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Strategies for Improved 3D Small-Tip Fast Recovery (STFR) Imaging

Hao Sun^{*,1}, Jeffrey A. Fessler^{1,2}, Douglas C. Noll², and Jon-Fredrik Nielsen²

¹Departments of Electrical Engineering and Computer Science, University of Michigan, Ann Arbor, MI, USA

²Departments of Biomedical Engineering, University of Michigan, Ann Arbor, MI, USA

Abstract

Purpose—Small-tip fast recovery (STFR) imaging is a recently proposed steady-state sequence that has similar image contrast as balanced steady-state free precession (bSSFP) but has the potential to simultaneously remove banding artifacts and transient fluctuation. STFR relies on a “tip-up” radiofrequency (RF) pulse tailored to the accumulated phase during the free precession (data acquisition) interval, designed to bring spins back to the longitudinal axis, thereby preserving transverse magnetization as longitudinal magnetization for the next TR. We recently proposed an RF-spoiled STFR sequence suitable for thin slab imaging, however in many applications, e.g., functional MRI or isotropic-resolution structural imaging, 3D steady-state imaging is desirable. Unfortunately, 3D STFR imaging is challenging due to the need for 3D tailored RF pulses. Here we propose new strategies for improved 3D STFR imaging, based on (i) unspoiled imaging, and (ii) joint design of non-slice-selective tip-down/tip-up RF pulses.

Theory and Methods—We derive an analytic signal model for the proposed unspoiled STFR sequence, and propose two strategies for designing the 3D tailored tip-down/tip-up RF pulses. We validate the analytic results using phantom and in-vivo imaging experiments.

Results—Our analytic model and imaging experiments demonstrate that the proposed unspoiled STFR sequence is less sensitive to tip-up excitation error compared to the corresponding spoiled sequence, and may therefore be an attractive candidate for 3D imaging. The proposed “joint” RF pulse design method, in which we formulate the tip-down/tip-up RF pulse design task as a magnitude least squares problem, produces modest improvement over a simpler “separate” design approach. Using the proposed unspoiled sequence and joint RF pulse design, we demonstrate proof-of-principle 3D STFR brain images with bSSFP-like signal properties but with reduced banding.

Conclusion—Using the proposed unspoiled sequence and joint RF pulse design, STFR brain images in a 3D region of interest (ROI) with bSSFP-like signal properties but with reduced banding can be obtained.

*Correspondence to: Hao Sun, 1073 B.I.R.B., 2360 Bonisteel Ave, Ann Arbor, MI 48109 - 2108, Phone: 734-358-8135, sunhao@umich.edu.

Keywords

steady-state MRI; pulse design; bSSFP; banding artifact; small-tip fast recovery; STFR

Introduction

Balanced steady-state free precession (bSSFP) is a rapid imaging sequence that has high signal-to noise ratio (SNR) and useful tissue contrast, but suffers from off-resonance banding artifacts and transient fluctuations [1]. Numerous methods have been proposed in the past decade for correcting these artifacts, including multi-TR sequences that seek to widen the separation between bands [2–5], and multiple phase-cycled acquisitions that are combined to produce uniform signal independent of off-resonance. However, all of these methods sacrifice signal strength and/or imaging time, and are not universally applicable to all bSSFP applications.

Recently, our group proposed a new steady state imaging sequence called small-tip fast recovery (STFR) [6], which is a potential alternative to bSSFP. There are two key ideas in STFR: First, after excitation and readout, a tip-up radio-frequency (RF) pulse tailored to the accumulated phase during free precession is transmitted to bring spins back to the longitudinal-axis, which “fast recovers” the transverse magnetization and preserves it as longitudinal magnetization for the next TR [6,7]. Second, after the tip-up pulse, it is necessary to play an unbalanced gradient to dephase residual transverse spins. With accurate tailored pulses, STFR imaging may have many of the benefits of bSSFP such as high SNR efficiency, good flow properties, and combined T2/T1 weighting [1], but does not suffer from banding artifacts. STFR therefore has the potential to provide an alternative to bSSFP for some applications, and may obviate the need for special artifact-reduction techniques such as phase-cycled imaging [8] or multiple-TR sequences [2–5].

However, STFR is challenging to implement in practice, due to the need for accurate tailored tip-up pulses. This is particularly true in 3D imaging, since the required 3D tailored pulses can be prohibitively long. Here we propose new strategies for improved 3D STFR imaging, based on (i) unspoiled imaging, and (ii) joint design of non-slice-selective tip-down/tip-up 3D tailored RF pulses.

We begin this article by deriving an analytic signal equation for the proposed unspoiled STFR sequence, which is then used to compare the properties of unspoiled and spoiled STFR. We then describe the proposed joint RF pulse design algorithm that treats the tip-down and tip-up pulses as one combined RF pulse, which is in turn designed using magnitude least-squares optimization. Next we describe our experimental methods and results (phantom and in-vivo), demonstrating that the proposed unspoiled STFR sequence is less sensitive to tip-up excitation error compared to the spoiled sequence in [6] and hence is a promising candidate for 3D imaging. We conclude with a discussion of limitations and future extensions of this work.

Theory

Unspoiled STFR

The proposed unspoiled STFR sequence and associated spin path are illustrated in Fig. 1(a). The spin is first tipped down by a small tip angle pulse with flip angle $\alpha(\mathbf{r})$. This tip-down pulse can be spatially tailored, i.e., the flip angle (magnitude and phase) may vary with the spatial coordinate $\mathbf{r}$. During the signal readout interval T_{free} , the spin precesses by an angle $\theta_f(\mathbf{r}) = \omega(\mathbf{r})T_{\text{free}}$, where $\omega(\mathbf{r})$ is the off-resonance frequency (B0 inhomogeneity) at position $\mathbf{r}$. A “tip-up”, or “fast recovery”, RF pulse with flip angle $\beta(\mathbf{r})$ tailored to the accumulated phase $\theta_f(\mathbf{r})$ is then transmitted to bring the magnetization vector back toward the longitudinal axis. The purpose of the tip-up pulse is to preserve as much longitudinal magnetization as possible prior to the next sequence repetition interval (TR) and hence to maximize SNR efficiency, and to introduce T2 weighting. Immediately after the tip-up pulse, an unbalanced gradient g is played out, designed to dephase the residual transverse magnetization left over after the tip-up pulse. This gradient causes a rotation θ_g of each spin isochromat, with θ_g varying along the direction of g . We will see below that this unbalanced gradient is necessary for banding-free imaging. Note that the RF phase offset from TR-to-TR is held constant, i.e., we do not use RF-spoiling (quadratic phase cycling, as was done in [6]) in the sequence proposed here.

Steady-state magnetization for a spin isochromat

To obtain a signal equation for unspoiled STFR, we first develop an expression for the steady state magnetization $\mathbf{M}_1(\theta_g)$ for a spin isochromat immediately after the tip-down pulse (see Fig. 1(a)), and then integrate the resulting expression over all isochromats within a voxel, i.e., we integrate over $\theta_g = [0, 2\pi]$. For clarity, we drop the explicit dependence on spatial position $\mathbf{r}$ in the following.

Without loss of generality, our derivation assumes the tip-down pulse to be aligned with the x-axis (zero phase). We ignore the RF pulse duration (which can vary depending on, e.g., excitation k-space trajectory), which is a common assumption when deriving analytic models for steady state sequences, especially for RF pulses that are short compared to TR [9]. We obtain the steady-state magnetization by modeling each step of the spin path using the Bloch equation in matrix form. Details of the derivation are provided in the Appendix. We obtain the following expression for the steady-state transverse magnetization of a spin isochromat:

$$M_{1,t} = M_0 \frac{a \cos(\theta_g + \phi) + b \sin(\theta_g + \phi) + c}{d \cos(\theta_g + \phi) + e \sin(\theta_g + \phi) + f} \quad (1)$$

where $M_{1,t}$ is the transverse component of $\mathbf{M}_1$, M_0 is the equilibrium magnetization and the factors a through f are defined as:

$$\begin{aligned}
a &= -iE_{g2}(E_{f2}(-1+E_{g1}+(-1+E_{f1})E_{g1}\cos\beta)\cos(\theta_f-\phi)\sin\alpha+(E_{f1}(-1+E_{g1})+(-1+E_{f1})\cos\alpha)\sin\beta+iE_{f2}(-1+E_{g1}+(-1+E_{f1})E_{g1}\cos\beta)\cos(\theta_f-\phi)\sin\alpha \\
b &= E_{g2}(E_{f2}((-1+E_{f1})E_{g1}+(-1+E_{g1})\cos\beta)\cos(\theta_f-\phi)\sin\alpha-(-1+E_{f1}+E_{f1}(-1+E_{g1})\cos\alpha)\sin\beta+iE_{f2}((-1+E_{f1})E_{g1}+(-1+E_{f1})E_{g1}\cos\beta)\cos(\theta_f-\phi)\sin\alpha \\
c &= i((-1+E_{g1}+(-1+E_{f1})E_{g1}\cos\beta)\sin\alpha+E_{f2}E_{g2}^2(E_{f1}(-1+E_{g1})+(-1+E_{f1})\cos\alpha)\sin\beta(\cos(\theta_f-\phi)+i\sin(\theta_f-\phi))) \\
d &= E_{g2}(-E_{f2}(-1+E_{f1}E_{g1})(1+\cos\alpha\cos\beta)\cos(\theta_f-\phi)+(E_{f1}-E_{f2}^2E_{g1})\sin\alpha\sin\beta) \\
e &= E_{f2}(-1+E_{f1}E_{g1})E_{g2}(\cos\alpha+\cos\beta)\sin(\theta_f-\phi) \\
f &= -1+E_{f1}E_{f2}^2E_{g1}E_{g2}^2+(E_{f1}E_{g1}-E_{f2}^2E_{g2}^2)\cos\alpha\cos\beta+E_{f2}(E_{g1}-E_{f1}E_{g2}^2)\cos(\theta_f-\phi)\sin\alpha\sin\beta
\end{aligned}$$

In the above expression, the T1 and T2 relaxation exponentials during the free precession and gradient dephasing intervals are denoted as $E_{f1} = e^{-T_{\text{free}}/T_1}$, $E_{f2} = e^{-T_{\text{free}}/T_2}$, $E_{g1} = e^{-T_g/T_1}$ and $E_{g2} = e^{-T_g/T_2}$.

Although Eq. (1) is only an intermediate expression needed to obtain the total voxel signal, it is instructive to examine its dependence on θ_g when the tip-up pulse is perfectly matched to the spin precession angle, i.e., $\varphi = \theta_f$ and $\beta = \alpha$. Then the θ_f terms in the coefficients a through f are canceled by φ , and these coefficients therefore become independent of the local off-resonance. $M_{1,t}$ then depends on off-resonance only through $\cos(\varphi + \theta_g)$ and $\sin(\varphi + \theta_g)$. Figure 2 plots Eq. (1) under these conditions, for $T_1/T_2 = 510/50$ ms and $\alpha = \beta = 16^\circ$. The most striking feature of Fig. 2 is the presence of narrow minima spaced 2π apart, which explains why fully balanced ($g = 0$ and thus $\theta_g = 0$) STFR imaging would be problematic, since narrow bands would be present in regions of the image where φ (and θ_f) equals an integer multiple of 2π . The minima in Fig. 2 are reminiscent of dark signal bands in bSSFP, except for one crucial difference: the neighboring “bands” in Fig. 2 are in-phase. We therefore expect the total voxel signal for unbalanced STFR, obtained by integrating over one full cycle (shaded region) in Fig. 2, to be high and contain no such banding artifacts.

Signal equation

To obtain the steady-state signal M_t from a voxel, we integrate $M_{1,t}(\theta_g)$ over the full distribution of spins:

$$\begin{aligned}
M_t(\phi, \theta_f, \alpha, \beta, T_1, T_2, T_{\text{free}}, T_g) &= \frac{1}{2\pi} \int_0^{2\pi} M_{1,t}(\phi + \theta_g) d\theta_g \\
&= M_0 \frac{1}{2\pi} \int_0^{2\pi} \frac{a\cos(\theta_g + \phi) + b\sin(\theta_g + \phi) + c}{d\cos(\theta_g + \phi) + e\sin(\theta_g + \phi) + f} d\theta_g \\
&= M_0 \left(\frac{c}{\sqrt{f^2 - d^2 - e^2}} - \frac{ad + be}{d^2 + e^2} \frac{f - \sqrt{f^2 - d^2 - e^2}}{\sqrt{f^2 - d^2 - e^2}} \right) \quad (2)
\end{aligned}$$

Here we denote the dependence on the various tissue and sequence parameters on the left-hand side only. Equation (2) describes the signal from a voxel immediately after the tip-down pulse, and must be multiplied by $e^{-TE/T_2 - jTE}$ to obtain the signal at the echo time (TE). Equation (2) is valuable in several respects: First, it provides a fast way to analyze the sequence properties and optimize the imaging parameters. Second, it shows that the STFR

signal is independent of off-resonance if we have a perfectly tailored pulse (off-resonance induced phase θ_f is canceled out by φ in coefficients a through f). Finally, this expression can be used to describe the extended Chimera sequence [10] that is similar to our unspoiled STFR except conventional RF pulses are used instead of tailored pulses.

Figure 3(a) plots Eq. (2) over a range of flip angles, for three different tissue types. Here we assume that the tip-up pulse is ideal, i.e., $\varphi = \theta_f$ and $\beta = \alpha$. For comparison, the calculated signals for bSSFP and spoiled STFR are also shown, using analytic results from [11] and [6], respectively. Notice we use twice the flip angle of STFR sequences in the calculation of bSSFP signals. Figure 3(b) plots the corresponding white/gray matter contrast. We see that unspoiled STFR produces similar tissue signal and contrast as bSSFP, as desired.

Figure 4(a) plots Eq. (2) as a function of the phase mismatch $\varphi - \theta_f$ between the tip-up phase φ and the spin phase θ_f . Such a phase mismatch is unavoidable in practice, since the tip-up pulse will never be perfectly accurate everywhere within the imaging region of interest (ROI). For comparison, the corresponding plot for spoiled STFR is also shown. In addition, experimentally observed signal curves are plotted, obtained by applying a linear gradient shim and imaging with sinc (i.e., untailored) tip-down and tip-up pulses (see Fig. 4(b)). The analytic curve was calculated based on the actual T1, T2 values of the phantom (T1/T2 = 510/50 ms), which were measured using inversion recovery and spin echo sequences, respectively. The signal for both unspoiled and spoiled STFR depends on $\varphi - \theta_f$, but unspoiled STFR decays less rapidly with increasing phase error. In other words, unspoiled STFR is less sensitive to tip-up phase error compared to spoiled STFR. The difference in the rate of signal drop versus phase mismatch varies with tissue relaxation parameters, as shown in Fig. 5. Note that the CSF signal of spoiled STFR drops significantly faster than for other tissues, and faster than the unspoiled STFR CSF signal.

RF pulse design

The key to successful STFR imaging is to design accurate tailored tip-up pulses that bring the magnetization close to the longitudinal axis. Here we consider 3D imaging using unspoiled STFR, and we restrict our designs to non-slice-selective 3D tailored pulses. (Although we could in principle use slice- or slab-selective 3D pulses, such pulses would most likely be prohibitively long.) We propose two different approaches to RF pulse design in STFR: “Separate” and “Joint”.

In our first approach, we design the tip-down and tip-up pulses independently, as follows: First, we tailor the tip-down pulse $\alpha(\mathbf{r})$ to a uniform magnitude excitation pattern with phase $-\theta_f(\mathbf{r})/2$, i.e., half the expected free precession angle. We then design an “intermediate” tip-down pulse $\beta_{\text{int}}(\mathbf{r})$ tailored to the expected spin phase at the end of T_{free} , i.e., $\angle\alpha(\mathbf{r}) + \theta_f(\mathbf{r})$. Finally, we obtain the tip-up pulse $\beta(\mathbf{r})$ by “rewinding” the intermediate pulse $\beta_{\text{int}}(\mathbf{r})$ as in [6], i.e., by time-reversing and negating $\beta_{\text{int}}(\mathbf{r})$. The advantage of this approach is that it is relatively easy to implement, e.g., using existing methods for small-tip RF pulse design.

The second approach to RF pulse design in STFR is based on the observation that the phase of tip-down pulse $\angle\alpha(\mathbf{r})$ does not in general need to be constrained to a particular pattern, as long as it varies reasonably smoothly across the ROI. In fact, the only requirement that

should be imposed on the tip-down pulse is that the magnitude $|\alpha(\mathbf{r})|$ should be as uniform as possible to avoid image shading. Using the small-tip (Fourier) approximation in which the transverse component of the excitation pattern is expressed as a linear transformation of the time-varying RF waveform [12], this requirement can be stated as

$$\sin \alpha = |A_1 \mathbf{b}_1| \quad (3)$$

where $\mathbf{b}_1$ is a discretization of the time-varying tip-down RF waveform $b_1(t)$, and α is the desired (uniform) flip angle. A_1 is a system matrix with elements $a_{ij} = \gamma M_0 e^{-ik(t_j)r_i - i\alpha(r_i)(t_j - T)}$, where $k(t)$ is the excitation k-space trajectory determined by the gradient waveforms for tip-down part and T is the duration of tip-down pulse. Similarly, we require that the magnitude of the magnetization after the tip-up pulse be as small as possible:

$$|A_2 \mathbf{b}_1 + A_3 \mathbf{b}_2| = 0 \quad (4)$$

where A_2 and A_3 are blocks of $\tilde{A} = [A_2 \ A_3]$ with elements $\tilde{a}_{ij} = \gamma M_0 e^{-ik(t_j)r_i - i\alpha(r_i)(t_j - T)}$, where T and $k(t)$ are the duration and excitation k-space trajectory determined by the gradient waveforms for the whole combined pulse, i.e., including tip-down excitation, free precession, and tip-up recovery.

We propose to solve Eqs. (3)-(4) jointly using the following magnitude least-squares formulation:

$$\begin{bmatrix} \hat{\mathbf{b}}_1 \\ \hat{\mathbf{b}}_2 \end{bmatrix} = \underset{\mathbf{b}_1, \mathbf{b}_2}{\operatorname{argmin}} \left\{ \left\| \begin{bmatrix} \sin(\alpha) \\ \mathbf{0} \end{bmatrix} - \begin{bmatrix} A_1 & 0 \\ A_2 & A_3 \end{bmatrix} \begin{bmatrix} \mathbf{b}_1 \\ \mathbf{b}_2 \end{bmatrix} \right\|_2^2 + \mu \|\mathbf{b}_1\|_2^2 + \mu \|\mathbf{b}_2\|_2^2 \right\}, \quad (5)$$

where μ is a Tikhonov regularization parameter that constrains the total RF energy [13]. Although the joint formulation in Eq. (5) is more computationally intensive than the Separate design, it may allow for improved tip-up accuracy for a given RF pulse duration since we are removing the constraints on spin phase.

Methods

We performed imaging experiments on a GE 3T scanner equipped with a quadrature transmit/receive head coil. Table 1 lists the various image acquisitions. The phantom was a GE resolution phantom, and the human subject was a healthy volunteer.

Table 2 lists the sequence timing for STFR and bSSFP. All image acquisitions used $256 \times 256 \times 65$ matrix size, $24 \times 24 \times 24$ cm field of view (FOV), and 62.5 KHz receive bandwidth. We used a FOV along z that was large enough to eliminate aliasing from untargeted slices, which in practice could be avoided by, e.g., aligning the frequency encoding direction with the z direction [14]. The bSSFP acquisitions used twice the flip angle as the STFR acquisitions, since our equation and simulations predict that bSSFP will give the same (on-resonance) signal level with twice the flip angle of the STFR sequence.

For the STFR acquisitions, we tailored the RF pulses to a 3D ROI consisting of a 3 cm axial slab. For this purpose we obtained a B0 map of the ROI using SPGR with echo times 3 ms and 5 ms. For the tailored pulses (both tip-down and tip-up), we used the spiral nonselective excitation k-space trajectory (SPINS) proposed in [14]. For the Separate design, we calculated the B1 waveforms using the small-tip iterative RF pulse design method in [13]. For the Joint design, we obtained the B1 waveforms by performing the magnitude least-square minimization in Eq. (5) using the method in [15]. Both designs were implemented with the MATLAB image reconstruction toolbox (IRT) from University of Michigan (<http://www.eecs.umich.edu/~fessler>). An example of the resulting B1 waveforms and SPINS gradients are shown in Fig. 1(b).

Results

Phantom observations

Figure 6 shows steady-state images of one of the target slices in the resolution phantom acquired with several different sequences, displayed using the same gray scale. For each image, the mean signal and standard deviation within the object are indicated. We observe a characteristic banding artifact in the bSSFP image, which is largely removed in the Joint unspoiled STFR acquisition. However, some non-uniformity remains in the Joint unspoiled STFR image, due to the limited ability to correct for B0 inhomogeneity over the ROI with the short (1.7 ms) RF pulses used here. Furthermore, STFR and (on-resonance) bSSFP have similar signal levels, about twice as high as SSFP-FID and significantly higher than SPGR, in agreement with theory. We also observe that unspoiled STFR produces more uniform images than spoiled STFR, as predicted. Finally, we note that Joint design produces a modest improvement in mean signal level (1.41) compared to Separate design (1.36). Based on this comparison experiment, we think the Joint unspoiled version is more suitable than other STFR sequences for 3D imaging.

In-vivo observations

Figure 7(a) shows steady-state images from the same slice obtained with bSSFP (180° RF phase cycling) and STFR. Similar to Fig. 6, we observe a banding artifact in the bSSFP image (arrow) that is not present in the unspoiled STFR image. Apart from the banding region, unspoiled STFR and bSSFP have similar signal levels and exhibit similar tissue contrast (e.g., bright cerebrospinal fluid (CSF)), as desired. The unspoiled STFR images still have signal loss in some regions due to phase mismatch (see Fig. 7(b)), but it is much more uniform than spoiled STFR, as predicted. We observe significant CSF signal loss in the spoiled STFR image in some regions (see, e.g., oval), which can be explained by comparing the phase mismatch in that region and the phase mismatch sensitivity plot (Fig. 5). The Joint design slightly improves image quality compared to the Separate design, i.e., Joint unspoiled STFR produces a more uniform image with better contrast, and we think this improvement is due to the decrease of phase mismatch using the Joint design. Finally, the high through-plane vessel signal in bSSFP is suppressed in the STFR images (see, e.g., box), which is generally desirable.

Figure 8(a) compares Joint unspoiled STFR and bSSFP in 5 adjacent slices spanning a 4 cm FOV along z (S/I), and highlights the ability of the proposed sequence to image a 3D ROI. The top two rows show bSSFP images obtained with 0° and 180° RF phase cycling, while the bottom row shows the Joint unspoiled STFR images. Both bSSFP acquisitions suffer from banding artifacts. The Joint unspoiled STFR sequence achieves similar signal level and tissue contrast as bSSFP over most of the FOV, although we observe some non-uniformity (image shading) due to large phase mismatch in some region, (see Fig. 8(b)). Note that the observation FOV (4 cm) along z is larger than the target FOV (3 cm) of the tailored pulse; however we can still get reasonably good images in the whole observation FOV because the excitation pattern and free precession accumulated phase pattern are all relatively smooth here.

Discussion

Our theory predicts that STFR has similar SNR as bSSFP (see Fig. 3), which agrees with our measured results (44.2/45.3 dB and 31.6/32.4 dB for bSSFP/STFR in phantom and gray matter ROIs, respectively). Therefore, the SNR efficiency (defined as $\text{SNR} / \sqrt{\text{total scan time}}$) of STFR will be lower than on-resonance bSSFP, since its TR is necessarily longer than the corresponding bSSFP sequence. Compared to multiple phase-cycled bSSFP acquisitions, whether STFR is more SNR efficient or not depends on the actual timing of the specific sequences and the method used to combine the phase-cycled images. In our experiments, we use $\text{TR} = 7.6$ ms and 10 ms for bSSFP and STFR respectively. The TR of bSSFP is not optimized in our experiment and can be as low as 6.8 ms given our scanner control code and the same readout time (4.9 ms) as STFR. Assuming $\text{TR} = 6.8$ ms for bSSFP and $\text{TR} = 10$ ms for STFR, the total scan time of STFR is $1/1.36$ of two phase-cycled bSSFP and $1/2.04$ of three phase-cycled bSSFP. On the other hand, the SNR increases by combining the phase-cycled bSSFP images, and the amount of increase depends on the tissue parameters, noise level and the combination method [8]. For simplicity, if we assume maximum intensity combination, STFR as implemented in our experiments would have similar SNR efficiency as two phase-cycled bSSFP, and better SNR efficiency than three phase-cycled bSSFP. It is therefore possible that in applications where image SNR is critical, bSSFP with two phase-cycles may be preferred over STFR. We note, however, that multiple acquisitions may not be preferred in some applications. For example, in bSSFP fMRI, repeating runs of a paradigm produces confounding effects from cognitive habituation to stimuli and is not ideal [16,17]. Alternating bSSFP that interleaves two phase-cycled bSSFP imaging can potentially solve this problem [18], but it needs catalyzation pulses every time the phase-cycling is changed, which reduces its SNR efficiency.

Here we have shown that STFR and bSSFP image contrast is similar with respect to T1 and T2 sensitivity, however we have performed preliminary work that indicates that these sequences have different sensitivity to diffusion and intra-voxel B0 homogeneity [19]. In bSSFP, because of the relative flat magnitude and phase frequency response curve in the passband, all the spins within a voxel typically have similar magnitude and phase, therefore, there is no T_2^* contrast. In STFR, because of the low spatial resolution of the tailored pulse, the spins within one voxel may experience different phase mismatch due to intra-voxel B0

field variation leading to a T_2^* -like contrast. This property of STFR can be used to detect blood-oxygen-level-dependent (BOLD) signal in functional imaging, which is reported in [19], and which will be investigated in detail in future work.

We have proposed a joint RF pulse design method for STFR, which produced a modest improvement over the Separate design. We expect that our Joint algorithm can be improved in at least two ways. First, since the Joint approach formulates a nonconvex magnitude least squares problem, it is possible that our solver gets “stuck” in a local minimum. Specifically, at each iteration our algorithm solves a least squares problem $\arg\min_{\mathbf{b}} \|\mathbf{A}\mathbf{b} - \mathbf{d}\|$ whereby the phase of the target excitation pattern $\mathbf{d}$ is updated. We attempted several different initializations to the phase pattern of $\mathbf{d}$ including all zero and random phase, and achieved similar results, suggesting we may have obtained a global minimum in our experiments. However, this is not a rigorous conclusion, and it is possible that alternative solvers may improve the RF design. Second, in our Joint design formulation, we used the small tip angle approximation but we enforced the spins to be tipped down in the middle of the combined pulse. Although we are working in the small tip regime ($< 20^\circ$), this forced tip-down in the middle may still make the small tip angle approximation method less accurate. It is possible that our Joint design can be improved by borrowing ideas from large-tip-angle pulse design, e.g., the additive angle method [20] or designs based on perturbation analysis of the Bloch equation [21].

In addition to improving the RF pulse design algorithm, other complementary methods can be used to improve STFR imaging performance. One straightforward approach is to reduce data acquisition time and hence T_{free} , which reduces the spatial inhomogeneity of the target phase pattern $\theta_j(\mathbf{r})$. This can be done by, e.g., employing fast non-Cartesian readout trajectories. This approach may reduce the SNR but the SNR efficiency may not decrease much because the tailored pulse length may be shorter. In addition, high-order gradient shim systems can be employed to reduce B_0 inhomogeneity, which also makes $\theta_j(\mathbf{r})$ vary more smoothly across the ROI. This approach would benefit bSSFP as well, but shimming itself may not be sufficient to remove all the banding in bSSFP. Alternatively, parallel RF transmission should allow for improved RF pulse accuracy for a given pulse duration. Parallel excitation has been an active research area in recent years, including by our group [22], and commercial support for such systems is emerging.

A drawback of the proposed non-slice-selective imaging approach is that signal from outside the ROI may alias into the FOV. Although slab selective 3D tailored pulses could in principle be used, such pulses may be prohibitively long [23]. One potential solution to this problem is to use Cartesian readout with frequency encoding in the S/I direction, i.e., using the data acquisition filter to remove signal from outside the FOV, but this approach may require longer scan time since the A/P and R/L directions must be fully phase encoded, and these directions typically have larger matrix size. Another potential solution is to use surface coils near the region of interest such that signal contribution from outside the ROI is minimized.

Conclusions

We have developed a new steady-state sequence, unspoiled STFR, and demonstrated using analytic modeling and experiments that this sequence produces bSSFP-like signal and tissue contrast but with reduced banding artifacts. Our analysis shows that the proposed sequence is less sensitive to RF pulse inaccuracies than its spoiled counterpart. We have also proposed a novel joint RF pulse design approach that formulates the RF design problem in STFR as a magnitude least-squares minimization problem, modestly improving image quality. With this approach, we have demonstrated that brain imaging over a 3-4 cm thick 3D ROI is possible using a standard quadrature transmit/receive head coil and short tailored 3D RF pulses of 1.7 ms duration. We expect that future improvements in high-order shimming or parallel transmit systems will allow expanded 3D ROIs to be imaged with the proposed approach.

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Appendix

Define the magnetization vector as $\mathbf{M} = (M_x, M_y, M_z)^T$. Referring to Fig. 1, we model each spin path segment as follows:

1. $\mathbf{M}_1$ to $\mathbf{M}_2$: Free precession and T1, T2 relaxation.

Define ω as the local off-resonance frequency, and T_{free} as the free precession time. The free precession phase is then $\theta_f = \omega T_{\text{free}}$. The Bloch equation in matrix form for this rotation is:

$$\mathbf{M}_2 = \mathbf{P} \mathbf{C}_f \mathbf{M}_1 + \mathbf{D}_f \text{ where } \mathbf{C}_f = \begin{bmatrix} e^{-\frac{T_{\text{free}}}{T_2}} & 0 & 0 \\ 0 & e^{-\frac{T_{\text{free}}}{T_2}} & 0 \\ 0 & 0 & e^{-\frac{T_{\text{free}}}{T_1}} \end{bmatrix}, \mathbf{D}_f = (\mathbf{I} - \mathbf{C}_f) \begin{bmatrix} 0 \\ 0 \\ M_0 \end{bmatrix}, \mathbf{P} = \begin{bmatrix} \cos\theta_f & \sin\theta_f & 0 \\ -\sin\theta_f & \cos\theta_f & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

2. $\mathbf{M}_2$ to $\mathbf{M}_3$: “Tip-up” RF pulse with phase ϕ and flip angle β .

$$\mathbf{M}_3 = \mathbf{R}_u \mathbf{M}_2 \text{ where } \mathbf{R}_u = \begin{bmatrix} \cos\phi & \sin\phi & 0 \\ -\sin\phi & \cos\phi & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos\beta & -\sin\beta \\ 0 & \sin\beta & \cos\beta \end{bmatrix} \begin{bmatrix} \cos\phi & -\sin\phi & 0 \\ \sin\phi & \cos\phi & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

3. $\mathbf{M}_3$ to $\mathbf{M}_4$: Unbalanced gradient g rotates $\mathbf{M}$ about z axis by θ_g . Also include T1, T2 relaxation.

$$\mathbf{M}_4 = \mathbf{G}\mathbf{C}_g\mathbf{M}_3 + \mathbf{D}_g \text{ where } \mathbf{G} = \begin{bmatrix} \cos\theta_g & \sin\theta_g & 0 \\ -\sin\theta_g & \cos\theta_g & 0 \\ 0 & 0 & 1 \end{bmatrix}, \mathbf{C}_g = \begin{bmatrix} e^{-\frac{T_g}{T_2}} & 0 & 0 \\ 0 & e^{-\frac{T_g}{T_2}} & 0 \\ 0 & 0 & e^{-\frac{T_g}{T_1}} \end{bmatrix}, \mathbf{D}_g = (\mathbf{I} - \mathbf{C}_g) \begin{bmatrix} 0 \\ 0 \\ M_0 \end{bmatrix},$$

4. $\mathbf{M}_4$ to $\mathbf{M}_1$: The tip-down pulse rotates $\mathbf{M}$ about the x axis by α .

$$\mathbf{M}_1 = \mathbf{R}_d\mathbf{M}_4 \text{ where } \mathbf{R}_d = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos\alpha & \sin\alpha \\ 0 & -\sin\alpha & \cos\alpha \end{bmatrix}$$

Combining these steps and requiring that the magnetization reaches a steady-state, we obtain:

$$\begin{aligned} \mathbf{M}_1 &= \mathbf{R}_d(\mathbf{G}\mathbf{C}_g(\mathbf{R}_u(\mathbf{P}\mathbf{C}_f\mathbf{M}_1 + \mathbf{D}_f)) + \mathbf{D}_g) \\ \Rightarrow \mathbf{M}_1 &= (\mathbf{I} - \mathbf{R}_d\mathbf{G}\mathbf{C}_g\mathbf{R}_u\mathbf{P}\mathbf{C}_f)^{-1}(\mathbf{R}_d\mathbf{G}\mathbf{C}_g\mathbf{R}_u\mathbf{D}_f + \mathbf{R}_d\mathbf{D}_g) \end{aligned}$$

We obtain an expression for the transverse part of $\mathbf{M}$, i.e., Eq. (1), by simplifying the above expression using symbolic math software (MATHEMATICA 8, Wolfram, Champaign, Illinois, USA). The MATHEMATICA code is available on our website (<http://www.umich.edu/~sunhao>).

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Figure 1.

Proposed “unspoiled STFR” pulse sequence. (a) Steady-state path for a spin isochromat. The spin is tipped back to the longitudinal axis by a tailored pulse with flip angle $-\beta(\mathbf{r})$ and phase $\phi(\mathbf{r})$. $\phi(\mathbf{r})$ is designed to be equal to the accumulated free precession angle $\theta_f(\mathbf{r}) = \omega(\mathbf{r})T_{\text{free}}$, where T_{free} is the free precession time. (b) Example pulse sequence diagram, using tailored pulses for both tip-down (red) and tip-up (blue) excitations, and 3D Cartesian data readout.

Figure 2.

Steady-state magnetization (Eq. (1)) for a spin isochromat as a function of $\varphi + \theta_g$, where φ is the phase of the tip-up pulse and θ_g is the precession induced by the applied unbalanced gradient. Narrow bands are spaced 2π apart, and neighboring bands are equal both in magnitude and phase. In the proposed unbalanced STFR sequence, the signal from a voxel can be calculated by integrating over one full cycle (shaded region). The result of this integration is given by Eq. (2).

Figure 3.

Predicted tissue signal for unspoiled STFR (Eq. (2)), spoiled STFR [6] and bSSFP [11].

These calculations assumed $T_1/T_2 = 4000/2000\text{ms}$, $1470/71\text{ms}$, $1110/56\text{ms}$ for CSF, gray matter, and white matter, respectively [24]. The bSSFP curves were calculated using a flip angle of 2α , which is expected to produce similar signal contrast as STFR using a flip angle of α . (a) STFR produces similar signal as bSSFP, as desired. (b) STFR and bSSFP are predicted to have similar gray/white matter contrast.

Figure 4.

(a) Steady-state signal for unspoiled STFR and spoiled STFR as a function of phase mismatch ($\varphi - \theta_f$, using the analytic result from Eq. (2) and [6] ($T_1/T_2 = 510/50$ ms, $T_{\text{free}}/TR = 9/12$ ms, $\alpha = \beta = 16^\circ$) and phantom observations. Note that the rate of signal drop due to phase mismatch is smaller for unspoiled STFR. We obtained the measured curves by applying a linear gradient shim in the x direction and imaging a gel phantom (shown in (b)) with *non-tailored* (sinc) pulses. We stress that the image in (b) was obtained for the sole purpose of obtaining the curve in (a), and is *not* representative of a typical STFR image acquisition. In particular, the goal in STFR is generally to design a tailored tip-up pulse that minimizes the phase mismatch and hence maximizes the signal within a target ROI.

Figure 5.

Steady-state signal for unspoiled STFR and spoiled STFR as a function of phase mismatch $\varphi - \theta_f$ for different tissues: gray matter (GM), white matter (WM), and cerebrospinal fluid (CSF). These calculations assumed $T_1/T_2 = 4000/2000$ ms, 1470/71 ms, 1110/56ms for CSF, GM, and WM, respectively [24], and $T_{\text{free}}/TR = 7/10$ ms, $\alpha = \beta = 20^\circ$. The spoiled STFR sequence is more sensitive to phase mismatch compared to unspoiled STFR for all three tissue types, and especially for CSF.

Figure 6.

Steady-state imaging, phantom results. Images are shown on the same gray scale. For each image, the mean signal and standard deviation within the object are indicated. Unspoiled STFR with the proposed “Joint” RF pulse design (right) produces signal levels that are comparable to on-resonance bSSFP, and has improved uniformity compared to bSSFP and spoiled STFR. Unspoiled STFR with the simpler “Separate” RF pulse design approach (second from right) shows improved signal and uniformity compared to spoiled STFR, but slightly lower overall signal compared to the Joint design. Conventional SPGR and SSFP-FID images are included for reference.

Figure 7.

(a) Comparison of bSSFP (left) with three different STFR acquisitions, in the same slice. (b) field map and phase mismatch maps using separate and joint design. Banding artifacts in the anterior part (arrow) of the bSSFP image are largely absent in the unspoiled STFR images. Spoiled STFR is less uniform than unspoiled STFR as predicted, and the signal drops more in the region with high phase mismatch. Note that the CSF in the oval region in the spoiled STFR image drops significantly more than the nearby tissue signal and the unspoiled STFR CSF signal, which agrees with the phase mismatch map and sensitivity to phase mismatch plot in Fig. 5. The Joint design has slightly smaller phase mismatch, which leads to improved signal uniformity and tissue contrast compared to the Separate design. Also note that the high through-plane vessel signal in the bSSFP image is suppressed in the STFR images (see, e.g., box).

Figure 8.

(a) Proof-of-principle demonstration of 3D unspoiled STFR imaging, using Joint 3D tailored RF pulses. Images are shown for Joint unspoiled STFR, and bSSFP with different phase cycling schemes, in 5 adjacent axial slices spanning 4 cm: (Top) 0° phase cycled bSSFP; (Middle) 180° phase cycled bSSFP; (Bottom) Joint unspoiled STFR. Both bSSFP acquisitions suffer from banding artifacts, which are reduced with the 3D Joint unspoiled STFR sequence. (b) field map and phase mismatch maps. The STFR signal drops more in the region with high phase mismatch (See, e.g., arrows in (a)).

Table 1

Summary of phantom and human imaging experiments.

Object	Sequence	RF pulse	Flip angle	TR
Phantom	spoiled gradient echo (SPGR, FLASH)	sinc	20	10ms
Phantom	SSFP-FID (GRASS, FISP)	sinc	20	10ms
Phantom	bSSFP (FIESTA, TrueFISP)	sinc	40	7.6ms
Phantom	spoiled STFR	tailored (Separate)	20	10ms
Phantom	unspoiled STFR	tailored (Separate)	20	10ms
Phantom	unspoiled STFR	tailored (Joint)	20	10ms
Brain	bSSFP (FIESTA, TrueFISP)	sinc	40	7.6ms
Brain	spoiled STFR	tailored (Separate)	20	10ms
Brain	unspoiled STFR	tailored (Separate)	20	10ms
Brain	unspoiled STFR	tailored (Joint)	20	10ms

Table 2

Sequence timing.

Sequence	Tip-down	Readout	Tip-up	Gradient crusher
STFR	1.7ms	4.9ms	1.7ms	1.2ms
bSSFP	1.2ms	4.9ms	n/a	n/a