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Quantitative description of RF power-based ratiometric chemical exchange saturation transfer (CEST) pH imaging

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Abstract

Chemical exchange saturation transfer (CEST) MRI holds great promise for imaging pH. However, routine CEST measurement varies not only with pH-dependent chemical exchange rate but also with CEST agent concentration, providing pH-weighted information. Conventional ratiometric CEST imaging normalizes the confounding concentration factor by analyzing the relative CEST effect from different exchangeable groups, requiring CEST agents with multiple chemically distinguishable labile proton sites. Recently, an RF power-based ratiometric CEST MRI approach has been developed for concentration-independent pH MRI using CEST agents with a single exchangeable group. To facilitate quantification and optimization of the new ratiometric analysis, we quantitated RF power-based ratiometric CEST ratio (rCESTR) and derived its signal-to-noise and contrast-to-noise ratio. Using creatine as a representative CEST agent containing a single exchangeable site, our study demonstrated that optimized RF power-based ratiometric analysis provides good pH sensitivity. We showed that rCESTR follows a base-catalyzed exchange relationship with pH independent of creatine concentration. The pH accuracy of RF power-based ratiometric MRI was within 0.15–0.20 pH unit. Furthermore, absolute exchange rate can be obtained from the proposed ratiometric analysis. To summarize, RF power-based ratiometric CEST analysis provides concentration-independent pH-sensitive imaging and complements conventional multiple labile proton groups-based ratiometric CEST analysis.

Keywords

chemical exchange saturation transfer (CEST); MRI; pH; quantitative CEST analysis (qCEST); ratiometric CEST analysis

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1. Introduction

Chemical exchange saturation transfer (CEST) MRI is sensitive to dilute CEST agents and physiochemical properties, and has been increasingly applied *in vivo* (1–5). Specifically, the CEST effect is sensitive to the exchange rate, which is often pH-dependent, therefore permitting minimally invasive or noninvasive pH imaging (6). Indeed, CEST MRI has been applied to investigate pH change in disorders such as acute stroke and renal injury (7–12). However, in addition to pH dependence, the CEST effect strongly varies with the CEST agent concentration, relaxation rates and experimental conditions, limiting pH specificity of routine CEST MRI (13–20). Conventional ratiometric CEST analysis ratios the CEST effects from different exchangeable groups to simplify pH determination, which, however, requires CEST agents with multiple chemically distinguishable labile proton sites such as 5,6-dihydrouracil and iopamidol (21–29). Recently, RF-power based ratiometric imaging has been developed, enabling concentration-independent pH imaging from CEST agents with a single exchangeable group, alleviating stringent requirements of conventional ratiometric CEST imaging on CEST agent properties (30).

Our work aims to quantitate and optimize the recently proposed RF power-based ratiometric CEST imaging. The dependence of CEST measurement on RF power can be described empirically by two factors: labeling coefficient, which denotes the radio frequency (RF) saturation efficiency of exchangeable protons, and spillover factor, which measures the concomitant direct saturation of bulk water signal (31–36). Because both labeling coefficient and spillover factor depend on RF power level, it is necessary to elucidate the effect of experimental parameters on the RF power-based ratiometric analysis (26). We postulated that RF power-based ratiometric index (rCESTR) can reasonably remove contributions from relaxation and labile proton concentration variables, permitting pH measurement. To achieve this, we derived rCESTR and solved its signal-to-noise ratio (SNR) and contrast-to-noise ratio (CNR). We evaluated the derivations with numerical simulation and further verified it experimentally using concentration and pH CEST phantoms. Our results quantitatively described the recently proposed RF power-based ratiometric CEST MRI, aiding its experimental optimization and translation.

2. Theory

The CEST effect can be described by an empirical solution as a multiplication of simplistic

CEST effect (i.e., $\frac{f_r \cdot k_{sw}}{R_{1w} + f_r \cdot k_{sw}}$), labeling coefficient (α) and spillover factor ($1 - \sigma$) (13):

$$\text{CESTR} = \frac{f_r \cdot k_{sw}}{R_{1w} + f_r \cdot k_{sw}} \cdot \alpha \cdot (1 - \sigma) \quad [1]$$

where k_{sw} is the chemical exchange rate from labile protons to bulk water, f_r is labile proton fraction ratio, and R_{1w} is bulk water longitudinal relaxation rate (33,37). We have

$\alpha = \frac{\omega_1^2}{p \cdot q + \omega_1^2}$, where $\omega_1 = 2\pi\gamma B_{1,\gamma}$ is the gyromagnetic ratio and B_1 is the irradiation RF

amplitude, $p = \Gamma_{2s} - \frac{k_{sw}k_{ws}}{\Gamma_{2w}}$ and $q = \Gamma_{1s} - \frac{k_{sw}k_{ws}}{\Gamma_{1w}}$, in which $k_{ws} = f_r \cdot k_{sw}$ (37). Moreover,

$r_{1w,s}=R_{1w,s}+k_{ws,sw}$ and $r_{2w,s}=R_{2w,s}+k_{ws,sw}$, respectively. The spillover factor is equal to

$1 - \frac{r_{1w}}{k_{ws}} \left(\frac{R_{1w}r_{zs}\cos^2\theta + R_{1s}k_{ws}\cos\theta\cos^2(\theta/2)}{r_{zw}r_{zs} - k_{ws}k_{sw}\cos^2(\theta/2)} - \frac{R_{1w}r_{2s}\cos^2\theta}{r_{zw}r_{2s} - k_{ws}k_{sw}\sin^2\theta} \right)$, where $\theta=\tan^{-1}(\omega_l/\omega_s)$, $r_{zw}=r_{1w}\cos^2\theta/2+r_{2w}\sin^2\theta/2$, $r_{zs}=r_{1s}\cos^2\theta+r_{2s}\sin^2\theta$ and ω_s is the labile proton chemical shift.

The RF power-based ratiometric analysis ratios CEST effects obtained under two RF power levels,

$$r_{CESTR} = \frac{\left(\frac{f_r \cdot k_{sw}}{R_{1w} + f_r \cdot k_{sw}} \right)}{\left(\frac{f_r \cdot k_{sw}}{R_{1w} + f_r \cdot k_{sw}} \right)} \cdot \frac{\alpha \cdot (1 - \sigma)|_{\omega_{1a}}}{\alpha \cdot (1 - \sigma)|_{\omega_{1b}}} \quad [2]$$

where ω_{1a} and ω_{1b} are two RF power levels. Because the simplistic CEST effect term is normalized, rCESTR is sensitive to exchange rate, not the labile proton ratio. For dilute CEST agents with typical relaxation rates, we have $p \approx R_{2s} + k_{sw}$ and $q \approx k_{sw}$. rCESTR can be shown to be

$$r_{CESTR} \approx \frac{\frac{\omega_{1a}^2}{k_{sw}(R_{2s} + k_{sw}) + \omega_{1a}^2}}{\frac{\omega_{1b}^2}{k_{sw}(R_{2s} + k_{sw}) + \omega_{1b}^2}} \cdot \left(\frac{(1 - \sigma)|_{\omega_{1a}}}{(1 - \sigma)|_{\omega_{1b}}} \right) \quad [3]$$

In order to solve the exchange rate, we simplified Eq. 3 and showed that

$$1 + \frac{\omega_{1b}^2 - \omega_{1a}^2}{k_{sw}(R_{2s} + k_{sw}) + \omega_{1a}^2} = \left(\frac{(1 - \sigma)|_{\omega_{1b}}}{(1 - \sigma)|_{\omega_{1a}}} \right) \cdot \frac{\omega_{1b}^2}{\omega_{1a}^2} \cdot r_{CESTR} \quad [4]$$

The exchange rate term can be shown to be

$$k_{sw}(R_{2s} + k_{sw}) = \frac{\omega_{1b}^2 - \omega_{1a}^2}{\left(\frac{(1 - \sigma)|_{\omega_{1b}}}{(1 - \sigma)|_{\omega_{1a}}} \right) \cdot \frac{\omega_{1b}^2}{\omega_{1a}^2} \cdot r_{CESTR} - 1} - \omega_{1a}^2 \quad [5]$$

, and the exchange rate can be solved as

$$k_{sw} = \frac{\sqrt{R_{2s}^2 + 4 \left(\frac{\omega_{1b}^2 - \omega_{1a}^2}{\left(\frac{(1 - \sigma)|_{\omega_{1b}}}{(1 - \sigma)|_{\omega_{1a}}} \right) \cdot \frac{\omega_{1b}^2}{\omega_{1a}^2} \cdot r_{CESTR} - 1} - \omega_{1a}^2 \right)} - R_{2s}}{2} \quad [6]$$

We also derived the SNR and CNR of the proposed RF power-based rCESTR index. Briefly, we have previously shown that SNR for CESTR derived from the asymmetry analysis is (38)

$$SNR_{CESTR} \approx \frac{CESTR}{\sqrt{2 + CESTR^2}} \cdot SNR_{I_0} \quad [7]$$

where SNR_{I_0} is SNR of the control image without RF irradiation. For the RF power-based ratiometric analysis, its SNR can be derived based on error propagation theory (Appendix) and we have

$$\begin{aligned}\sigma_{\text{rCESTR}}^2 &\approx \left(\frac{\partial \text{rCESTR}}{\partial \text{CESTR}(\omega_{1a})} \right)^2 \sigma_{\text{CESTR}(\omega_{1a})}^2 + \left(\frac{\partial \text{rCESTR}}{\partial \text{CESTR}(\omega_{1b})} \right)^2 \sigma_{\text{CESTR}(\omega_{1b})}^2 \\ &= \frac{\text{CESTR}^2(\omega_{1a})}{\text{CESTR}^2(\omega_{1b})} \left(\frac{1}{\text{SNR}_{\text{CESTR}(\omega_{1a})}^2} + \frac{1}{\text{SNR}_{\text{CESTR}(\omega_{1b})}^2} \right)\end{aligned}\quad [8]$$

and

$$\text{SNR} = \frac{\text{rCESTR}}{\sigma_{\text{rCESTR}}} = \frac{\text{SNR}_{\text{CESTR}|\omega_{1a}} \cdot \text{SNR}_{\text{CESTR}|\omega_{1b}}}{\sqrt{\text{SNR}_{\text{CESTR}|\omega_{1a}}^2 + \text{SNR}_{\text{CESTR}|\omega_{1b}}^2}} \quad [9]$$

The standard deviation of the pH-sensitive rCESTR contrast (rCESTR) can be derived as,

$$\sigma_{\Delta \text{rCESTR}}^2 = \left(\frac{\partial \Delta \text{rCESTR}}{\partial \text{rCESTR}|_{\text{pHa}}} \right)^2 \sigma_{\text{rCESTR}|_{\text{pHa}}}^2 + \left(\frac{\partial \Delta \text{rCESTR}}{\partial \text{rCESTR}|_{\text{pHb}}} \right)^2 \sigma_{\text{rCESTR}|_{\text{pHb}}}^2 = \sigma^2 \Big|_{\text{rCESTR}(\text{pHa})} + \sigma^2 \Big|_{\text{rCESTR}(\text{pHb})} \quad [10]$$

where pH_a and pH_b refer to two pH values of interest. The contrast to noise ratio (CNR) can be shown to be

$$\text{CNR} = \frac{\Delta \text{rCESTR}}{\sigma_{\Delta \text{rCESTR}}} = \frac{(\text{rCESTR}|_{\text{pHa}} - \text{rCESTR}|_{\text{pHb}})}{\sqrt{\left(\frac{(1+\text{rCEDTR}^2)}{\text{CESTR}^2(\omega_{1b})} \Big|_{\text{pHa}} + \frac{(1+\text{rCEDTR}^2)}{\text{CESTR}^2(\omega_{1b})} \Big|_{\text{pHb}}}} \cdot \frac{\text{SNR}_{I_0}}{\sqrt{2}} \quad [11]$$

Eq. 11 decouples CNR into rCNR and $\text{SNR}(I_0)$. rCNR largely depends on CEST effect under the influence of parameters such as RF irradiation level and duration. In addition, $\text{SNR}(I_0)$ mainly depends on parameters such as TR, TE, flip angle, number of average, field strength and voxel size etc.

3. Materials and methods

Phantom

Two phantoms were prepared with creatine and phosphate buffer solution. For the pH phantom, the creatine concentration was fixed to 60 mM while its pH was titrated to 5.99, 6.48, 6.75, 7.02 and 7.24 (EuTech Instrument, Singapore). For the concentration phantom, we varied creatine concentration from 100, 80, 60, 40 to 20 mM, and titrated their pH to 6.75. The solution was transferred into centrifuge tubes and inserted into two separate phantom containers. The containers were then filled with 1% low gelling point agarose solution and solidified at room temperature to fixate the creatine-PBS tubes.

Simulation

CEST MRI effect was simulated using the Bloch-McConnell 2-pool exchange model in Matlab (Mathworks, Natick MA), as described previously (31). We assumed typical T_{1w} and T_{2w} of 2 s and 100 ms, and T_{1s} and T_{2s} of 1 s and 15 ms, respectively, with the labile proton chemical shift of 1.9 ppm at 4.7 T. Exchange rate was varied from 20 to 1,000 s^{-1} (20). In addition, to elucidate the SNR and CNR dependence upon selection of RF power levels, we simulated rCESTR with RF irradiation levels from 0 to 4 μT .

MRI

All images were obtained from a 4.7 T MRI scanner (Bruker Biospec, Billerica, MA). We collected single-shot echo planar imaging (EPI) with an acquisition bandwidth of 200 kHz. We chose a slice thickness of 5 mm, field of view (FOV) of 76×76 mm and imaging matrix of 64×64. We acquired CEST MRI with continuous wave (CW) RF irradiation applied at ± 1.9 ppm (± 375 Hz at 4.7 Tesla) from the bulk water resonance, in addition to a control scan without RF irradiation (repetition time (TR)/echo time (TE)=22,000/28 ms, time of saturation (TS)=10,000 ms, number of average (NSA)=2). The RF power level was varied from 0.3 to 3 μT : from 0.3 to 1 μT with an increment step of 0.1 μT , followed by 1.25, 1.5, 1.75, 2, 2.5 and 3 μT . In addition, T_1 -weighted inversion recovery MRI was obtained with inversion intervals (TI) from 250 to 10,000 ms (recovery time/TE =12s/28 ms, NSA=2). T_2 -weighted MRI was acquired using spin echo images with TE from 50 to 500 ms (TR=12s, NSA=2) (39). The B_0 map was obtained using phase images with off-centered echo time of 1, 3, 5 and 7 ms. The B_1 field was calibrated by varying the pre-pulse flip angle (θ) from 10 to 180°, with intervals of 10°.

Data Processing

Data were processed in Matlab (Mathworks, Natick, MA). The T_1 map was obtained by least-squares fitting of the signal (I) as a function of the inversion time ($I=I_0[1-(1+\eta)e^{-TI/T_1}]$), where η is the inversion efficiency and I_0 is the equilibrium signal. The T_2 map was derived by fitting the signal intensity as a function of TE, I_0e^{-TI/T_1} . B_0 map was derived by fitting the phase map (ϕ) against the echo time shift (τ) using

$\Delta B_0 = \frac{2\pi}{\gamma} \frac{\phi}{\Delta\tau}$, where γ is the gyromagnetic ratio. The magnetic field was highly homogeneous, with B_0 being 5 ± 5 Hz and 2 ± 4 Hz for the pH and concentration phantoms, respectively. B_1 field was calibrated by fitting the image intensity using $I(\theta) = I_0 \cdot |\cos(\eta \cdot B_1 + B_1) \cdot \tau|$, where B_1 and η are the offset and scaling factor, respectively. We found $B_1 = -0.21$ and $\eta = 1.02$. The RF power irradiation level for CEST MRI was calibrated, being 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 1.0, 1.3, 1.5, 1.8, 2.3 and 2.7 μT . CEST effect was calculated by taking the difference of reference (I_{ref}) and labels scans (I_{label}), normalized by the control scan without RF irradiation

$$CESTR = (I_{ref} - I_{label}) / I_0 \quad [12]$$

Results were reported as mean $\pm$ standard deviation, and P values less than 0.05 were considered statistically significant.

4. Results

Fig. 1 shows simulated rCESTR as a function of labile proton ratio and exchange rate. Briefly, Fig. 1a shows CEST effect calculated from the asymmetry analysis as a function of B_1 for two representative exchange rates of 50 (dashed dotted) and 300 s^{-1} (solid). CESTR initially increases with B_1 due to more efficient RF saturation, but decreases at higher RF power level because of concomitant direct saturation (spillover) of the bulk water signal. Fig. 1b shows rCESTR contrast between two exchange rates under varied B_1 levels (rCESTR). For simplicity, we assumed B_{1a} is stronger than B_{1b} . Because CESTR is small under weak irradiation levels, rCESTR peaks when taking the ratio of CESTR obtained under a pair of weak and strong B_1 levels. Because of the broad range of rCESTR, we showed logarithm of rCESTR in Fig. 1b. It is necessary to note that the relative CNR ($\text{rCNR} = \text{CNR}/\text{SNR}_{\text{f0}}$) has to be considered when optimizing the RF power-based ratiometric MRI. Fig. 1c shows that simulated rCNR as a function of B_1 level up to $4 \mu\text{T}$. rCNR reasonably plateaus under two moderate B_1 levels, being around $0.5\text{--}1$ and $1.5\text{--}2.5 \mu\text{T}$, respectively. rCESTR was simulated for a range of labile proton concentration (1:2000 to 1:500) and exchange rate (20 to 1000 s^{-1}), assuming two typical B_1 of 0.5 and $2 \mu\text{T}$. Fig. 1d shows rCESTR strongly depends on exchange rate with little change with labile proton ratio.

Fig. 2 evaluates the RF power-based ratiometric CEST MRI measurement in the pH phantom. Figs. 2a and 2b show CESTR maps obtained under RF power levels of 0.5 and $2.3 \mu\text{T}$. Notably, CESTR appears slightly hyperintense for intermediate pH values under $0.5 \mu\text{T}$, while CESTR for higher pH vials substantially increased at $2.3 \mu\text{T}$. This is because a weak RF power of $0.5 \mu\text{T}$ is inefficient to saturate relatively fast exchangeable protons at high pH, leading to a small labeling coefficient. The saturation efficiency substantially increases for B_1 of $2.3 \mu\text{T}$, resulting in stronger CEST effect at high pH (Fig. 2b). Fig. 2c evaluates the CNR between pH compartments of 5.99 and 7.24 as a function of RF power levels. We found CNR peaks when taking the ratio of CESTR maps obtained using a moderately weak ($\sim 0.5 \mu\text{T}$) and an intermediate RF power ($\sim 2.3 \mu\text{T}$) levels. Although we used CNR in Fig. 2c while we showed simulated rCNR in Fig. 1c, they displayed similar trend. Fig. 2d shows rCESTR map obtained under optimal B_1 levels, showing consistent increase with pH.

Fig. 3 evaluates the RF power-based ratiometric CEST MRI measurement in the creatine concentration phantom. Figs. 3a and 3b show CESTR maps for RF powers of 0.5 and $2.3 \mu\text{T}$. Notably, CESTR appears relatively hyperintense for the vial of the highest creatine concentration, and CESTR increased substantially when RF power was increased from 0.5 to $2.3 \mu\text{T}$. This is because all vials were titrated to the same pH, resulting in similar exchange rate and hence labeling coefficient. As a result, CESTR increased with labile proton concentration. Because rCESTR normalizes the confounding CEST agent concentration factor, there was little contrast between different creatine concentration vials. Fig. 3c evaluates the CNR between 20 and 100 mM creatine vials, which showed little dependence with RF power levels. Using the optimal RF power levels determined from pH phantom, rCESTR map (Fig. 3d) shows little change with creatine concentration.

Fig. 4 compares rCESTR as a function of pH and creatine concentration from *in vitro* MRI measurement. Specifically, Fig. 4a shows that rCESTR increases with pH, following a base-

catalyzed relationship, being $rCESTR = 0.76 + 0.87 \cdot 10^{pH-6.76}$ (dash dotted line). The base-catalyzed fitting was in good agreement with $rCESTR$ measurement, suggesting dominantly base-catalyzed amine proton exchange rate ($P < 0.01$, linear regression t-test). In comparison, $rCESTR$ showed little change with creatine concentration, being $rCESTR = -0.007 \cdot [Cr] + 2.13$, where $[Cr]$ is creatine concentration in mM (Fig. 4b). Importantly, no significant correlation between $rCESTR$ and creatine concentration was found ($P > 0.05$, linear regression t-test). Using the relationship between $rCESTR$ and pH determined from Fig. 4a, pH map was derived for the pH (Fig. 4c) and concentration phantom (Fig. 4d). Fig. 4e shows pH derived from RF power-based ratiometric analysis strongly correlates with pH ($P < 0.01$, linear regression t-test) while it showed non-significant correlation with creatine concentration ($P > 0.05$, Fig. 4f, linear regression t-test). Particularly, for the pH phantom, pH_{MRI} was within 0.11 pH unit from titrated pH values while for the creatine concentration phantom, pH_{MRI} accuracy was within 0.20 pH unit.

Fig. 5 shows the exchange rate derived from RF power-based ratiometric CEST MRI measurement. The bulk water T_1 and T_2 were obtained by extrapolating relaxation time as a function of creatine concentration, being 3.0 and 1.9 s, respectively. Fig. 5a shows that exchange rate determined from Eq. 7 for the pH phantom increases with pH, consistent with the fact that creatine amine proton chemical exchange is dominantly base-catalyzed. Fig. 5b shows that the exchange rate as a function of pH can be described by $k_{sw} = 54 + 1.16 \cdot 10^{pH-4.98}$ ($R^2 = 0.964$, $P < 0.01$, linear regression t-test). In comparison, exchange rate determined from the concentration phantom had very little change with creatine concentration (Fig. 5c). Fig. 5d shows that the exchange rate among different creatine concentration was not statistically significant ($P > 0.05$, linear regression t-test). Indeed, the exchange rate was 140 s^{-1} from the pH compartment of 6.75 at 60 mM, in good agreement with the exchange rate of $142 \pm 22 \text{ s}^{-1}$, determined from the concentration phantom with creatine concentration varied from 20 to 100 mM (pH=6.75).

Fig. 6 evaluates the simulated effects of labile proton ratio, relaxation rate and labile proton offset on the RF power-based $rCESTR$ analysis. We assumed two B_1 levels of 0.5 and 2 μT with typical $f_r = 1:1000$, $\delta = 400 \text{ Hz}$ (2 ppm at 4.7 T), T_{1w} and T_{2w} of 2 and 0.1 s, and T_{1s} and T_{2s} of 1 s and 15 ms respectively, and one parameter was varied for each simulation (labile proton ratio and offset, T_{1w} and T_{2w}). Although CESTR approximately increases linearly with the labile proton ratio, Fig. 6a shows that $rCESTR$ decreases slightly with labile proton ratio from 1:2000 to 1:500, with the relative $rCESTR$ difference from that of the median f_r being from -10 to 12%. This is because the increase of experimental factor (i.e., $\alpha \cdot (1-\sigma)$) with respect to labile proton ratio is faster under dilute CEST concentration (40). Fig. 6b shows that SNR increases substantially with labile proton ratio due to higher raw CEST effect. Interestingly, SNR peaks at an intermediate exchange rate of 200 s^{-1} due to the choice of two moderate RF power levels (0.5 and 2 μT), and the dependence of $rCESTR$ upon labile proton exchange rate and chemical shift is further investigated in Fig. 7. In addition, Fig. 6c shows that $rCESTR$ decreases slightly with T_{1w} , with the relative $rCESTR$ difference from that of the median T_{1w} being from -28 to 20% for T_{1w} between 2.5 and 1.5 s. This is because the experimental factor and hence $rCESTR$ decreases slightly with T_{1w} . As such, T_1 normalization could allow enhanced pH determination. Briefly, we calculated

T_1 -corrected pH using first order correction of $pH_{MRI}'(j) = \frac{pH_{MRI}(j)}{T_{1w}(j)} \cdot \overline{T_{1w}(j)}$, where j refers to j^{th} pH or creatine concentration. We showed slightly more accurate pH determination, within 0.15 instead of 0.20 pH unit (data not shown). Importantly, SNR increases substantially with T_1 due to increased CEST effect at long T_1 (Fig. 6d). Fig. 6e shows that rCESTR slightly increases with T_{2w} , with the relative difference from -25% to 19% for T_{2w} between 100 and 200 ms, with slightly increased SNR (Fig. 6f). This is because the RF spillover effect is less at longer T_2 , resulting in higher magnitude and sensitivity of ratiometric CEST MRI. Moreover, we showed that rCESTR increases substantially with labile proton offset, with the relative difference varying from -85% to 42% for offset from 200 to 1000 Hz. Similarly, SNR increases at large labile proton offset due to less concomitant direct RF saturation effect.

5. Discussion

Our study demonstrated that the RF-power based ratiometric CEST analysis provides a simple concentration-independent pH-sensitive MRI index. It relieves the limitation of conventional ratiometric CEST MRI that is only applicable to CEST agents containing multiple chemically distinguishable labile proton sites. By elucidating the magnitude and sensitivity of RF-power based ratiometric CEST MRI, our work aids its experimental optimization and quantification, particularly important for in vivo translation.

The proposed rCESTR solution advances prior quantitative CEST (qCEST) analysis. For example, quantification of exchange rate with saturation power (QUESP), time (QUEST), and time with ratiometric analysis (QUESTRA) have been demonstrated (16,32,41). Because these results are sensitive to labile proton ratio-weighted exchange rate, their specificity may be limited without knowledge of CEST agent concentration. We have previously shown that RF power (RFP)-CEST analysis enables delineation of labile proton ratio from exchange rate, which, however, requires multi-parameter non-linear fitting (20). We recently showed that the RF spillover effect can be estimated, the correction of which improves precision of omega plot analysis for quantification of diamagnetic CEST agents (40,41). Modified linear analysis methods have also been developed to estimate fast chemical exchange rate, providing simple alternatives (42). However, these modified quantitative CEST analysis requires reasonable estimation of bulk water relaxation rates and regression analysis. In comparison, the RF power-based ratiometric CEST analysis only requires ratioing CEST measurements obtained under two different RF power levels, which provides a pH-sensitive index that is simple to use yet reasonably accurate.

Although it takes one B_1 level to optimize routine CEST imaging, the RF power-based ratiometric CEST effect depends on two RF power levels, which are related to not only the pH contrast (i.e. rCESTR) but also rCESTR and CESTR of each pH compartment (Eq. 11). Because analytical solution of two optimal RF power levels requires multi-parameter optimization, and the boundary conditions such as the maximally applicable B_1 level have to be considered, we solved the optimal power levels with numerical simulation. To demonstrate this, we simulated rCESTR MRI for exchange rate from 20 to 1000 s^{-1} at 4.7T, assuming typical T_{1w} and T_{2w} of 2 s and 100 ms, respectively. Fig. 7a shows that the

simulated peak rCNR increases with the difference between two exchange rates. Fig. 7b plots the numerically-derived optimal B_1 levels under which peak rCNR was obtained for a pair of exchange rates. Interestingly, B_{1a} consistently increased with exchange rate while B_{1b} remained relatively constant. On the other hand, optimal B_1 level can be derived for each exchange rate independently, which typically increases with exchange rate (13). Fig. 7c shows the numerically simulated optimal B_1 levels for peak rCNR normalized by optimal B_1 levels for each exchange rate independently, which deviated substantially from unity. This suggests that choice of optimal B_1 levels for RF power-based ratiometric CEST MRI aims to maximize SNR and/or CNR of rCESTR, different from conventional CEST MRI that optimizes each exchange rate independently. Because the RF spillover effect decreases at large chemical shift, it results in increased peak rCNR (Fig. 7d). These findings demonstrate the importance of elucidating RF power dependence of rCESTR for optimization of RF power-based ratiometric pH MRI. It is necessary to briefly discuss the effect of field strength on the ratiometric measurement. Because T_1 is typically longer at higher field, CEST effect and hence sensitivity of RF power-based ratiometric CEST MRI increase with field strength. Although T_2 may decrease somewhat with field strength, labile proton offset in Hz scales linearly with the field strength, resulting in less RF spillover effects and hence higher sensitivity. Furthermore, because SNR of the control image substantially increases with the field strength, it is advantageous to conduct RF power based-ratiometric CEST MRI at high field, as expected.

Our study chose a relatively simple 2-pool exchange model to elucidate the RF power-based ratiometric MRI and demonstrated it *in vitro* using creatine. Recent studies have investigated creatine CEST imaging in tumor (43) and muscle (44), and chosen it as an *in vitro* model CEST agent (40,45,46). Because creatine labile proton is relatively close to the bulk water resonance, it is susceptible to RF spillover effect. As such, *in vitro* demonstration of RF power-based ratiometric CEST MRI using creatine complements our prior work and further demonstrates the generality of the new ratiometric CEST MRI approach. Our *in vitro* study investigated creatine concentration from 20 to 100 mM, with corresponding labile proton ratio being 1:2000 and 1:400, respectively. This represents cases of dilute and reasonably concentrated CEST agents, which are of tremendous interest to the field of CEST MRI. It is important to point out that although illustrative, *in vitro* systems are simplistic and there is a lack of semisolid macromolecular magnetization transfer (MT) and nuclear overhauser effects (NOE). Such concomitant effects have to be taken into account when translating RF power-based ratiometric CEST imaging *in vivo*. For example, Longo et al. showed that in renal pH imaging, the confounding RF irradiation effects could be delineated by monitoring MRI signal difference before and after contrast agent administration (30). In addition, our study used a long saturation time to reach the steady state. It has been shown that TS-dependent CEST effect can be crudely approximated by $\text{CESTR}(\text{TS}) = \text{CESTR}(\infty) \cdot (1 - e^{-R_{1p} \cdot \text{TS}})$, where R_{1p} is the spin locking longitudinal relaxation rate and $\text{CESTR}(\infty)$ is the steady state CEST effect (47,48). Because R_{1p} increases with B_1 , rCESTR at high B_1 approaches its steady state more quickly than that of lower B_1 . This means that rCESTR reaches its steady state more quickly than CESTR. In addition, the SNR and/or CNR approximately follows the time course of rCESTR (i.e., $1 - e^{-R_{1p} \cdot \text{TS}}$). As such, moderate saturation time can be used for rCESTR MRI, provided that SNR is sufficient for

satisfactory measurement. It is important to note that the endogenous amide proton transfer (APT) MRI effect is relatively weak due to small chemical exchange rate difference during acute stroke, and it remains somewhat challenging to directly apply RF power-based ratiometric imaging to determine tissue pH noninvasively (12,33). As such, development of sensitive acquisition schemes and novel post-processing routines is crucial for further advancing the generalized ratiometric CEST MRI for endogenous pH quantification in diseases such as stroke, tumor, and renal injury (29,45,49–52).

6. Conclusions

Our study demonstrated that RF power-based ratiometric analysis is sensitive to the exchange rate with little dependence on the CEST agent concentration. Using creatine as a representative CEST agent containing a single exchangeable site, we showed that rCESTR MRI provides pH-sensitive imaging with a pH accuracy of within 0.15-0.2 pH unit. We further elucidated the magnitude and sensitivity of rCESTR MRI, aiding its experimental optimization and in vivo translation.

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Abbreviations

CEST	Chemical exchange saturation transfer
CESTR	Chemical exchange saturation transfer ratio
CNR	Contrast to noise ratio
qCEST	Quantitative chemical exchange saturation transfer
rCESTR	Ratiometric CEST ratio
RF	radio frequency
SNR	Signal to noise ratio

Appendix

For the recently proposed RF power-based ratiometric CEST index (rCESTR), we have

$$\text{rCESTR} = \frac{\text{CESTR}(\omega_{1a})}{\text{CESTR}(\omega_{1b})} \quad [\text{A.1}]$$

The partial derivative of rCESTR against CESTR obtained at each RF power level can be derived as

$$\left(\frac{\partial \text{rCESTR}}{\partial \text{CESTR}(\omega_{1a})}\right)^2 = \frac{1}{\text{CESTR}^2(\omega_{1b})} \quad [\text{A.2.a}]$$

$$\left(\frac{\partial \text{rCESR}}{\partial \text{CESTR}(\omega_{1b})}\right)^2 = \frac{\text{CESTR}^2(\omega_{1a})}{\text{CESTR}^4(\omega_{1b})} \quad [\text{A.2.b}]$$

The standard deviation of rCESTR can be shown to be,

$$\begin{aligned} \sigma_{\text{rCESTR}}^2 &\approx \left(\frac{\partial \text{rCESTR}}{\partial \text{CESTR}(\omega_{1a})}\right)^2 \sigma_{\text{CESTR}(\omega_{1a})}^2 + \left(\frac{\partial \text{rCESTR}}{\partial \text{CESTR}(\omega_{1b})}\right)^2 \sigma_{\text{CESTR}(\omega_{1b})}^2 \\ &= \frac{1}{\text{CESTR}^2(\omega_{1b})} \sigma_{\text{CESTR}(\omega_{1a})}^2 + \frac{\text{CESTR}^2(\omega_{1a})}{\text{CESTR}^4(\omega_{1b})} \sigma_{\text{CESTR}(\omega_{1b})}^2 \\ &= \frac{\text{CESTR}^2(\omega_{1a})}{\text{CESTR}^2(\omega_{1b})} \frac{\sigma_{\text{CESTR}(\omega_{1a})}^2}{\text{CESTR}^2(\omega_{1a})} + \frac{\text{CESTR}^2(\omega_{1a})}{\text{CESTR}^2(\omega_{1b})} \frac{\sigma_{\text{CESTR}(\omega_{1b})}^2}{\text{CESTR}^2(\omega_{1b})} \\ &= \text{rCESTR}^2 \cdot \left(\frac{1}{\text{SNR}_{\text{CESTR}(\omega_{1a})}^2} + \frac{1}{\text{SNR}_{\text{CESTR}(\omega_{1b})}^2} \right) \end{aligned} \quad [\text{A.3}]$$

The SNR can be shown to be

$$\text{SNR}_{\text{rCESTR}} = \frac{\text{SNR}_{\text{CESTR}(\omega_{1a})} \cdot \text{SNR}_{\text{CESTR}(\omega_{1b})}}{\sqrt{\text{SNR}_{\text{CESTR}(\omega_{1a})}^2 + \text{SNR}_{\text{CESTR}(\omega_{1b})}^2}} \quad [\text{A.4}]$$

To calculate CNR, we have rCESTR being the difference of rCESTR of two pH values.

$$\Delta \text{rCESTR} = \text{rCESTR}|_{\text{pHa}} - \text{rCESTR}|_{\text{pHb}} \quad [\text{A.5}]$$

The standard deviation of rCESTR can be derived as

$$\sigma_{\Delta \text{rCESTR}}^2 = \left(\frac{\partial \Delta \text{rCESTR}}{\partial \text{rCESTR}|_{\text{pHa}}}\right)^2 \sigma_{\text{rCESTR}|_{\text{pHa}}}^2 + \left(\frac{\partial \Delta \text{rCESTR}}{\partial \text{rCESTR}|_{\text{pHb}}}\right)^2 \sigma_{\text{rCESTR}|_{\text{pHb}}}^2 = \sigma^2 \Big|_{\text{rCESTR}(\text{pHa})} + \sigma^2 \Big|_{\text{rCESTR}(\text{pHb})} \quad [\text{A.6}]$$

We have

$$\text{CNR} = \frac{\Delta r_{\text{CESTR}}}{\sigma_{\Delta r_{\text{CESTR}}}}$$

$$= \frac{\left| \frac{\text{CESTR}(\omega_{1a})}{\text{CESTR}(\omega_{1b})} \right|_{\text{pHa}} - \left| \frac{\text{CESTR}(\omega_{1a})}{\text{CESTR}(\omega_{1b})} \right|_{\text{pHb}}}{\sqrt{\left| \frac{\text{CESTR}(\omega_{1a})}{\text{CESTR}(\omega_{1b})} \left(\frac{1}{\text{SNR}_{\text{CESTR}(\omega_{1a})}^2} + \frac{1}{\text{SNR}_{\text{CESTR}(\omega_{1b})}^2} \right) \right|_{\text{pHa}} + \left| \frac{\text{CESTR}(\omega_{1a})}{\text{CESTR}(\omega_{1b})} \left(\frac{1}{\text{SNR}_{\text{CESTR}(\omega_{1a})}^2} + \frac{1}{\text{SNR}_{\text{CESTR}(\omega_{1b})}^2} \right) \right|_{\text{pHb}}}}$$

[A. 7]

For small CEST effect, we have $\text{SNR}_{\text{CESTR}} \approx \frac{\text{CESTR}}{\sqrt{2}} \cdot \text{SNR}_{I_0}$ (38) and CNR can be simplified as

$$\text{CNR} \approx \frac{\left(\left| \frac{\text{CESTR}(\omega_{1a})}{\text{CESTR}(\omega_{1b})} \right|_{\text{pHa}} - \left| \frac{\text{CESTR}(\omega_{1a})}{\text{CESTR}(\omega_{1b})} \right|_{\text{pHb}} \right)}{\sqrt{\left(\left| \frac{\text{CESTR}(\omega_{1a})}{\text{CESTR}(\omega_{1b})} \left(\frac{2}{\text{CESTR}^2(\omega_{1a})} + \frac{2}{\text{CESTR}^2(\omega_{1b})} \right) \right|_{\text{pHa}} + \left| \frac{\text{CESTR}(\omega_{1a})}{\text{CESTR}(\omega_{1b})} \left(\frac{2}{\text{CESTR}^2(\omega_{1a})} + \frac{2}{\text{CESTR}^2(\omega_{1b})} \right) \right|_{\text{pHb}} \right)} \cdot \frac{1}{\text{SNR}_{I_0}^2}}$$

$$= \frac{\left(\left| \frac{\text{CESTR}(\omega_{1a})}{\text{CESTR}(\omega_{1b})} \right|_{\text{pHa}} - \left| \frac{\text{CESTR}(\omega_{1a})}{\text{CESTR}(\omega_{1b})} \right|_{\text{pHb}} \right) \cdot \frac{\text{SNR}_{I_0}}{\sqrt{2}}}{\sqrt{\left(\left| \frac{1}{\text{CESTR}^2(\omega_{1b})} + \frac{\text{CESTR}^2(\omega_{1a})}{\text{CESTR}^4(\omega_{1b})} \right|_{\text{pHa}} + \left(\frac{1}{\text{CESTR}^2(\omega_{1b})} + \frac{\text{CESTR}^2(\omega_{1a})}{\text{CESTR}^4(\omega_{1b})} \right) \right|_{\text{pHb}}}}$$

$$= \frac{\left(r_{\text{CESTR}}|_{\text{pHa}} - r_{\text{CESTR}}|_{\text{pHb}} \right)}{\sqrt{\left| \frac{(1+r_{\text{CESTR}}^2)}{\text{CESTR}^2(\omega_{1b})} \right|_{\text{pHa}} \left| \frac{(1+r_{\text{CESTR}}^2)}{\text{CESTR}^2(\omega_{1b})} \right|_{\text{pHb}}}}} \cdot \frac{\text{SNR}_{I_0}}{\sqrt{2}}$$

[A. 8]

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Fig. 1. Simulation of RF power-based rCESTR analysis. a) Routine asymmetry analysis (i.e., CESTR) as a function of B_1 level for two representative exchange rates. b) Logarithm of rCESTR contrast ($\Delta r\text{CESTR}$) as a function of B_1 level. c) Relative contrast to noise ratio (rCNR) of rCESTR as a function of B_1 level. d) Simulated rCESTR under typical B_1 levels of 0.5 and 2 μT for representative labile proton ratio and exchange rate.

Fig. 2.
rCESTR analysis in a pH CEST phantom. a) CESTR map ($B_1 = 0.5 \mu\text{T}$). b) CESTR map ($B_1 = 2.3 \mu\text{T}$). c) CNR between pH of 5.99 and 7.24. d) rCESTR map ($B_{1a} = 2.3$ and $B_{1b} = 0.5 \mu\text{T}$).

Fig. 3.
rCESTR analysis in a concentration CEST phantom. a) CESTR map ($B_1 = 0.5 \mu\text{T}$). b) CESTR map ($B_1 = 2.3 \mu\text{T}$). c) CNR between 20 and 100 mM creatine vials. d) rCESTR map ($B_{1a} = 2.3$ and $B_{1b} = 0.5 \mu\text{T}$).

Fig. 4.

Comparison of rCESTR from pH and concentration phantoms. a) rCESTR as a function of pH. b) rCESTR as a function of creatine concentration. c) pH map determined from rCESTR map of the pH phantom. d) pH map determined from rCESTR map of the concentration phantom. e) Regression analysis between pH determined from rCESTR MRI (pH_{MRI}) with titrated pH for the pH phantom. f) Regression analysis between pH_{MRI} with creatine concentration for the creatine concentration phantom.

Fig. 5.

Derivation of exchange rate from rCESTR analysis. a) Exchange rate map for the pH phantom. b) Exchange rate can be described by a dominantly base-catalyzed chemical exchange relationship. c) Exchange rate map for the creatine concentration phantom. d) Exchange rate as a function of creatine concentration.

Fig. 6.

Investigation of rCESTR sensitivity. a) rCESTR as a function of labile proton ratio and exchange rate. b) rSNR as a function of labile proton ratio and exchange rate. c) rCESTR as a function of T_{1w} and exchange rate. d) rSNR as a function of T_{1w} and exchange rate. e) rCESTR as a function of T_{2w} and exchange rate. f) rSNR as a function of T_{2w} and exchange rate. g) rCESTR as a function of labile proton offset and exchange rate. h) rSNR as a function of labile proton offset and exchange rate.

Fig. 7.

Optimization of rCESTR MRI. a) Numerically derived peak rCNR for exchange rates from 20 to 1000 s^{-1} ($T_{1w}/T_{2w}=2s/100ms$, $\delta_s=2$ ppm at 4.7 Tesla). b) Simulated optimal B_1 levels for peak rCNR. c) Optimal B_1 levels for peak rCNR normalized by optimal B_1 levels for each exchange rate independently. d) Peak rCNR as a function of chemical shift.