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Multiscale methods for computational RNA enzymology

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Abstract

RNA catalysis is of fundamental importance to biology and yet remains ill-understood due to its complex nature. The multi-dimensional “problem space” of RNA catalysis includes both local and global conformational rearrangements, changes in the ion atmosphere around nucleic acids and metal ion binding, dependence on potentially correlated protonation states of key residues and bond breaking/forming in the chemical steps of the reaction. The goal of this article is to summarize and apply multiscale modeling methods in an effort to target the different parts of the RNA catalysis problem space while also addressing the limitations and pitfalls of these methods. Classical molecular dynamics (MD) simulations, reference interaction site model (RISM) calculations, constant pH molecular dynamics (CpHMD) simulations, Hamiltonian replica exchange molecular dynamics (HREMD) and quantum mechanical/molecular mechanical (QM/MM) simulations will be discussed in the context of the study of RNA backbone cleavage transesterification. This reaction is catalyzed by both RNA and protein enzymes, and here we examine the different mechanistic strategies taken by the hepatitis delta virus ribozyme (HDVr) and RNase A.

Keywords

multiscale modeling; RNA catalysis; molecular dynamics; QM/MM; 3D-RISM; CpHMD; HREMD

1 Introduction

RNA plays several key roles in cellular function (Guttman & Rinn, 2012; Garst, Edwards, & Batey, 2011), ranging from the regulation of gene expression and signaling pathways to catalysis of important biochemical reactions, including protein synthesis (D. N. Wilson & Cate, 2012; Schmeing & Ramakrishnan, 2009) and pre-mRNA splicing (Hoskins & Moore, 2012; Valadkhan, 2010). Since the discovery that RNA molecules could act as enzymes, the study of the novel catalytic properties of RNA has been an area of intense interest and research (Sharp, 2009; Fedor & Williamson, 2005). These efforts have given birth to the field of ribozyme engineering (Link & Breaker, 2009; X. Chen & Ellington, 2009) and influenced theories into of the origin of life itself (T. J. Wilson & Lilley, 2009; X. Chen, Li,

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& Ellington, 2007). Ultimately, the elucidation of the mechanisms of RNA catalysis promise to yield a wealth of new insights that will extend our understanding of biological processes and facilitate the design of new RNA-based technologies including allosterically controlled ribozymes that may act as molecular switches (Fastrez, 2009; Suess & Weigand, 2008) in RNA chips and new ultra-sensitive biosensing devices (Penchovsky, 2014).

A detailed understanding of the general strategies whereby molecules of RNA can catalyze chemical reactions, including the factors that regulate their activity, provides guiding principles to aid in molecular design. A deep understanding of mechanism, however, requires an interdisciplinary approach that integrates both theory and experiment (Kellerman, York, Piccirilli, & Harris, 2014; Rhodes, Réblová, Sponer, & Walter, 2006). Experiments can be designed to probe mechanism, but due to the inherent difficulty of directly observing a transition state, primary experimental observables only indirectly report on mechanism and do not provide an atomic-level picture of catalysis (Fedor, 2009; Al-Hashimi & Walter, 2008; Walter, 2007). Computational approaches, and in particular molecular simulation methods, provide a wealth of molecular-level detail, but are derived from approximate models that, without validation from experiments, are not meaningful (Hashem & Auffinger, 2009; McDowell, Spacková, Sponer, & Walter, 2006). Thus, while experimental structural biology, molecular biology, and molecular biophysics approaches provide critical data about ribozyme mechanisms, the translation of this data into knowledge requires interpretation through theoretical models.

In this paper, we provide a discussion of the multiscale methods used for computational RNA enzymology. These methods have particular relevance to the study of catalytic riboswitches that combine molecular recognition and binding of an effector molecule with conformational changes in the expression platform that lead to catalysis. Each of these elements are sensitive to environmental conditions, including the specific content of the ionic atmosphere as well as pH. Recently, there have been advances in both computational tools as well as experimental methods that have advanced our understanding of RNA catalysis. The goal of this paper is to present an overview of the multiscale modeling tools used in computational enzymology, what they are used for, and how they can be connected with experiments. Ultimately, a goal of these efforts is to develop robust computational models that not only aid in the interpretation of experimental data, but that also provide predictive insight.

The paper is organized as follows. In the first section, an overview of the multiscale modeling approach is given, along with a discussion of why RNA poses particular computational challenges. The second section describes methods for modeling the ionic environment around RNA as a function of ionic conditions. The third section addresses issues of protonation states as a function of pH. The fourth section describes examination of conformational events required to reach a catalytically active structure, and how this structure evolves along the reaction path. The fifth section examines methods to study the catalytic chemical steps of the reaction once a catalytically active state has been achieved. The sixth section will focus on the calculation of kinetic isotope effects to verify the rate-controlling transition state structure. Along the way, we will use examples of the catalytic

mechanism of the hepatitis delta virus ribozyme (HDVr) and RNase A to illustrate key points.

2 The “Problem Space” of Computational RNA Enzymology

The goal of computational RNA enzymology is to provide a detailed atomic-level description of catalysis that is able to unify the interpretations of a wide range of experiments such that a consensus view of mechanism emerges. Ultimately, the elucidation of mechanism requires consideration of specific chemical reaction pathways through a multidimensional free energy landscape that connects reactants to products while departing from a presumed catalytically competent *active state* (T.-S. Lee, Radak, Pabis, & York, 2013; Ensing, De Vivo, Liu, Moore, & Klein, 2006; Vanden-Eijnden, 2009; Wojtas-Niziurski, Meng, Roux, & Bernèche, 2013). However, the mapping of any given pathway is not meaningful unless one also characterizes the free energy associated with formation of the active state itself; *i.e.* the probability of finding the system in the active state as a function of experimentally tunable environmental variables such as pH and ionic conditions. The active state will be a function of the RNA conformation, protonation state of key residues, and metal ion binding modes. Together with the catalytic chemical steps, these dimensions define the scope of the “problem space” (Figure 1) that needs to be explored and characterized.

RNA molecules are highly charged and exhibit a high degree of structural variation that is sensitive to the protonation state of nucleobase residues as well as the binding of metal ions and, in the case of riboswitches, small molecules (Bevilacqua, Brown, Nakano, & Yajima, 2004; Draper, 2008; Roth & Breaker, 2009). Other factors involving greater complexity, such as the binding of proteins and intermolecular interactions that occur in macromolecular assemblies, also influence RNA structure and function, but are beyond the scope of the present discussion.

In the case of ribozymes, protonation state and metal ion binding, in addition to being important to achieve a catalytically active conformation, may also play a role in the chemical steps of the reaction. Divalent metal ions (usually Mg^{2+}) are universally important for folding under physiological conditions (Misra & Draper, 2002; Grilley, Soto, & Draper, 2006) and, in ribozymes, have been implicated in many instances as directly participating in catalysis (Wong & York, 2012; J. Chen et al., 2013). This makes their roles in folding and catalysis difficult to untangle (Misra & Draper, 1998; Gong, Chen, Bevilacqua, Golden, & Carey, 2009; Gong, Chen, Yajima, et al., 2009). Similarly, the structure and energetics of RNA, in particular tertiary interactions, are sensitive to pH (Murray, Dunham, & Scott, 2002; Wadkins, Shih, Perrotta, & Been, 2001; Nixon & Giedroc, 2000), as are the catalytic protonation state requirements of key active site residues in ribozymes (Butcher & Pyle, 2011; Doudna & Cech, 2002). The duality of influence of protonation state and metal ion binding on RNA structure and catalytic activity is further complicated by the fact that they are often coupled. Metal ion binding can perturb the pK_a values of active site residues such that they can be more effective as general acids or bases under physiological conditions, and conversely, ionization events can adjust the occupation of nearby metal binding sites.

In what follows, we outline a multiscale modeling strategy that takes a “divide-and-conquer” approach to deconstructing the problem space for RNA catalysis using different computational methods. We then go on to give examples of the use of these methods in application to RNA backbone cleavage transesterification reactions catalyzed by a protein and an RNA enzyme that employ two different mechanisms.

3 Multiscale Modeling Strategy

Multiscale simulations involve the integration of a hierarchy of models that, used together, can solve problems that span multiple spatial and/or temporal scales (Feig, Karanicolas, & Brooks, III, 2004; Sherwood, Brooks, & Sansom, 2008; Meier-Schellersheim, Fraser, & Klauschen, 2009; York & Lee, 2009; van der Kamp & Mulholland, 2013; Lodola & Mulholland, 2013; Dama et al., 2013). In the context of biocatalysis, this implies consideration of the enzyme, along with its substrate and any required cofactors, acting in a realistic condensed phase environment. The active site, where chemical bond formation or cleavage occurs, generally requires a computationally intensive quantum mechanical description (Garcia-Viloca, Gao, Karplus, & Truhlar, 2004; Xie, Orozco, Truhlar, & Gao, 2009; van der Kamp & Mulholland, 2013; Lodola & Mulholland, 2013; Hou & Cui, 2013) and this problem is amplified by the need for different levels of phase space sampling to capture events that occur on vastly different time scales. Consequently, biocatalysis applications demand the use of multiscale models that can overcome these challenges in a fashion that is both reliable and computationally tractable.

Multiscale modeling simulations of RNA catalysis are laden with challenges that are more pronounced relative to their protein enzyme counterparts (A. A. Chen, Marucho, Baker, & Pappu, 2009; T.-S. Lee, Giambalvo, & York, 2010). The high degree of charge in RNA systems demands careful treatment of electrostatic interactions in the solvated ionic environment, accurate models for ion interactions and long equilibration times. The increased conformational heterogeneity of RNA relative to typical proteins demands special consideration of sampling in order to get converged structural and thermodynamic properties. The methods used to address these challenges will be described within the context of the example applications that apply them.

4 Catalytic Strategies for Cleavage of the RNA Backbone

We will focus on cleavage of the phosphodiester backbone of RNA, a fundamental reaction in biology that is catalyzed by protein and RNA enzymes. Studying protein and RNA enzymes together has been a long standing strategy for better understanding biocatalysis at a fundamental level (Doudna & Lorsch, 2005) since protein catalysts are composed of a diverse set of amino acid side chains while ribozymes only have four similar nucleobase building blocks to work with. Here, we apply a multiscale modeling approach in the context of a prototype protein enzyme, RNase A, and HDVr which belongs to the class of small self-cleaving nucleolytic ribozymes. RNase A and HDVr catalyze the same phosphoryl transfer reaction via general acid/base mechanisms (Lilley, 2011a, 2011b) (Figure 2) and require one or more nucleobase or amino acid residues to be in a non-standard protonation state for catalytic activity (Gong et al., 2007; Wilcox, Ahluwalia, & Bevilacqua, 2011). Enzymes

belonging to the RNase superfamily degrade single stranded RNA specifically and bovine pancreatic RNase A has been a model enzyme system for studying protein structure and catalytic mechanism for decades (Herschlag, 1994). The HDVr is involved in, and essential for, the rolling-circle replication of the human pathogen, the hepatitis D virus (HDV) where its role is to self-cleave the replicated RNAs into unit-length (Ferré-D'Amaré, Zhou, & Doudna, 1998). For RNase A, two histidine residues, His12 and His119, are the proposed general acid and base, respectively (Raines, 1998) while in the case of the HDVr, a Mg^{2+} ion has been directly implicated in catalysis as the general base, with C75 playing the role as the general acid (Nakano, Chadalavada, & Bevilacqua, 2000; Das & Piccirilli, 2005; Gong, Chen, Bevilacqua, et al., 2009).

5 Modeling Ion and Nucleic Acid Interactions

The first dimension in the computational RNA enzymology “problem space” (Figure 1) refers to metal ion interactions with RNA. The structure and function of RNA is strongly influenced by interactions with metal ions in solution. These interactions range from tight, specific site binding of divalent metal ions to diffuse territorial binding of monovalent ions in the ion atmosphere around the RNA. Here we provide a brief overview of the most commonly applied ion models used in biomolecular simulations, and highlight recent developments in the application of integral equation theories and their relation to recent “ion counting” experiments.

5.1 Ion Models used in Biomolecular Simulations

The most commonly used force fields for simulating nucleic acid systems are based on non-polarizable pairwise potential models (Case et al., 2014; Cornell et al., 1995; Wang, Cieplak, & Kollman, 2000; Pérez et al., 2007; Zgarbová et al., 2011; MacKerell, Jr. & Banavali, 2000; Foloppe & MacKerell, Jr., 2000; Oostenbrink, Villa, Mark, & van Gunsteren, 2004; Jorgensen, Maxwell, & Tirado-Rives, 1996; Kaminski, Friesner, Tirado-Rives, & Jorgensen, 2001) which gain tremendous advantage in computational efficiency at the expense of neglecting explicit many-body quantum effects that are known to be important for many problems (Ponder et al., 2010; Anisimov, Lamoureux, Vorobyov, Roux, & MacKerell, Jr., 2005). Ion parameters are typically parametrized to reproduce bulk properties such as solvation free energies, first shell ion-water distances and water exchange barriers. For monatomic ions that lack internal conformational degrees of freedom, the main consideration for obtaining correct bulk properties involves balancing the ion-water and ion-ion interaction parameters.

Early monovalent ion parameters that were not properly balanced were found to form aggregated clusters in simulations of various salts in aqueous solution (Auffinger, Cheatham III, & Vaiana, 2007; A. A. Chen & Pappu, 2007). Joung and Cheatham subsequently derived new monovalent ion parameters that considered multiple experimental properties that included structure, dynamics and solvation, and in addition, salt crystal lattice energies that were sensitive to the cation-anion interactions (Joung & Cheatham III, 2008). This led to a new set of alkali and halide monovalent ion parameters that corrected the “salting out” artifacts of some previous models, but because the ion-ion and ion-water interactions needed to be balanced, it was necessary that separate sets of ion parameters be developed for

specific water models. Nonetheless, these parameter sets provided a necessary advance that allowed simulations of nucleic acids to be more reliably extended to longer time domains.

Progress in the development of divalent metal ion models is more challenging, but has nonetheless been the focus of considerable recent effort (Martínez, Pappalardo, & Marcos, 1999; Babu & Lim, 2006; Li, Roberts, Chakravorty, & Merz, Jr., 2013; Li & Merz, Jr., 2014). Recently, a Mg^{2+} ion model has been developed for biomolecular simulations that correctly reproduces the ion-water coordination and inner sphere water exchange barrier in solution (Allnér, Nilsson, & Villa, 2012), but that does not necessarily accurately predict absolute solvation thermodynamics (Panteva, Giambalvo, & York, n.d.). More recently, Li *et al.* (Li et al., 2013) have developed a series of water model dependent “12-6” models for divalent metal ions that primarily target a single experimental observable. Unlike the monovalent ion parameters, however, the 12-6 divalent metal ion parameters cannot simultaneously reproduce both structural and thermodynamic properties at the same time, owing largely to the neglect of the electronic polarization energy of waters in the first coordination sphere. Follow-up work by the same authors (Li & Merz, Jr., 2014) then introduced “12-6-4” divalent metal ion parameters that make use of a pairwise potential that includes the contribution of the charge-induced dipole interaction in the form of an additional r^{-4} term added to the traditional Lennard Jones potential. These divalent ion models have been shown to simultaneously reproduce multiple different properties (Li & Merz, Jr., 2014; Panteva et al., n.d.).

The result of these efforts clearly illustrates the need to create models for metal ions with properly balanced ion-ion and ion-water interactions in order to accurately model bulk properties. In the case of biomolecular simulations involving RNA, these models need to be extended so that the ion-RNA interactions are similarly balanced. The effort to create new models for metal ion interactions with RNA is still in its infancy, owing largely to the fact that there currently is a paucity of quantitative experimental binding and competition data that is amenable to robust force field parameterization efforts. Nonetheless, there has been some preliminary progress in the modeling of the ion atmosphere around nucleic acids, and our recent contributions to this area are described in the next section.

5.2 Modeling the Ion Atmosphere around Nucleic Acids

The most common approaches to study the distribution of ions around nucleic acids include explicit solvent MD simulations, the three-dimensional reference interaction site model (3D-RISM) (Beglov & Roux, 1997; Kovalenko & Hirata, 2000; Kovalenko, Ten-no, & Hirata, 1999) or through solving the nonlinear Poisson-Boltzmann (NLPB) equation (Kirmizialtin, Silalahi, Elber, & Fenley, 2012; Chu, Bai, Lipfert, Herschlag, & Doniach, 2007; Pabit et al., 2009; Draper, 2008; Bond, Anderson, & Record, Jr., 1994; Bai et al., 2007). Until recently, solving the NLPB equation was the most common way reported in the literature to study the ion atmosphere surrounding nucleic acids, providing solvation thermodynamics as well as three dimensional ion distributions. NLPB calculations are simple and computationally efficient, but are limited in the treatment of water as a uniform dielectric and neglect explicit ion-ion correlation. Thus, there is compelling evidence that conventional NLPB does not accurately model the ion atmosphere around nucleic acids

(Giambra u, Luchko, Herschlag, York, & Case, 2014). Methods that consider explicitly the role of water and the correlations between ions, such as 3D-RISM and molecular dynamics simulations with explicit solvent, have only recently become practical to study such problems (A. A. Chen, Draper, & Pappu, 2009; Luchko et al., 2010; Giambra u et al., 2014; Yoo & Aksimentiev, 2012).

Molecular dynamics simulations, from a theoretical perspective, offer the most rigorous description of solvent structure and dynamics. These simulations, however, are extremely costly, and require consideration of very large system sizes (A. A. Chen, Draper, & Pappu, 2009; Giambra u et al., 2014; Yoo & Aksimentiev, 2012) and long time scales for ion equilibration (Rueda, Cubero, Laughton, & Orozco, 2004; Thomas & Elcock, 2006). Further, solvation thermodynamics is extremely difficult to extract from these calculations. 3D-RISM calculations, on the other hand, integrate out the solvent degrees of freedom and thus allow direct access into solvation thermodynamics, and are sufficiently fast (for fixed solute configurations) that a wide range of ionic conditions can be examined. 3D-RISM calculations can also efficiently explore low salt concentrations (e.g., μM -mM range) where MD suffers from convergence issues that require very long equilibration times and more sophisticated enhanced sampling methods. 3D-RISM calculations are thus potentially very powerful as tools to study the ion atmosphere for nucleic acid systems that can be represented by a relatively small ensemble of rigid conformations. Both MD and 3D-RISM use molecular force fields and, unlike NLPB, yield similar layered solvent and ion distributions (Giambra u et al., 2014; Maruyama, Yoshida, & Hirata, 2010; Yonetani, Maruyama, Hirata, & Kono, 2008; Howard, Lynch, & Pettitt, 2011) (Figure 3). A challenge for both 3D-RISM calculations and MD simulations that has been fully recognized only recently (A. A. Chen, Draper, & Pappu, 2009; Giambra u et al., 2014; Yoo & Aksimentiev, 2012) is the need to consider a sufficiently large amount of solvent such that regions far from the solute exhibit bulk behavior. This is particularly important when comparisons are to be made with experiments that are being performed under different ionic conditions, and thus it is necessary to know what bulk salt concentration the simulations are in equilibrium with.

Recently, several experimental methods have been developed to examine the nature of ion atmosphere around nucleic acids through *ion counting* (IC) experiments that rely on anomalous small-angle X-ray scattering (ASAXS) (Pabit et al., 2010; Pollack, 2011; Andresen et al., 2008, 2004), buffer equilibration atomic absorption spectroscopy (BE-AES) (Bai et al., 2007; Greenfeld & Herschlag, 2009) and titration with fluorescent dyes (Grilley et al., 2006). In previous decades, ^{23}Na or ^{39}Co NMR relaxation rates have also been employed (Bleam, Anderson, & Record, Jr., 1980; Braunlin, Anderson, & Record, Jr., 1987). IC experiments are important as they quantitatively report directly on the contents of the ion atmosphere around nucleic acids, and therefore can be used to facilitate the development of new models. The key observable that allows comparison with experiment is the preferential interaction parameter (Γ) that is, at the microscopic level, an integral measure of the perturbation of the local density of solution components by the highly charged nucleic acid. We have recently reproduced a series of IC measurements using MD simulations, 3D-RISM and NLPB calculations (Giambra u et al., 2014) (Figure 4).

5.3 Current Challenges

The difficulties in modeling ion-nucleic acid interactions molecular mechanically are more pronounced when divalent metal ions are involved. Although experimental ion counting data is available for divalent metal ions, MD simulations are challenging due to the very slow exchange rates of waters and ligands in the first coordination sphere, and generally slower equilibration time scales. It is likely that enhanced sampling methods will have to be developed in order to extend the scope of MD simulations that can be directly compared with IC experiments. 3D-RISM calculations, on the other hand, are made challenging with applications to divalent metal ions due to convergence issues that arise from the non-linear equations that need to be solved. These are also influenced by the specific “closure relation” that is applied, and can lead to quantitatively different predicted preferential interaction parameters (Giambra et al., 2014). Consequently, there are technical challenges that need to be met before MD simulations and 3D-RISM calculations can be widely tested and applied to divalent metal ion interactions with nucleic acids, and new models to emerge.

6 Modeling pH-rate Profiles for Enzymes

The second dimension in the computational RNA enzymology “problem space” (Figure 1) involves examination of protonation states. Within the context of catalysis, the specific protonation states of key residues is a critical requirement of the catalytically active state. For general acid/base catalysis, such as in RNase A and HDVr, the general base must be in the deprotonated form (able to accept a proton) whereas the general acid must be in the protonated form (able to donate a proton) for catalytic activity.

In the analysis of kinetic data as a function of pH, the simplest mechanistic assumption is that the catalytic rate is directly proportional to the probability of the general acid and base being in the active state (Herschlag, 1994). If this assumption is true, and if other protonation events within the pH range of interest are benign with respect to affecting the rate, then general acid/base catalysts will give a classic bell-shaped profile that can be fit to a simple kinetic model where the parameters are the “apparent pK_a ” values of the general acid and base (Bevilacqua, 2003). Agreement between the kinetic “apparent pK_a ” values and macroscopic pK_a values from direct measurements (such as NMR) of the postulated general acid and base, are usually considered as evidence in support of their roles in acid/base catalysis. An underlying assumption in this interpretation, however, is that the protonation states of the general acid and base are not correlated (Klingen, Bombarda, & Ullmann, 2006; Ullmann, 2003), *i.e.*, the pK_a of the general acid is independent of the protonation state of the general base, and vice versa. The validity of this assumption, which is system dependent, can be tested computationally in order to gain a more fundamental understanding of catalytic mechanism for a particular system (Dissanayake, Swails, Harris, Roitberg, & York, n.d.).

Constant pH molecular dynamics (CpHMD) and pH replica exchange molecular dynamics (pH-REMD) have emerged as powerful computational tools for deriving pH-rate profiles for general acid-base catalysts. CpHMD is a method where protonation states are sampled dynamically from a Boltzmann distribution at a fixed pH (Baptista, Martel, & Petersen, 1997; Baptista, Teixeira, & Soares, 2002; M. S. Lee, Salsbury, Jr., & Brooks III, 2004; Mongan, Case, & McCammon, 2004; Khandogin & Brooks III, 2005). We adopt a discrete

protonation state model that employs Metropolis Monte Carlo (MC) exchange attempts between different protonation states throughout the course of the MD simulation, (Baptista et al., 2002; Mongan et al., 2004) which has been recently implemented in the AMBER software suite (Mongan et al., 2004) for proteins. Unlike free energy perturbation and thermodynamic integration calculations, CpHMD intrinsically takes into account the correlated effects of residue protonation states for a fixed value of pH. The use of pH-REMD allows multiple simulations to be performed over a range of discrete pH values, and is used to enhance sampling and ensure that simulations are in equilibrium with one another. The result is that complete atomic-level simulation data, including conditional probabilities for different protonation states (including tautomers) are generated over a range of pH values. From this data, titration and pH-activity curves can be predicted and used to aid in the interpretation of experimental data.

6.1 Application to apo and cCMP-bound RNase A

In this section we apply the CpHMD/pH-REMD method in explicit solvent to RNase A, both in the apo form, and bound to a 2'3'-cyclic phosphate (cCMP) complex. The simulation data is used to predict the macroscopic and microscopic pK_a values for the general acid and base, as well as the shape of the pH-rate profile. These results allows us to examine the validity of assumptions about “apparent pK_a ” values commonly used to interpret experimental pH-rate profiles.

Consider the kinetic model illustrated in Figure 5 used to interpret pH-rate data in which it is assumed that the functional forms of the general base and acid are B^- and AH^+ , respectively, and only the active state $AH^+E_B^-$ goes on to give products with a first-order rate constant k_{cat} . Based on the acid-base equilibrium, there are four different micro-states whose probabilities (fractions) are denoted as $f_{(AH^+/B^-)}$, $f_{(AH^+/BH)}$, $f_{(A/BH)}$ and $f_{(A/B^-)}$. The most common and simplest assumption that can be made is that the protonation states of the general acid and base are uncorrelated and can be modeled by “apparent pK_a ” values for the general acid ($pK_{a,A}$) and base ($pK_{a,B}$); *i.e.*, $pK_{a,A} = pK_{a,A}^{BH} = pK_{a,A}^{B^-}$ and $pK_{a,B} = pK_{a,B}^A = pK_{a,B}^{AH^+}$. The “apparent pK_a ” values are determined through fitting to the active fraction $f_{(AH^+/B^-)}$, and can be compared to the simulated macroscopic pK_a values obtained from the Hill equation. This procedure is analogous to what is typically done experimentally. Alternately, the full microscopic model in Figure 5 can be used to fit all the fractions determined from the simulation data. This allows one to assess the degree to which the assumptions inherent in the “apparent pK_a ” model are valid, and to provide a more detailed and direct interpretation of experimental pH-rate data.

The CpHMD/pH-REMD simulations predict macroscopic pK_a values for His12 and His119 (6.0 and 6.2, respectively) in the apo structure that are quite close to the experimental values (5.8 and 6.2, respectively). The corresponding calculated macroscopic pK_a values for the cCMP complex (8.5 and 7.3, respectively) are in reasonable agreement with experimental data on 3'-CMP (8.0 and 7.4, respectively) (Dissanayake et al., n.d.). Correspondence of these values with the “apparent pK_a ” values derived from pH-activity profiles would suggest a mechanistic role for His12 and His119 as the general acid and base.

Figure 6 plots the predicted pH-activity curves (as fractions, or probabilities, for each micro-state) from the pH-REMD simulations for RNase A in the apo form and complexed with cCMP (Dissanayake et al., n.d.). Plotted are the probabilities of the active fractions (red points are from the simulations, and red lines are fitted with the full microscopic pK_a model illustrated in Figure 5). Also shown are the fractions for the non-active states. It is clear from the figure that the microscopic pK_a model fits the simulated data extremely well.

Table 1 compares parameters derived from the microscopic model to relevant NMR experiments (Quirk & Raines, 1999). Overall, the calculated and experimental results are quite similar. The general acid and base microscopic pK_a values (*i.e.*, small pK_a values; *i.e.*, less than 0.12 for the simulation results) indicate that the protonation states, in these two examples, are not strongly coupled. This supports the idea that the “apparent pK_a ” model may be used. Indeed the “apparent pK_a ” model gives values of 6.0 and 6.3, respectively, for the apo enzyme, and 8.5 and 7.3, respectively, for the cCMP complex (Dissanayake et al., n.d.). These are within 0.05 pK_a units of one another. Applying the CpHMD/pH-REMD method in conjunction with fitting the computed pH-activity data with the microscopic model will be particularly useful when general acid and base residues are oppositely charged and in closer proximity in the active site, as is the case with many ribozyme systems.

6.2 Current Challenges

The ability to accurately compute macroscopic and microscopic pK_a values of residues involved in acid-base catalysis while at the same time treating effects of correlated protonation states using the CpHMD/REMD method will be an invaluable tool to aid in the interpretation of pH-activity data for catalytic RNAs. This has not yet been demonstrated for RNA systems. It has only been very recently (Goh, Knight, & Brooks III, 2012; Goh, Knight, & Brooks, III, 2013) that models for simulating nucleic acids using CpHMD have been extended to nucleic acids, and they have yet to be thoroughly tested. Challenges that will need to be overcome for application to RNA include consideration of nucleobase tautomers, and coupling of protonation state with divalent metal ion binding (such as has been implicated for HDVr). Finally, at this point proton exchange attempts are accepted or rejected based on energies obtained using a Generalized Born (GB) implicit solvation model (Onufriev, Bashford, & Case, 2004), even though the conformational ensembles are generated through MD simulation in explicit solvent. The degree to which this is sufficiently robust for RNA applications has yet to be determined, and may need further development.

7 Modeling Conformational States

The third dimension in the computational RNA enzymology “problem space” (Figure 1) considers the exploration of thermally accessible conformational states. The characterization of relevant states requires exploration of a vast conformational landscape using accurate models and often specialized methods to enhance sampling. The past few decades have witnessed significant maturation of molecular mechanical force fields for nucleic acids based on relatively simple fixed charge models and pairwise potentials for non-bonded interactions (Wang et al., 2000; Pérez et al., 2007; Zgarbová et al., 2011; Brooks et al., 2009). The computational efficiency of these models allows MD simulations to routinely access μ s timescales (Salomon-Ferrer, Götz, Poole, Le Grand, & Walker, 2013; Dror, Dirks,

Grossman, Xu, & Shaw, 2012), making it a viable method for capturing large scale conformational changes in catalytic riboswitches (Giambasu et al., 2010; Giambasu, Lee, Scott, & York, 2012). Taken together, these developments have provided insight into the condensed phase structure and dynamics of ribozymes both in their pre-cleaved ground state and at various points along a reaction path (T.-S. Lee, Giambasu, Harris, & York, 2011; T.-S. Lee et al., 2010; T.-S. Lee, Wong, Giambasu, & York, 2013). Of key importance to the understanding of ribozyme function is to understand what conformational event leads to the catalytically active pre-cleaved ground state, and how does the ribozyme environment respond so as to preferentially stabilize high energy transition states and intermediates as the reaction progresses. Computational mutagenesis provides insights into the origin of experimental mutational effects on the catalytic rate (T.-S. Lee & York, 2008) and may lead to experimentally testable predictions such as chemical modifications that test a specific mechanistic hypothesis or correlated mutations that exhibit a rescue effect (T.-S. Lee & York, 2010). In this way, molecular simulations serve as a tool to aid in the interpretation of experimental functional studies, and may guide the design of new experiments.

7.1 Catalytic Strategies of Ribozymes

Nucleolytic ribozymes employ a broad range of catalytic strategies for RNA backbone cleavage transesterification (Lilley, 2011a; Cochrane & Strobel, 2008). These may include activation of the nucleophile by a general base, promotion of leaving group departure by a general acid, electrostatic stabilization of the transition state by hydrogen bonding or cationic interactions, and facilitation of proton transfer by Lewis acid activation. However, these are merely general mechanistic considerations that are applicable to many different phosphoryl transfer enzymes (Golden, 2011; Ji & Zhang, 2011). The key question that remains at the heart of our understanding of RNA catalysis is how do certain molecules of RNA, with their relatively limited repertoire of reactive functional groups, adopt three-dimensional conformations that convey catalytic activity that rivals many protein enzymes. Insight into some of these questions may be gleaned from molecular simulations. To date, some general guiding principles have begun to emerge. Current molecular simulation evidence suggests that ribozymes are able to engineer electrostatically strained active sites that can cause shifts of the pK_a values of key residues or recruit solvent components, including solvent and in some cases divalent metal ions, to assist in catalysis. In the case of the hairpin ribozyme, electrostatic effects in the active site (Nam, Gao, & York, 2008a) account for a large part of the observed rate acceleration, and cause a shift of the pK_a of an adenine nucleobase which acts as a general acid catalyst to facilitate leaving group departure (Nam, Gao, & York, 2008b). The hammerhead ribozyme, on the other hand, has engineered a highly electronegative active site that can recruit a threshold occupation of cationic charge (T.-S. Lee et al., 2009) (a Mg^{2+} ion under physiological conditions, or multiple monovalent cations under high salt conditions) that facilitates formation of an active in-line attack conformation (T.-S. Lee, Wong, et al., 2013; T.-S. Lee et al., 2008), stabilizes accumulating charge in the transition state and increase the acidity of the 2'OH group of a conserved guanine residue in order to facilitate proton transfer to the leaving group (Wong, Lee, & York, 2011). In both the hairpin and hammerhead ribozymes, as well as other ribozymes such as the *glmS* riboswitch (Klein, Been, & Ferré-D'Amaré, 2007; Viladoms, Scott, & Fedor, 2011) and Varkud satellite ribozyme (T. J. Wilson et al., 2010), a guanine is position

near to the nucleophile, and possibly acts as a general base, but its role is still actively debated. In the case of HDVr, the situation appears to be more complex and controversial (Nakano, Proctor, & Bevilacqua, 2001; Golden, 2011). While the HDVr requires divalent metal ions for catalytic activity under physiological conditions, the role of the metal ion, its catalytically active binding mode, and its correlation with other protonation events in the active site are yet to be resolved (Wadkins et al., 2001; Lévesque, Reymond, & Perreault, 2012; Golden, Hammes-Schiffer, Carey, & Bevilacqua, 2013).

7.2 General Considerations when Starting MD Simulations from Inactive Structures

Structural characterization of ribozymes by X-ray crystallography, NMR and small-angle X-ray scattering have often implicated the involvement of key residues in catalysis based on close proximity to the cleavage site. On departing from these ribozyme structures to run molecular dynamics simulations, however, there are several considerations to take into account. Structures that are not highly resolved, have fractional occupations, or that exhibit a large degree of conformational variation pose difficulties for the computational chemist. Often it becomes necessary to perform many independent MD simulations departing from different starting structures in order to eliminate bias from using a single starting structure.

At the current point in time, the most abundant structural data for ribozymes has been derived from X-ray crystallography (Scott, 2007; Lilley, 2005). This data has been crucial for the field of computational RNA enzymology (Lodola & Mulholland, 2013). Crystal structures must be trapped in a particular state along the reaction path in order to be resolved. Oftentimes, this means deactivating the ribozyme by blocking the nucleophilic O2' group by either methylating it or else removing it completely, or by mutating other residues that are known to be critical for activity at different stages along the reaction coordinate. Invariably, these lead to structures that, with respect to the degree to which they represent an active state, are artificial. Ribozymes can also be trapped in transition state mimic structures, such as vanadate (Davies & Hol, 2004) or 2',5'-phosphodiester linkage (Torelli, Krucinska, & Wedekind, 2007; Klein et al., 2007), at the cleavage site. One must further consider the effect of the crystalline environment as RNA structures can be influenced by crystal packing artifacts that are sensitive to crystallization conditions (Ennifar, Walter, & Dumas, 2003; Auffinger, Bielecki, & Westhof, 2004). In general, one must remember that, although X-ray crystal structures provide invaluable data and critical starting points for molecular simulations, they nonetheless represent static pictures of deactivated enzymes in a crystal environment, whereas meaningful biological interpretation of mechanism requires a dynamical picture of active enzymes in solution. In many cases molecular dynamics crystal simulations are performed in order to aid in the interpretation of crystallographic data, and help to separate the effects of chemical modifications and crystal packing environment on the structure and dynamics of the active enzyme in solution (Martick, Lee, York, & Scott, 2008; Heldenbrand et al., 2014).

7.3 Application to HDVr

In the case of the HDVr, several different experimental results are available which highlight the importance and challenge of computational modeling. First, to date, no pre-cleavage wild-type HDVr crystallographic structure exists that includes a fully resolved active site.

Until recently, the only pre-cleavage HDVr structure available was that of a catalytically inactive C75U mutant, which has a distinctly different active site architecture compared to the wild-type product state (Ferré-D'Amaré et al., 1998; Ke, Zhou, Ding, Cate, & Doudna, 2004). Specifically, in the inactivated mutant ribozyme, U75 is poised to act as the general base while in the post cleavage structure C75 is located in close proximity to the leaving group, suggesting a general acid role (Ferré-D'Amaré et al., 1998). This role is now strongly supported by biochemical studies (Das & Piccirilli, 2005).

Furthermore, in the C75U structures, no resolved divalent ion shows apparently catalytic importance, although biochemical studies support a direct catalytic role for Mg^{2+} . It has also been suggested that the pK_a of C75 in the ribozyme environment is anti-correlated with the presence of Mg^{2+} (Gong et al., 2007) and that C75 protonation is linked to changes in Mg^{2+} inner-sphere coordination and binding mode (Gong, Chen, Bevilacqua, et al., 2009; Gong et al., 2008). More recently, a wild-type pre-cleavage HDVr structure (via deoxy mutation of U-1) has been resolved to 1.9 Å. This structure includes a resolved Mg^{2+} ion with water-mediated contacts to a previously unobserved G-U reverse wobble pair in the active site. Unfortunately, much of the scissile phosphate (and all of the upstream U-1 nucleotide) in this structure is disordered and could not be resolved; instead it was modeled using analogy to the active site of the HHR (J.-H. Chen et al., 2010). In this modeled active site structure, U-1 is directly coordinated to Mg^{2+} via both the O2' nucleophile and a non-bridging oxygen. This structural data, along with recent kinetic studies of G-U reverse wobble mutants (J. Chen et al., 2013; Lévesque et al., 2012), suggest that a Mg^{2+} ion may be responsible for activating the nucleophile.

We have previously performed a series of MD simulations of HDVr along the reaction path by using the pre-cleaved C75U mutant structure as a starting point (T.-S. Lee et al., 2011). U75 was modeled as C75 and simulations of the reactant state, precursor state (nucleophile deprotonated), early transition state, late transition state and product state were conducted for 350 ns each. Representative snapshots from the simulations can be found in Figure 7.

In the inactive mutant structure, a Mg^{2+} ion was directly coordinating U75:O4' while in our simulations a Mg^{2+} starting in this position would not remain stably bound. Instead, the Mg^{2+} was restrained to be within 2 Å of G1:N7 as suggested by Chen *et al.* (J.-H. Chen, Gong, Bevilacqua, Carey, & Golden, 2009) and along the reaction path the coordination of this ion in the active site changed. After about 100 ns, the active site of our starting structure for the product state simulation began to converge to the product state crystal structure. This illustrates the importance of running extensive MD simulations to correct for local and/or global conformational changes due to inactive or inaccurate experimental starting structures. Within the context of computational RNA enzymology, one of the main objectives of these MD simulations is to identify a set of plausible catalytically active structure, along with the conformational events that lead to their formation, in order to proceed to the final stage of investigation: to explore the chemical steps of the reaction by testing specific mechanistic hypotheses using quantum mechanical simulations. This topic will be discussed in the following section.

7.4 Current Challenges

Although MD simulation is an increasingly powerful computational tool to study ribozyme mechanism, several limitations exist. The timescales accessible to MD simulations (now on the order of μ s) still restricts the types of motions that can be investigated computationally (Zwier & Chong, 2010; Dror et al., 2012). Comprehensive nucleic acid force fields, especially for divalent metal ions, are still being tested and developed and are not as robust as their protein counterparts (Pérez, Luque, & Orozco, 2011). Finally, as mentioned earlier, exploration of the “problem space” of RNA catalysis is complicated by the fact that metal ion interactions, protonation states and conformational events are intimately coupled, and more progress needs to be made in the development of methods that can efficiently and reliably model this coupling.

8 Modeling the Chemical Steps of Catalysis

Thus far, we have discussed the use of computational methods to explore the three dimensions of the computational RNA enzymology “problem space” (Figure 1) in order to arrive at an active state that is competent to proceed on to the catalytic chemical steps of the reaction. It may be the case that more than one plausible active state is identified, and each may have a different probability of being realized under different pH and ionic conditions. To complete the mechanistic picture, it remains to characterize the free energy landscape corresponding to the chemical steps of the reaction. The individual pathways through this landscape correspond to specific mechanisms, and elucidation of the free energy barriers for each pathway allows prediction of those paths that are most probable. In order to predict reaction kinetics, it is necessary to know the probability of observing the catalytically active state (or more specifically, the pre-catalytic “reactant” ground state), the pathway and free energy barrier(s) that connect the reactant state with the product state, as well as other factors (Garcia-Viloca et al., 2004) such as barrier re-crossings, quantum tunneling contributions, etc. In the remainder of this section, we discuss in detail the issue of computing the free energy landscapes and identifying mechanistic pathways for the chemical reaction. This sets the stage for the last section, which is to validate the rate-controlling transition state of a predicted pathway by analyzing kinetic isotope effects.

Exploration of the free energy landscape for the chemical steps of catalysis where bond formation and cleavage are occurring requires a quantum mechanical model to describe the changes in electronic structure and energetics. Most enzyme systems are far too large to treat with a fully quantum mechanical method, although recently advances in so-called linear-scaling quantum force fields may alter that paradigm (Giese, Chen, Huang, & York, 2014; Giese, Huang, Chen, & York, 2014). An attractive alternative that has been widely applied is to use so-called combined quantum mechanical/molecular mechanical (QM/MM) models (QMMM, enzyme reactions, electrostatic and steric stabilization, 1976; QMMM, molecular dynamics, 1990). These models typically treat a relatively small, localized region of the system, such as the key residues in the enzyme active site, with a QM model, whereas the vast remainder of the system is treated with a classical MM force field. QM/MM methods have been widely applied to simulations of enzyme reactions (Garcia-Viloca et al., 2004; Senn & Thiel, 2009; van der Kamp & Mulholland, 2013; QM/MM, enzymes, review, 2010).

8.1 General Considerations

In QM/MM methods, the first important factor to be considered is the choice of the QM and MM models. The QM method must be accurate to model the reactive chemistry of interest, while also being sufficiently fast to be applied with the required amount of sampling that the application demands. The MM method should be able to reliably model the electrostatic environment surrounding the QM region as well as the relevant conformational events that occur. With a choice of QM and MM models, it then becomes necessary that the QM/MM interaction parameters, and in particular the non-bonded Lennard-Jones potentials, are appropriately balanced so as to give correct energetics. Other specialized terms are required when the boundary between the QM and MM systems occurs across a chemical bond, and have been described in detail elsewhere (Gao, Amara, Alhambra, & Field, 1998; Y. Zhang, Lee, & Yang, 1999; Reuter, Dejaegere, Maigret, & Karplus, 2000).

Here we will use a fast, approximate semiempirical quantum model that has been especially designed to accurately model phosphoryl transfer reactions such as those considered in the present work (Nam, Cui, Gao, & York, 2007). This model has been applied previously to examine cleavage transesterification in the hairpin (Nam et al., 2008a, 2008b) and hammerhead (Wong et al., 2011) ribozymes.

Reliable determination of free energy landscapes for enzyme reactions requires sufficient sampling of the generalized coordinates used to define the landscape, in addition to the degrees of freedom orthogonal to the reaction coordinates. A wide range of sampling methods have been developed to overcome these challenges (Zuckerman, 2011). Some of the most widespread include multistage/stratified sampling (Valleau & Card, 1972), statically (Torrie & Valleau, 1974; Torrie & Valleau, 1977; Hamelberg, Mongan, & McCammon, 2004) and adaptively (Darve, Rodríguez-Gómez, & Pohorille, 2008; Laio & Parrinello, 2002; Babin, Roland, & Sagui, 2008) biased sampling, self-guided dynamics (Wu & Brooks, 2012), constrained dynamics (den Otter, 2000; Darve & Pohorille, 2001), as well as multicanonical (Berg & Neuhaus, 1992; Nakajima, Nakamura, & Kidera, 1997) and replica exchange (Sugita, Kitao, & Okamoto, 2000; Chodera & Shirts, 2011) algorithms.

Free energy analysis methods need to be incorporated with all simulation data to construct the free energy profile of the reaction coordinates. The weighted histogram analysis method (WHAM) (Kumar, Bouzida, Swendsen, Kollman, & Rosenberg, 1992; Souaille & Roux, 2001) is widely used but requires highly overlapped data and the results are often noisy. The multistate Bennett acceptance ratio (MBAR) (Bennett, 1976; Shirts & Chodera, 2008; Tan, Gallicchio, Lapelosa, & Levy, 2012) methods are broadly applicable but can also suffer from statistical error in the estimation of free energy surfaces when there is low sampling coverage. The recently developed vFEP method uses a general maximum likelihood framework to provide robust, analytic estimates to the free energy surface, and offers some advantage over alternative methods (T.-S. Lee, Radak, et al., 2013; T.-S. Lee, Radak, Huang, Wong, & York, 2014).

8.2 Constructing Free Energy Profiles of HDVr

In this section we provide a demonstration application of the calculation of the 2D free energy profile for the general acid step in HDVr catalysis. The goal is to examine the feasibility of a previously proposed mechanistic hypothesis (J.-H. Chen et al., 2010; Golden, 2011) whereby the catalytic precursor state involves a Mg^{2+} ion bound in a bridging position between the scissile phosphate and a phosphate from a neighboring strand. In this position, the divalent ion is able to coordinate the nucleophile and facilitates its activation. The presumed general acid in this mechanism is a protonated cytosine residue (C75).

Figure 8 shows the 2D free energy surfaces, departing from the activated nucleophile, for the reaction in the presence and absence of a bound Mg^{2+} ion, henceforth referred to as simply “ Mg^{2+} ” and “no Mg^{2+} ” simulations. Two reaction coordinates are used to describe the reaction progression: ξ_{ProT}^{GA} is a “general acid proton transfer” coordinate, defined as the difference in distances between the proton and the general acid, and the proton and leaving group; ξ_{PhoT} is a “phosphoryl transfer” progression coordinate defined as the difference in distances between the phosphorus and the leaving group, and the phosphorus and the nucleophile.

Analysis of the 2D free energy profiles in the presence and absence of a Mg^{2+} bound at the active site suggests the minimum free energy pathways are similar, with phosphoryl transfer leading to a late transition state with an almost fully cleaved bond to the leaving group, followed by asynchronous proton transfer from the general acid. Although the mechanistic pathways are similar, the free energy barrier in the absence of Mg^{2+} (10.0 kcal/mol) is approximately 8 kcal/mol lower than that for the model where Mg^{2+} is present (18.0 kcal/mol), and both of the barriers are considerably lower than the experimental catalytic barrier (estimated to be approximately 19.6–19.8 kcal/mol in the presence of Mg^{2+}). The reason for this apparent discrepancy is that one needs to consider the free energy associated with formation of the activated pre-catalytic state with the nucleophile deprotonated, which was the starting state for the QM/MM calculations. This activation is expected to be considerably less in the presence of the Mg^{2+} ion, but it is not yet clear as to whether this is enough to account for the experimental difference. Work to further reconcile these issues are in progress.

Hence the simulation-derived free energy profiles suggest that based on the proposed mechanistic hypothesis (J.-H. Chen et al., 2010; Golden, 2011), these two cases should have similar mechanisms but the reaction barriers departing from the activated nucleophile are different due to the presence of the proposed active site Mg^{2+} . The QM/MM work presented here is therefore not yet conclusive, and ongoing work is needed to characterize the free energy associated with Mg^{2+} ion binding, and determine the resulting pK_a shift on the nucleophile. In addition, alternative competing mechanistic hypotheses that are consistent with experiments should also be explored. Finally, as will be discussed in the next section, once plausible pathways have been determined and the rate-controlling transition state identified, further validation of the pathway can be sought through the measurement and calculation of kinetic isotope effects.

8.3 Current Challenges

Computationally tractable methods are needed that allow accurate determination of free energy surfaces using high-level density-functional methods. Currently, the QM/MM studies that have used density-functional methods for ribozymes have done so with small basis sets (which are notoriously problematic for anionic systems) and either neglected to do any simulation or else employed very short time scales. A promising research direction involves developing methods that allow free energy surfaces generated from exhaustive sampling with low level methods to be systematically corrected to higher levels with significantly reduced sampling requirements. Further, the current models treat the QM/MM interactions as decoupled from the electron density; e.g., they are independent of the local charge. This can lead to over-stabilization of anions which are larger, and hence less solvated. Finally, the ability to calculate free energy profiles from linear-scaling quantum force fields is forthcoming, and promises to advance the field.

9 Computing Kinetic Isotope Effects to Verify Transition State Structure

Kinetic isotope effects (KIEs) are powerful experimental probes that report directly on properties of the rate controlling transition state (Hengge, 2002; Cleland & Hengge, 2006). In these experiments, the isotopic mass of one or more atoms involved in the reaction are selectively altered, typically to a heavier isotope. Experiments are then devised to accurately measure the ratio of rate constants corresponding to reactions of the light and heavy isotope ($KIE = k_{light}/k_{heavy}$). KIE values that are greater than unity are referred to as “normal”, whereas values less than unity are referred to as “inverse”. Most importantly, KIEs are very sensitive to changes in transition state bonding environment, and ultimately encode information about the transition state that allows validation of predicted pathways that pass through it, which in turn provides insight into enzyme mechanism (Harris & Cassano, 2008; Lassila, Zalatan, & Herschlag, 2011). Nonetheless, a detailed interpretation of KIE data in terms of structure and bonding in the transition state requires the use of computational quantum mechanical models (Wong et al., 2012; H. Chen et al., 2014).

9.1 Application of KIE on RNase A and Zn^{2+} Catalytic Mechanisms

We have recently investigated the mechanistic details of RNase A using a joint experimental and theoretical approach through the determination of experimental KIEs and their interpretation using computational models (Gu et al., 2013). These results are placed into context of baseline non-enzymatic reaction models (Wong et al., 2012), and models where catalysis is affected by Zn^{2+} ions in solution (H. Chen, Harris, & York, n.d.). KIE values for the nucleophile O2', non-bridging phosphoryl oxygens, and leaving group O5', designated $^{18}k_{NUC}$, $^{18}k_{NP\ O}$ and $^{18}k_{LG}$, respectively, were calculated with density-functional QM models (H. Chen et al., n.d.) as well as measured. The results are summarized in Figure 9.

The non-enzymatic model has a $^{18}k_{NUC}$ value near unity and a very large $^{18}k_{LG}$ value. The models indicate the transition state is very late (cleavage to the leaving group is almost complete). The reaction catalyzed by RNase A shows a $^{18}k_{NUC}$ value that is trending toward being slightly inverse, and the $^{18}k_{LG}$ value is significantly reduced. Overall, the models

indicate that this corresponds to a late transition state that is overall more compact than the non-enzymatic model reaction. More recently, the KIEs for RNA transphosphorylation catalyzed by Zn^{2+} ions in solution have been measured (S. Zhang et al., n.d.). It is of considerable interest that the experimental KIE values for the Zn^{2+} -catalyzed reaction are similar to those measured for the reaction catalyzed by RNase A. Further, the computational models for both these reactions that give the closest agreement with experiment are strikingly similar. The Zn^{2+} ion positions mimic closely those of the protonated histidine residues for RNase A. A slight difference is that, for the Zn^{2+} -catalyzed reaction, there is an additional hydrogen bond to the nucleophile donated from a Zn^{2+} -coordinated water molecule. This manifests itself in making the $^{18}k_{\text{NUC}}$ value slightly more inverse. Overall, these results suggest that the transition states for the catalyzed reactions are altered from that of the non-enzymatic model in a similar fashion by the RNase A enzyme environment or by Zn^{2+} ions in solution. Further, the agreement between the experimental and calculated KIE results provides support that the predicted mechanistic pathway for RNase A passes through a late transition state where the interactions illustrated in Figure 9 are preserved.

9.2 Current Challenges

At the moment, the calculation of KIEs for large enzyme or ribozyme systems is very tedious and time consuming. The development of computationally more efficient electronic structure methods that were made to be linear-scaling and seamlessly integrated into a multiscale modeling framework for the calculation of KIEs would be extremely valuable.

10 Conclusions

In this chapter, we have applied a multiscale modeling strategy to the computational RNA enzymology “problem space” that, for the purposes here, consists of four major modeling components: metal ion-nucleic acid interactions, pH-rate profiles, catalytically active conformations and the catalytic chemical steps in the reaction. Each of these components has a direct connection with experiment, and can be integrated to form a detailed, atomic-level picture of ribozyme mechanism. The ultimate goal of computational RNA enzymology is to provide a unified interpretation of a wide range of experiments that leads to a consensus view of mechanism. Toward this end, a variety of computational methods have been brought to bear on different elements of the problem space.

Classical MD simulations have proven to be instrumental to probe structure and dynamics of ribozymes along their reaction path, as well as providing the most rigorous (although less practical) description of the solvated ionic atmosphere around nucleic acids. Other molecular solvation theory models, such as 3D-RISM, appear very promising as a practical tool to investigate a wide range of ionic conditions for a sufficiently small ensemble of structures. Molecular simulations under conditions of constant pH, together with pH-REMD, can be used to predict and interpret pH-rate profiles for general acid/base catalysts, and account for coupling between protonation states that are difficult to probe experimentally. Departing from a presumed active state, QM/MM simulations can be used with enhanced sampling methods such as Hamiltonian replica exchange methods to determine multidimensional free energy landscapes for catalysis. Minimum free energy pathways through these surfaces provide predictions of the specific mechanisms. Predicted

mechanisms can be further tested by calculation of kinetic isotope effects for the rate controlling transition state along a given path, which can then be verified experimentally. Overall, this field is still rapidly maturing, and much progress is to be expected over the next decade in the development of integrated methods that will allow even closer connections between theory and experiment to be made, and models that provide a predictive understanding of ribozyme mechanism.

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Figure 1.

Complexity of the ribozyme (R) "problem space" involving metal ion interactions/metal binding (M), protonation state (p), and conformational state (ζ) coordinates that lead to a catalytically "active state" (green). Other variables that represent binding of small molecules and interaction with proteins or other macromolecules are not illustrated. Substrate binding is also not shown, as the primary application focus here is on small self-cleaving RNA enzymes.

Figure 2.

Reaction schematic of RNA 2'-*O*-transesterification. The O_{2'} nucleophile is activated via loss of a proton to a general base and undergoes inline attack on phosphorous to form a pentacoordinate transition structure, followed by departure of the O_{5'} leaving group which is facilitated by proton donation from a general acid.

Figure 3.

Comparison of ion distributions around a 24-mer of duplex B-DNA from MD simulation, 3D-RISM and conventional NLPB. Distributions are shown along a rotating “untwisted” coordinate frame along the DNA axis as described in Giambra et al., 2014. Shown are the untwisted Na⁺ densities from MD, 3D-RISM and NLPB for 0.17 M bulk NaCl concentration. MD and 3D-RISM predict a layered Na⁺ structure, whereas NLPB is unstructured and not even qualitatively similar.

Figure 4. Ion counting profiles for Na^+ from MD, 3D-RISM, NLPB and data from Bai et al., 2007.

Figure 5.

The microscopic model used in interpretation of pH-rate data. The protonation equilibria between pairwise protonation states are defined in the thermodynamic cycle. The active fraction $f_{(\text{AH}^+/\text{B}^-)}$, leads to the products.

Figure 6.

The pH-activity curves for top: apo-RNase A and bottom: cCMP-bound RNase A. The titratable residues are His12 and His119. The four curves represent the fractions (probabilities) for each of the four possible protonation states, with the red curve being the fraction of the catalytically active micro-state, $f_{(AH^+/B^-)}$.

Figure 7.

Representative snapshots taken from simulations of HDVr along the reaction path starting from an inactive C75U mutant crystal structure and compared with the crystal structure of the product state (PDB ID: 1CX0).

Figure 8.

2D free energy surfaces for the general acid step of HDVr catalysis departing from a state where the nucleophile has been activated in a prior step. Shown are simulations in the absence (top) and in the presence (bottom) of a Mg^{2+} bound in the active site. Minima and saddle points (diamonds) and the minimum free energy path (white points) are also indicated.

Figure 9.

(a) Snapshot of RNase A transition state mimic structure from MD simulation and (b) transition state geometries and KIEs of non-enzymatic (left), RNase A catalyzed (middle) and Zn²⁺ catalyzed (right) RNA transphosphorylation model reactions obtained from QM calculations.

Table 1
Experimental and calculated microscopic pK_a s for apo and cCMP-bound RNase A

	$pK_{a,B}^{AH+}$	$pK_{a,B}^A$	$pK_{a,B}$	$pK_{a,A}^{BH}$	$pK_{a,A}^{B-}$	$pK_{a,A}$
apo-RNase A						
Expt. ^a	5.87	6.18	0.31	6.03	6.34	0.31
Microscopic model	5.94	6.06	0.12	6.15	6.26	0.12
cCMP-RNase A						
Expt. (3'-UMP) ^a	7.95	7.85	0.1	6.45	6.35	0.1
Microscopic model	7.30	7.24	0.06	8.50	8.44	0.06

The calculated microscopic pK_a values are derived from the thermodynamic cycle illustrated in Figure 5. The pK_a values are the differences in the microscopic pK_a values, and indicate coupling between protonation states (zero pK_a values indicate no coupling, as in the “apparent pK_a ” model).