cm and varied from one cell to another by $\pm 0.3 \text{ cm}$ due to inherent variation in cell design. The resistance imparted by each electrolyte, R_{soln} (Ω), was measured at eight concentrations in the range 0.007–0.154 M for monovalent electrolytes and 0.007–0.077 M for polyvalent electrolytes. These values were converted to molar conductivity of the electrolytes Λ_{soln} ($\text{cm}^2\text{mol}^{-1}\Omega^{-1}$) using the relationship $\Lambda_{\text{soln}} = K/(R_{\text{soln}}c)$, where c is the electrolyte concentration expressed in $\text{mol}\cdot\text{cm}^{-3}$. Molar conductivity at infinite dilution, Λ_{soln}^0 , was calculated as the y-intercept of a plot of Λ_{soln} versus $\sqrt{c}$, i.e. the Kohlrausch plot.²⁵ Values of Λ_{soln}^0 so determined were compared with literature values³⁵ to test the accuracy of the method.

For the nail conductivity measurements, cadaveric human nail plates (3 per electrolyte) were placed between the nail adaptors within the diffusion cells, and the temperature was maintained at $32.0 \pm 0.1^\circ\text{C}$. The samples were hydrated for 24 hours in deionized water and then exposed to increasing concentrations of electrolytes in the same range as the solution experiments. Each concentration was maintained for a duration of 24 h before measuring the resistance, yielding a total study time of 9 days for each nail sample. The electrolyte solutions were used without pH adjustment in order to avoid any contribution to conductivity from buffering ions. The pH values of all the solutions were measured to be in the range 5.5–7.5 before the experiment and 5.6–7.8 after the experiment.

The resistance measured in this leg of the study, R_{total} , contains contributions from both the nail and solution, i.e. $R_{\text{total}} = R_{\text{nail}} + R_{\text{soln}}$. To obtain R_{nail} , R_{soln} values at 25°C at each concentration (obtained from the solution-only experiments) were first corrected to 32°C by multiplying by the water viscosity ratio, $\eta^{32}/\eta^{25} = 0.765\text{cp}/0.891\text{cp} = 0.859$, then subtracted from R_{total} . Values of R_{nail} so calculated were found to comprise 85 to 98 percent of R_{total} . Nail specific resistivity values, $\rho_{\text{nail}} = R_{\text{nail}} A/L$, were calculated using the exposed cross sectional area (A) and thickness (L) of the nail sample, then converted to effective molar conductivities in nail ($\text{cm}^2\text{mol}^{-1}\Omega^{-1}$) using the relationship $\Lambda_{\text{nail}} = 1/(\rho_{\text{nail}}c)$, where c is the external electrolyte concentration expressed in $\text{mol}\cdot\text{cm}^{-3}$. Note that this calculation does not employ the cell constant K . There is an assumption built into the calculation that will be discussed later, namely the use of the external electrolyte concentration to calculate Λ_{nail} .

The limiting molar conductivity at infinite dilution (Λ_{nail}^0) was determined from the Kohlrausch plot. For all the nail experiments the two lowest concentration data were excluded from the fit, since significant positive deviations from the Kohlrausch law were observed. Conductivity data for selected electrolytes in solution and nail plate are included in the Supplemental Material.

Transport Number Measurements

The stationary state electromotive force (EMF) method^{25,36–41} was employed to determine cation transport numbers for the electrolytes yielding reversible electrode reactions, namely chloride- and bromide-containing electrolytes, and for nail plates immersed therein. Ag/AgCl electrodes were employed for the Cl^- electrolytes and Ag/AgBr electrodes for Br^- electrolytes. Thus, a total of 22 cation transport numbers were determined, 11 in solution and 11 in nail. Solution transport number measurements were conducted at 25°C using two dialysis membranes to separate the two compartments as described by LaCount and Kasting.²⁵ The peak EMF values were measured after 30–45 seconds.

The nail transport number experiments were performed at 32°C on the same samples used in conductivity experiments to reduce variability. Following the conductivity experiments, the nails were equilibrated for 24 hours with electrolyte solution at the highest concentration under consideration (0.154M for monovalent electrolytes and 0.077M for polyvalent electrolytes). The solution in the left compartment (facing the dorsal side of nail) was then replaced with fresh solution of the same concentration (c_1) and the solution in the right compartment was varied from 0.0125M to 0.077M (c_2) ensuring that the concentration ratio c_1/c_2 was always 2. Five different concentration ratios were evaluated: 12.3, 7.7, 4.4, 3.1

and 2. At each concentration ratio, the system was allowed to equilibrate for 4 hours. The solutions in both the chambers were then replaced with fresh solutions of the same concentrations, and the stationary state EMF (volts) was measured after an additional 4 hours by inserting two pre-equilibrated electrodes connected to the Agilent 34410A multimeter. The system was magnetically stirred to minimize boundary layer effects on the measured potential.³⁶ The dimensionless mean cation transport number (t_{m+}) was calculated as:^{36–39}

$$\text{EMF} = \frac{\nu}{\nu_+} \frac{RT}{F} \frac{t_{m+}}{z_+} \ln \frac{c_2 \gamma_{2\pm}}{c_1 \gamma_{1\pm}} \quad (4)$$

where $\nu = \sum \nu_{\pm}$ is the total number of cations and anions per mole of salt, R is the gas constant ($8.314 \text{ J K}^{-1} \text{ mol}^{-1}$), T is temperature (K), F is Faraday's constant ($96,485 \text{ C mol}^{-1}$), z_+ is the cation valence, and the $\gamma_{i\pm}$ are mean ionic activity coefficients calculated according to extended Debye-Huckel theory.⁴²

$$\log \gamma_{\pm} = \frac{B z_1 z_2 \sqrt{\mu}}{1 + \sqrt{\mu}} \quad (5)$$

In Eq. 5 B is a constant having a value 0.509 for water at 25°C and 0.516 at 32°C and μ is the ionic strength.

For radiochemical transport measurements, nail samples were prepared, mounted and hydrated in side-by-side diffusion cells as described above. Cation transport numbers of NaCl and TEACl were determined under symmetrical, fully hydrated conditions at three different concentrations (0.007M, 0.04M and 0.154M). The donor and receptor chambers were filled with unlabeled solutions of NaCl (or TEACl) of same molarity and allowed to equilibrate for 24 hours. After 24 hours, the donor and receptor chambers were replaced with fresh unlabeled solutions. The donor chamber was then spiked with $1 \mu\text{Ci } ^{22}\text{NaCl}$ (100–2000 Ci/g) or $^{14}\text{C-TEABr}$ (3.5 mCi/mmol). Ag-AgCl electrodes prepared by electrolyzing Ag strip (99.9% purity - Alfa Aesar, Wardhill, MA) in 0.1N KCl solution were placed in the receptor compartment and Ag electrodes in the donor compartment. A constant direct current iontophoretic device, Phoresor II Auto, Model PM 850 (Iomed, Inc., Salt Lake City, UT) was used to drive the system, with the Ag electrode serving as the anode. A custom-made variable potentiometer was used to reduce the 100 μA minimum current supplied by the device to 10 μA . The resistance of the nail plate plus intervening solution was measured by the four terminal technique prior to the experiment and periodically thereafter. This was useful in adjusting the potentiometer to yield the desired current. The test durations for $^{22}\text{Na}^+$ and $^{14}\text{C-TEA}^+$ experiments were 16 and 56 h, respectively.

Aliquots of the donor solution (10 μL) and receptor solution (2 mL) were removed at predetermined time intervals. The receptor solution was replaced with 2 mL of fresh unlabeled electrolyte solution to maintain a constant volume. The samples were mixed with 10mL of UltimaGold™ scintillation fluid (PerkinElmer Life and Analytical Sciences, Shelton, CT) and analyzed with a liquid scintillation counter (Beckman Counter LS6500, Fullerton, CA). The steady-state flux of the permeant J_i ($\text{mol cm}^{-2}\text{s}^{-1}$) across the nail plate was calculated from the slope of the linear portion of the plot of cumulative moles of

permeant transported across the nail plate per unit area versus time. The transport number for the radiolabeled species was calculated from the steady-state flux and the current density I ($A\ cm^{-2}$) as:

$$t_i = \frac{|z_i| F J_i}{I} \quad (6)$$

Data Analysis

Data were analyzed as described in LaCount and Kasting,²⁵ but with the corrected membrane thickness given later.²⁶ According to Kohlrausch's law of independent migration of ions, the term Λ^0 can be decomposed into additive contributions from the individual ionic species and is given as:^{35,43}

$$\Lambda^0 = \sum \nu_i \lambda_i \quad (7)$$

Here, ν_i is the number of equivalents of species i per mole of salt and λ_i is its limiting equivalent conductance at infinite dilution. The relationship between transport number t_i^0 and molar conductivity at infinite dilution is given as:³⁵

$$t_i^0 = \nu_i \lambda_i / \Lambda^0 \quad (8)$$

A non-linear minimization procedure was performed on the 17 conductivity relationships (Eq. 7) and 11 transport number relationships (Eq. 8) for both nail and solution data to yield optimized values of λ_i for the 12 ionic species in the study.²⁵ The conventional ionic mobilities (u_i^0) in $cm^2 V^{-1} s^{-1}$ and ionic diffusivities (D^0) in $cm^2 s^{-1}$ at infinite dilution were calculated by using the relationships $u_i^0 = \lambda_i / |z_i| F$ and $D^0 = u_i^0 RT / |z_i| F$, respectively.³⁵ Because nail plate is not a homogeneous medium we will refer to mobility and diffusivity values so obtained in this medium as "effective" values.

Hydrodynamic radii were calculated according to the Stokes-Einstein relationship,³⁵

$$r_{SE} = k_b T / 6\pi\eta D^0 \quad (9)$$

Here k_b is Boltzmann's constant (1.3806×10^{-16} erg K⁻¹), T is absolute temperature (K) and η is the viscosity of water (0.00891 poise at 25°C). As a comparative measure of size, hydrated ionic radii (r_H) were obtained from the literature using the values proposed by Nightingale.⁴⁴ Values which were not published were read from the calibration curve⁴⁴ by using WebPlotDigitizer version 2.5. These values are larger than r_{SE} for solutes for which $r_{SE} < 5 \times 10^{-8}$ cm (5 Å). A third measure of size, originally proposed by Gierer and Wirtz⁴⁵ for small, uncharged solutes, was also considered. The rationale for focusing the analysis on r_{SE} is discussed in the Supplemental Material.

RESULTS

Nail Hydration Studies

The water content of the fully hydrated nail plate was found to be $w = 31 \pm 2\%$ (mean $\pm$ SD, $n = 6$). This value falls within the range of values reported in the literature (28–34%).^{7,8,28,46} The water uptake capacity of dry nail was found to be $v' = 0.44 \pm 0.05$ g H₂O/g dry nail. The keratin fiber volume fraction was calculated to be $\phi_f = 0.64 \pm 0.02$.

Conductivity Measurements

Equivalent conductances at infinite dilution of 17 electrolytes in solution (Λ_{soln}^0) and nail plate (Λ_{nail}^0) are shown in Table 1. Conductance values in the nail plate were reduced relative to those in free solution by factors ranging from 440 to 1380.

Transport Experiments

Cation transport numbers of 11 electrolytes in solution (t_{soln}^0) and hydrated nail plate (t_{nail}^0) determined by the EMF method are shown in Table 2. Transport numbers calculated from the regressed values of the individual ionic conductances and electrolyte composition are also presented. The ratio $t_{\text{nail}}^0/t_{\text{soln}}^0$ is shown in the last column. This ratio was significantly greater than one for the small, monovalent ions Na⁺ and K⁺, close to one for the medium-sized tetramethyl ammonium (TEA⁺) and olamine (OlamH⁺) ions, and significantly less than one for Ca²⁺ and the large, monovalent ions methyl triphenylphosphonium (MTPP⁺) and tetraphenylphosphonium (TPP⁺).

The transport numbers of Na⁺ and TEA⁺ ions in nail plate immersed in their respective chloride solutions determined by the radiochemical method are shown in Fig. 2. Two way ANOVA analysis ($\alpha = 0.05$), blocking on treatment and nail sample, showed that there were no significant differences between values determined by radiochemical and EMF methods. The lag times for achieving steady state flux for ²²Na⁺ and ¹⁴C-TEA⁺ experiments were approximately 4 and 20 h, respectively. Electrical current was nearly constant throughout the experiments, although a slight variation (~ 5–14% increase) was observed in a few samples for ¹⁴C-TEA⁺. This fluctuation may be attributed to variation in nail plate resistance (tissue condition) over the 56 h test period. Average current over the test period was used to calculate transport numbers. The variability associated with the change in current over time for ¹⁴C-TEA⁺ was less than the inter-nail variability.

Effective Ionic Mobilities and Diffusivities in Nail Plate

Calculated values of individual ionic conductivities, mobilities and diffusivities at infinite dilution of the 12 ionic species in hydrated nail plate are listed in Table 3. The aqueous diffusivities of these ions and two measures of their size are listed in Table 4.

In order to isolate the effects of the nail plate from the known behavior of ions in solution, we prepared log-log plots of the ratio of effective ionic diffusivity in nail (D_{nail}^0) to that in solution (D_{soln}^0) versus the hydrodynamic radius of each ion, r_{SE} . This ratio directly shows the impact of diffusive hindrance in the nail, above and beyond the resistance of the aqueous

medium. The results are shown in Fig. 3. It is evident that values of $D_{\text{nail}}^0/D_{\text{soln}}^0$ for cations at any given radius are higher than those for anions. Values are inversely related to ionic radius, with more scatter evident amongst the anions. It should be noted that D_{nail}^0 values for sulfate, benzoate and acetate ions were imprecisely determined (cf. the λ_1 values in Table 3) due to the small number of electrolytes and lack of transport number measurements for these species. The value for sulfate was particularly low. Because of this and the fact that its behavior in aqueous solution is already unusual,⁴² sulfate ion was excluded from the remainder of the analysis. Although this decision may be arbitrary, inclusion of sulfate would not qualitatively change the results that follow.

Linear regression of the data in Fig. 3 was conducted under the hypothesis that the magnitude of the effective ionic diffusivities in nail could be different for cations and anions, but the size dependence should be the same. Thus the slopes of the lines for cations were constrained to the same values. The regression equations were then transformed to power laws by taking the antilog. This procedure yielded

$$D_{\text{nail}}^0/D_{\text{soln}}^0 = 0.00522 r_{\text{SE}}^{-1.75} \text{ cations}$$

$$0.00170 r_{\text{SE}}^{-1.75} \text{ anions} \quad (10)$$

$$n=11; s=0.168; r^2=0.851$$

where the root mean square deviation s is expressed in base 10 log units. Equation 10 shows that the effective diffusivity of cations in nail plate exceeds that of comparably sized anions by a factor of $522/170 = 3.07$. We argue below that this difference actually reflects more favorable partitioning of cations than anions into the negatively charged nail plate, as would be expected from a Donnan equilibrium,⁴⁷ rather than higher intrinsic mobility.

Unconstrained fits of the data in Fig. 3 in which the slopes of the regression lines for cations and anions were allowed to differ gave nearly the same results as Eq. 10, when sulfate ion was excluded from the analysis. This was not the case when the hydrated radius, r_{H} , was substituted for the hydrodynamic radius, r_{SE} . The use of r_{H} also gave much steeper slopes, because the hydrated radii for very small ions greatly exceed their hydrodynamic radii (cf. Table 4, Cols 5 and 6).

DISCUSSION

Passive diffusion studies of uncharged solutes permeating human nail plate have shown little dependence on lipophilicity, but a steep dependence on size.⁴⁸ This result led these investigators and others^{49,50} to describe nail as a “hydrophilic gel membrane”, with resistance to diffusion provided by the keratin fibers suspended in a continuous aqueous medium. Notably, both Kobayashi et al.⁴⁸ and Mertin and Lippold⁴⁹ found that nail was less permeable to ionic solutes than to uncharged solutes, in contrast to earlier findings by Walters et al.⁵¹ They discussed this finding in the context of Donnan exclusion of charged

compounds from the negatively charged nail plate. Yet, the electrostatic coupling between cationic and anionic species in these passive diffusion experiments complicates this picture. The two species must diffuse together.⁵²

Conductivity measurements yield a different limit in which electrostatically-coupled diffusion is overwhelmed by the effect of the electric field.⁵² Mobilities and diffusivities of the individual species may be ascertained, at least in the dilute solution limit where ion-ion interactions are minimal.⁴³ The present measurements fall into this category. By extrapolating electrolyte conductivity measurements in human nail plate to infinite dilution and analyzing the results in conjunction with independently measured cation transport numbers, we were able to discover the pattern of behavior shown in Fig. 3. There are clear differences between cations and anions in the effective diffusivities in nail inferred from these measurements. Both show a strong size dependence, describable over the range $1 \text{ \AA} < r_{SE} < 5 \text{ \AA}$ in terms of a power law with an exponent of -1.75 ± 0.27 , but the magnitudes of the fitted curves vary between charge types, with those for cations exceeding those for comparably sized anions by about a factor of three. These results differ from a comparable analysis of ionic transport in skin, where the corresponding power law exponent was found to be -0.65 ± 0.29 and there was no discernable difference in the magnitude of diffusivity for cations and anions.^{25,26} A graphical comparison of these results is shown in Fig. 4. It is evident that nail is considerably more size-selective than skin for transverse transport of small ions.

In order to place the size dependencies in a familiar context, we fit a cylindrical pore hindered diffusion model for uncharged solutes (centerline approximation) to both the skin and nail data in Fig. 4. Details are given in the Supplemental Material to this report. The results are shown as dotted red lines in Fig. 4. The optimum pore radius for the skin data (Fig. 4a) was $16 \text{ \AA}$ (range $12\text{--}28 \text{ \AA}$), whereas the nail data (Fig. 4b) yielded a minimum centered at $11 \text{ \AA}$ (range $9\text{--}14 \text{ \AA}$). The pore model with a small pore radius predicted a substantial convex curvature to log-log plots of diffusivity versus size, which is not evident in Fig. 4b. For the nail, we considered also the fiber matrix models for uncharged solutes described in Baswan et al.²⁷ (see Supplemental Material). As in that report, neither of the models considered accurately described the results. The size-selectivity of the fiber matrix models was closer to that of nail plate than the cylindrical pore model; however, the absolute values of the calculated hindrance factors were substantially in error. Although nail plate seems (to us) to be a dense fiber matrix comprised predominately of keratin, it is evident that more development of diffusion theory for such systems is required to explain its permeability.

The analysis in this report, summarized in Eqs. 7–9 and described in more detail elsewhere,²⁵ is the standard analysis for solution electrochemistry. It is based on limiting ionic conductance determined from Kohlrausch plots, in which conductivity is plotted versus the square root of the molar electrolyte concentration, c . For solutions, c is known precisely, but for tissues bathed in an external electrolyte only the external concentration is known. Consequently the values of Λ_{nail}^0 determined in this study reflect a tissue/solution partition coefficient that is not present in solution measurements. This is why cations and anions of comparable size may have different values of effective diffusivity in the nail plate,

D_{nail}^0 . Due to the negative charge associated with nail keratin, cations partition more favorably into the membrane than do anions, resulting in higher internal concentrations, c_{nail} , and higher limiting ionic conductivities, λ_{nail} .

The question may be asked as to whether the results of this analysis may be used to predict iontophoretic transport in nail of other ions or the passive diffusion results of Kobayashi et al.⁴⁸ and others. For larger ions it is possible to estimate radii from correlations with molecular weight developed for uncharged solutes as discussed by Ibrahim et al.⁵³ Solution diffusivities can then be calculated by rearranging Eq. 9 and effective diffusivity in nail can be estimated by extrapolation of Eq. 10. However, under passive diffusion conditions in vivo, ionic drug transport is coupled to other ions in the donor solution as well as to those in the viable skin layers, especially sodium and chloride.⁵² Quantitative analysis of this problem for charged membranes and polyvalent ions involves solution of a complicated boundary value problem that will not be discussed here.⁵⁴ An update on this solution may be found in a recent PhD thesis from our group;⁵⁵ however, neither the original analysis nor the update deal with the hindrance provided by the keratin fiber matrix in the nail plate. Nevertheless, we show in Fig. 3 that the present estimates of the ratio $D_{\text{nail}}^0/D_{\text{soln}}^0$ are comparable to a similar ratio calculated for uncharged solutes in nail by Baswan et al.²⁷ The conductivity data are more precise than the passive diffusion data and allow a better estimate of the size dependence of diffusion for solutes in the 1–5 Å range. A modest extrapolation of the regressions given in Eq. 10 and Fig. 3, combined with appropriate electrostatic coupling,⁵² can be anticipated to yield plausible diffusion constants in human nail plate for therapeutic antifungal drugs having radii of 5–7 Å.²⁷

So how, indeed, can this information be synthesized to predict iontophoretic drug delivery through nail? We present in Table 5 a stepwise procedure that may be anticipated to yield useful estimates. Assumptions implicit in this analysis include (1) the electroneutrality approximation for solution of the Nernst-Planck flux equations⁵⁶ is valid for the nail system; (2) electro-osmotic effects are minimal (see Hao and Li⁵⁷ for a discussion); (3) ion transport numbers remain constant at the target current densities. Steps 2 and 3 require experience with electrolyte transport in membranes; nevertheless, the process is well defined. The biggest uncertainties are the estimation of membrane charge effects in Step 2 and the possible influence of electro-osmosis. A test of the proposed procedure is warranted.

CONCLUSIONS

Limiting ionic mobilities and diffusivities of twelve ionic species in solution and hydrated nail plate were determined by performing *in vitro* conductivity and EMF experiments with seventeen electrolytes. Permselectivity of the nail plate for cationic transport was found to be related to the size and valence of the cation; it was a 1.3- to 1.5-fold increment in transport number relative to solution values for the small, monovalent cations Na^+ and K^+ but vanished for large or polyvalent ions in the presence of smaller counter-ions. An inverse relationship between effective ionic diffusivity in nail and size, describable in terms of a power law with an exponent of -1.75 , was found for both cations and anions. Under the assumption that the size effect was the same for both species, effective diffusivities of cations in nail were more than three-fold greater than anions of comparable size, very likely

reflecting the preferential partitioning of cations into the negatively charged nail plate. A method for using this information to predict transungual iontophoretic delivery in nail is proposed.

Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

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Figure 1.
Diffusion cell configuration for four-terminal resistance measurements.

Figure 2.

Cation transport numbers in hydrated nail plate for (a) NaCl and (b) TEACl determined by the radiochemical method. The first column in each panel shows the mean value determined by the EMF method (Column 5 of Table 2).

Figure 3.

Double logarithmic plot of the effective diffusivity of ions in the nail plate relative to their diffusivity in solution plotted versus Stokes-Einstein radius, r_{SE} . The solid lines correspond to Eq. 10 in the text. Sulfate ion (open diamond) was excluded from the regression analysis. The red crosses represent passive diffusion data for uncharged solutes in nail assembled by Baswan et al.²⁷

Figure 4.

Effective ionic diffusivity ratios with respect to aqueous solution for (a) skin^{25,26} and (b) nail (this study), plotted as a function of hydrodynamic radius of the ion. The straight lines correspond to the power law regressions described in LaCount and Kasting²⁶ and Eq. 10, respectively (solid lines – cations; dashed lines – anions). The dotted red lines correspond to fits of a cylindrical pore model to the data, as described in the Supplemental Material. (a) $r_p = 16 \text{ Å}$, $\varepsilon/\tau = 2.6 \times 10^{-5}$; (b) $r_p = 11 \text{ Å}$, $\varepsilon/\tau = 1.88 \times 10^{-3}$.

Table 1

Limiting equivalent conductance values (mean $\pm$ SD) of electrolytes in aqueous solution (Λ^0_{soln}) and hydrated nail plate (Λ^0_{nail}) at infinite dilution.

Electrolyte	$\Lambda^0_{\text{soln}}{}^a$ ($\text{cm}^2\text{mol}^{-1}\Omega^{-1}$)		$\Lambda^0_{\text{nail}}{}^b$ ($\text{cm}^2\text{mol}^{-1}\Omega^{-1}$)	$\Lambda^0_{\text{nail}}/\Lambda^0_{\text{soln}}{}^c$ $\times 100$
	Observed	Literature ^d		
NaCl	126.4 $\pm$ 1.7	126.4	0.277 $\pm$ 0.030	0.188
NaBr	127.3 $\pm$ 1.7	128.2	0.293 $\pm$ 0.031	0.196
Na-Ac	89.2 $\pm$ 1.0	91.0	0.208 $\pm$ 0.027	0.196
Na-Bz	82.6 $\pm$ 1.8	82.4	0.212 $\pm$ 0.004	0.221
KCl	149.2 $\pm$ 3.4	149.8	0.372 $\pm$ 0.026	0.213
KBr	150.7 $\pm$ 3.2	151.6	0.399 $\pm$ 0.025	0.226
TEACl	108.8 $\pm$ 1.7	108.9	0.161 $\pm$ 0.016	0.127
TEABr	113.9 $\pm$ 1.7	110.7	0.174 $\pm$ 0.023	0.135
TEA-Ac	72.6 $\pm$ 0.7	73.5	0.061 $\pm$ 0.011	0.071
TEA-Bz	64.8 $\pm$ 2.0	64.9	0.065 $\pm$ 0.005	0.086
MTPPBr	100.2 $\pm$ 0.6	-	0.163 $\pm$ 0.011	0.140
TPPBr	93.4 $\pm$ 0.9	-	0.158 $\pm$ 0.005	0.145
Olam-HCl	116.9 $\pm$ 1.2	118.5	0.190 $\pm$ 0.012	0.138
$\frac{1}{2}$ CaCl ₂	135.9 $\pm$ 9.9	135.8	0.191 $\pm$ 0.032	0.121
$\frac{1}{2}$ CaBr ₂	135.9 $\pm$ 10.3	137.6	0.235 $\pm$ 0.024	0.147
$\frac{1}{2}$ Na ₂ SO ₄	130.7 $\pm$ 5.9	130.1	0.201 $\pm$ 0.019	0.133
$\frac{1}{2}$ K ₂ SO ₄	149.3 $\pm$ 4.5	153.5	0.260 $\pm$ 0.027	0.145

^a25°C

^b32°C

^c Λ^0_{soln} experimental values corrected to 32°C by multiplying by the viscosity ratio, $\eta^{25}/\eta^{32} = 1.165$

^dRobinson and Stokes³⁵

Table 2

Cation transport numbers t_{+}^0 in solution and nail plate.

Electrolyte	Solution			Nail		t_{+nail}^0/t_{+soln}^0
	Obs ^a	Calc ^b	Lit ^c	Obs ^d	Calc ^e	
NaCl	0.392 ± 0.005	0.390	0.40	0.581 ± 0.012	0.577	1.48
NaBr	0.385 ± 0.003	0.386	0.39	0.552 ± 0.005	0.545	1.41
KCl	0.495 ± 0.005	0.486	0.49	0.685 ± 0.007	0.655	1.35
KBr	0.484 ± 0.006	0.482	0.48	0.622 ± 0.015	0.625	1.30
TEACl	0.280 ± 0.005	0.279	0.30	0.297 ± 0.006	0.314	1.13
TEABr	0.273 ± 0.008	0.275	0.29	0.321 ± 0.029	0.287	1.04
Olam- HCl	0.356 ± 0.0003	0.354	0.36	0.362 ± 0.016	0.359	1.01
CaCl ₂	0.381 ± 0.027	0.392	0.44	0.186 ± 0.018	0.222	0.57
CaBr ₂	0.389 ± 0.004	0.388	0.43	0.206 ± 0.003	0.201	0.52
MTPPBr	0.194 ± 0.006	0.194	-	0.045 ± 0.003	0.045	0.23
TPPBr	0.183 ± 0.009	0.182	-	0.050 ± 0.013	0.050	0.27

^a Experimental value (mean ± SD) by EMF method at 25°C

^b Calculated from Eq. 8 using the values of λ_i in Column 3 of Table 3

^c Calculated from Eq. 8 using the values of λ_i in Column 4 of Table 3

^d Experimental value (mean ± SD) by EMF method at 32°C

^e Calculated from Eq. 8 using the values of λ_i in Column 2 of Table 3

^f Ratio of Column 6 to Column 3

Limiting ionic conductances (λ_i), effective mobilities (μ^0) and effective diffusivities (D^0) calculated from the data in Tables 1 and 2.

Table 3

Ionic species	λ_i $\text{cm}^2\text{mol}^{-1}\Omega^{-1}$			$\mu^0 \times 10^5$ $\text{cm}^2\text{V}^{-1}\text{s}^{-1}$			$D^0 \times 10^7$ cm^2s^{-1}		
	Nail <i>a,b</i>	Soln ^c	Lit ^d	Nail <i>a</i>	Nail <i>a</i>	Nail <i>a</i>	Nail <i>a</i>	Nail <i>a</i>	Nail <i>a</i>
Na ⁺	0.182 ± 0.023	51.0 ± 4.9	50.1	0.188	0.188	0.188	0.495	0.495	0.495
K ⁺	0.253 ± 0.030	75.3 ± 6.5	73.5	0.262	0.262	0.262	0.688	0.688	0.688
TEA ⁺	0.061 ± 0.011	30.7 ± 3.5	32.6	0.063	0.063	0.063	0.166	0.166	0.166
Ca ²⁺	0.076 ± 0.017	102.8 ± 8.6	119.0	0.039	0.039	0.039	0.052	0.052	0.052
OlamH ⁺	0.075 ± 0.018	43.6 ± 6.3	42.2	0.077	0.077	0.077	0.203	0.203	0.203
TPP ⁺	0.008 ± 0.009	18.0 ± 3.9	-	0.008	0.008	0.008	0.022	0.022	0.022
MTPP ⁺	0.007 ± 0.009	19.5 ± 3.9	-	0.007	0.007	0.007	0.020	0.020	0.020
Cl ⁻	0.133 ± 0.014	79.6 ± 5.2	76.3	0.138	0.138	0.138	0.362	0.362	0.362
Br ⁻	0.151 ± 0.016	80.9 ± 5.2	78.1	0.157	0.157	0.157	0.412	0.412	0.412
SO ₄ ²⁻	0.027 ± 0.064	153.7 ± 20.0	160.0	0.014	0.014	0.014	0.018	0.018	0.018
Bz ⁻	0.017 ± 0.051	32.9 ± 18.2	32.3	0.018	0.018	0.018	0.047	0.047	0.047
Ac ⁻	0.013 ± 0.051	40.1 ± 18.2	40.9	0.014	0.014	0.014	0.036	0.036	0.036

^a_{32°C}

^b Values given as mean ± 67% confidence limit

^c 25°C. Values given as mean ± 95% confidence limit

^d Literature values in solution at 25°C³⁵

Table 4
Aqueous diffusivities at infinite dilution corrected to 32°C and two measures of ionic size.

Ionic species	MW Da	$D^0_{\text{soln}} \times 10^7, \text{cm}^2\text{s}^{-1}$		r_{SE}^a (Å)	r_{H}^b (Å)
		Observed ^c	Literature ^d		
Na ⁺	23	161.8	159.1	1.84	3.58
K ⁺	39	239.0	233.4	1.25	3.31
TEA ⁺	130	97.6	103.5	2.82	4.00
Ca ²⁺	40	81.6	94.5	3.09	4.12
OlanH ⁺	61	138.5	134.0	2.18	3.70
TPP ⁺	339	57.1	-	5.11 ^f	5.16
MTPP ⁺	277	61.9	-	4.72 ^f	4.94
Cl ⁻	35	252.7	242.4	1.21	3.32
Br ⁻	80	257.0	248.1	1.18	3.30
SO ₄ ²⁻	96	122.0	127.0	2.30	3.79
Bz ⁻	121	104.4	102.5	2.85	4.03
Ac ⁻	59	127.3	129.9	2.25	3.75

^a Stokes-Einstein radius calculated from Eq. 9 and literature value of D^0_{soln}

^b Hydrated ionic radius⁴⁴

^c Calculated from data in column 3 of Table 3

^d Calculated from data in column 4 of Table 3

Table 5

Procedure for estimating iontophoretic delivery in nail from effective ionic diffusivity data and regression (Eq. 10).

1	Assemble molar concentrations and valence of each diffusible ion present in the drug delivery compartment and in the body. For the latter, an electrolyte composition of 0.154 M NaCl, pH 7.4, is a suitable starting point.
2	Estimate hydrodynamic radii, r_{SE} , for all ions, then calculate their aqueous diffusivities at skin temperature using the Stokes-Einstein relationship (Eq. 9). Estimate effective diffusivities in nail using Eq. 10. If the pH in the donor compartment is substantially lower than the range 5.5 – 7.8 represented by Eq. 10, use a judicious estimate of the fixed charge on the nail plate to appropriately adjust cation and anion diffusivities within the range bounded by Eq. 10. For example, if the pH of the donor compartment was 4, the fixed charge of the nail plate would approach zero, and cation and anion diffusivities for similar sized species would be expected to be equal.
3	<p>a. <i>Compositions containing monovalent ions only.</i> Use the Nernst-Planck solution for uncharged membranes under the electroneutrality approximation⁵⁶ to estimate the flux of each ion as a function of potential drop across the membrane, ϕ. Cases 1 and 2 in the cited reference give examples of how to do this. Calculate ion transference numbers, t_i, for each diffusing species by dividing ion flux, J_i, by the total calculated iontophoretic current, I_{calc}, associated with ϕ.</p> <p>b. <i>Compositions containing monovalent and polyvalent ions.</i> The Nernst-Planck solution for ions of multiple valences in charged membranes^{54,55} must be used in lieu of Ref. 56 in order to calculate J_i and t_i. Spreadsheets implementing these calculations are available from the authors.</p>
4	Calculate the flux of the ion of interest as a function of the experimental iontophoretic current, I_{exp} , as $J_i = t_i \times I_{exp}$.