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What Can We Learn From Fitness Landscapes?

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Abstract

A combinatorially complete data set consists of studies of all possible combinations of a set of mutant sites in a gene or mutant alleles in a genome. Among the most robust conclusions from these studies is that epistasis between beneficial mutations often shows a pattern of diminishing returns, in which favorable mutations are less fit when combined than would be expected. Another robust inference is that the number of adaptive evolutionary paths is often limited to a relatively small fraction of the theoretical possibilities, owing largely to sign epistasis requiring evolutionary steps that would entail a decrease in fitness. Here we summarize these and other results while also examining issues that remain unresolved and future directions that seem promising.

Introduction

In evolutionary biology, the fitness landscape of set of mutants is the mapping of genotypes onto phenotypes when the phenotype is fitness or some proxy for fitness such as growth rate or drug resistance. When the set of mutants is not too large, it is possible to create every possible combination of mutants and map these to fitness. Such combinatorially complete datasets have great potential to inform us about molecular and population genetic mechanisms that drive evolutionary change. They indicate how many evolutionary pathways are present in the landscape in which each successive mutational step results in increasing fitness. They also reveal patterns of interaction or epistasis among the mutant sites and whether particular combinations of mutants interact synergistically or antagonistically. Here we examine what has been accomplished already and what it means, but more importantly on what opportunities the approach has opened that have yet to be explored.

The experimental protocol

Given a relatively small number of mutations in the same or different genes that contribute to adaptive evolution, one could construct all possible combinations of the mutations and assay the contribution of each combination of mutants to the adaptation. If there are n genetic changes in the adaptation, with two choices for each, then there are 2^n different

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combinations. This set of mutations is said to be *combinatorially complete* [1,2••]. The usual experimental assay for level of adaptation is fitness or some proxy for fitness under specified environmental conditions. Proxies for fitness include growth rate, enzyme activity, and protein stability. In this context, one combination of mutants is regarded as superior to another if the combination increases organismal fitness. Among the $n!$ irreversible pathways (or trajectories) through 2^n combinations of n mutants, a pathway through the sequence space is considered permissible if and only if each step in the pathway increases organismal fitness. Typically, only a limited number of trajectories through sequence space is permissible [3–8••]. The mapping between genotypes and fitness (or a proxy for fitness) defines the *adaptive topography* for that set of mutants under the given set of conditions. The adaptive topography (or landscape) is a venerable metaphor in evolutionary genetics dating back to Haldane [9] and [10] (see Ref. [11] for review).

One great advantage of combinatorial completeness is that it uncovers the effect of each individual mutation when present in every possible genetic background and hence reveals quantitatively the extent of interaction between pairs, triplets, and higher-order combinations [1,2••]. The approach affords an opportunity to compare actual levels of gene interaction with predicted levels based on systems models of metabolism and reveals tradeoffs between enzyme kinetic parameters, protein stability, and other biochemical and biophysical properties [4,5,12]. Knowing the adaptive topography also enables computer simulations to estimate number and relative probabilities of different evolutionary trajectories [4].

The approach also has limitations. Although it enables estimation of growth rate, metabolic flux, enzyme activity, and other phenotypic characteristics to a high level of accuracy because of replication under controlled, reproducible conditions, the adaptive topography is defined only for that set of conditions and it is not in general known how robust adaptive topographies may be to changing environments. A second limitation is how many genotypes can be constructed and assayed with sufficient replication. For example, Salverda et al. [13] list 18 amino acid residues in TEM-1 β -lactamase at which one or more replacements have a measurable effect on antibiotic resistance in clinical isolates. A combinatorially complete set of these amino acid replacements would require analysis of a prohibitively large number of alleles. The large number of residues that can contribute to resistance in TEM-1 β -lactamase makes one wonder how an adaptive topography based on a small subset of such mutants might differ according to the TEM-1 sequence background. Nevertheless, some information can be gleaned from combinatorially incomplete data [13,14].

Combinatorially complete datasets

Experiments analyzing combinatorially complete sets of alleles have been summarized by Weinreich et al. [2••] about as well as they can be summarized, and there is no need to repeat their summary here. Suffice it to say that the experimental systems are diverse and include 3–7 genes or protein-coding sites (average 4.6). The systems include:

- 3 examples of metabolic enzymes or pathways — avian lysozyme [15], *Escherichia coli* isopropyl malate dehydrogenase [12,16], and *Solinaceae* sesquiterpine synthetase [17];

- 2 examples of other proteins — mammalian glucocorticoid receptor [18] and HIV glycoprotein [19];
- 3 examples of visible mutants — in *Drosophila melanogaster* [20], *Aspergillus niger* [21,22], and *Saccharomyces cerevisiae* [23];
- 2 examples of adaptations in experimental evolution — in *Metholobacterium extorquens* [24] and *E. coli* [14];
- 5 examples of drug targets — dihydrofolate reductase in *E. coli* [25], β -lactamase in *E. coli* [4,6], *Plasmodium falciparum* dihydrofolate reductase transgenes in *E. coli* [5], *P. falciparum* dihydrofolate reductase transgenes in *S. cerevisiae* [7,26,27], and *P. vivax* dihydrofolate reductase transgenes in *S. cerevisiae* and *E. coli* [28•].

From these 15 exemplars as well as other related experiments and observations, one can draw some inferences on the nature of evolution in complex systems. Some of the inferences are supported by numerous observations and are likely of general applicability, others are supported less well and should be considered tentative.

Inferences so far

The limited data so far available seem to support a number of far-reaching inferences. These are discussed in the following sections, grouped under several headings, but numbered consecutively.

Properties of adaptive landscapes

- 1 Negative pairwise epistasis between beneficial mutations entails a pattern of diminishing returns, in which favorable mutations brought together in combination are less fit than would be expected from their individual effects [24,29,30]. Recent evidence from yeast suggests that diminishing-returns epistasis is a genome-wide property of beneficial mutations [31••].
- 2 Negative pairwise epistasis for fitness arises because the mapping from biochemical and physiological traits to fitness is nearly always concave [12,14,16,24,32,33]. This pattern is observed experimentally and also one expected on theoretical grounds [29,34••,35]. If fitness is related to a metabolic flux that converges asymptotically to a plateau as a function of increasing enzyme activity, for example, then the fitness–activity curve is concave (Figure 1). The implication concavity is that, near the origin when fitness is low, the relation between activity and fitness is nearly linear, hence mutations that cause small differences in activity are approximately additive with respect to fitness, and there is negligible epistasis. Likewise on the plateau when fitness is high, but at this level even mutations with quite large effects on activity are approximately additive. On the shoulder between these extremes, however, the curvature implies nonadditive effects of activity on fitness, and mutations in this range are expected to show sign epistasis of the diminishing-returns type.

- 3 *Reciprocal sign epistasis*, in which single mutants each have a lower fitness than either the double mutant or wildtype, does occur [27,36] but is not pervasive among amino acid replacements [4,5,12,15–19]. The hedge “among amino acid replacements” is important because reciprocal sign epistasis is widespread in RNA molecules that form foldback structures because single mutants that disrupt base pairing in the stem have lower fitness than the double mutant that restores the ability to base pair. In one example of a plant RNA virus, more than half of all significant epistatic interactions were cases of reciprocal sign epistasis [37].
- 4 Because reciprocal sign epistasis is less prevalent among amino acid replacements than might be expected, fitness landscape can be rugged but are nearly always smoother than expected were fitness effects of single mutants and their combinations uncorrelated [11,21–23,25]. The fitness effects of alleles that share mutations are correlated for reasons similar to those that explain why offspring resemble their parents.

Adaptive evolutionary paths

- 5 The number of adaptive mutational paths through sequence space is limited and often a relatively small fraction of the theoretical possibilities [4–8••]. This is one of the most strongly supported conclusions among the studies carried out so far.
- 6 Adaptive pathways through sequence space are limited largely by *sign epistasis*, in which a path is inaccessible because one or more steps would entail a decrease in fitness [4,6,8••].
- 6 Adaptive reversions are possible in which a favorable substitution incorporated early in a pathway becomes unfavorable and is reversed at a later stage [8••,38], but see also Ref. [6]. Adaptive reversions allow indirect routes to attain fitness peaks that may not be directly accessible.
- 8 While the number of mutational paths through sequence space is constrained, there may nevertheless be enough alternative mutational pathways that the predictability and repeatability of evolutionary trajectories is limited [21].

Adaptive trade-offs

- 9 Evolutionary pathways often include compensatory mutations that mitigate unfavorable fitness interactions introduced at earlier stages [26,39].
- 10 The use of alternating antibiotics that have the same target can restore susceptibility to antibiotics after resistance has evolved. The antibiotics may be structurally similar as in the case of TEM β -lactamase [8] or structurally dissimilar as in alternate drugs targeting the chloroquine resistance transporter in *P. falciparum* as well alternate drugs targeting dihydroorotate dehydrogenase in *P. falciparum* [40••]. These results are based on laboratory experiments,

however clinical data on antibiotic resistance is so far consistent with evolutionary trajectories predicted from in vitro results [5,7,27].

- 11 Genetic recombination does little to speed adaptation [21–23]. This effect occurs owing to the recombinational breakdown of genotypes on fitness peaks, and it is most pronounced for relatively weak linkage. Theoretically, for tight linkage the situation is reversed [41•]. In principle, in genomes with tight physical linkage between strongly epistatic mutations, recombination allows the attainment of higher fitness peaks owing to the generation of combinations of mutations that may include individually deleterious mutations that enable jumping across fitness valleys [41•].

Next level challenges and opportunities

Despite the impressive list of inferences that have already emerged from combinatorially complete experiments, a number of important issues remain unresolved and some have barely been addressed. While far from exhaustive, the following list highlights some issues that seem to us to follow naturally from the pioneering work already done.

How important is higher-order epistasis? For a combinatorially complete set of n mutant sites or alleles, there are n main effects, $n(n-1)/2$ pairwise epistatic interactions, $n(n-1)(n-2)/3!$ three-way epistatic interactions and, in general, $\binom{n}{k}$ k -way epistatic interactions.

Evolutionary geneticists usually limit their considerations to main effects and pairwise interactions, however higher-order interactions ($k \geq 3$) might also be important if for no other reason than because there are so many of them. Weinreich et al. [2••] have estimated levels of higher-order epistasis using Walsh coefficients [42,43], which are linear combinations of fitness values that isolate the effect of each combination of mutants, averaged across all genetic backgrounds, in such a way that each epistatic contribution is independent of all others. For all of the combinatorially complete datasets described above, substantial levels of higher-order epistasis are observed [2••].

Some of the higher-order epistasis is due to the pervasiveness of diminishing-returns epistasis. In the fitness-activity relation in Figure 1, for example, suppose the red dot represents a nonmutant allele, the blue dot any of three single-mutants, the green dot any pairwise combination of the three single mutants, and the orange dot the three-way combination. In this situation, the pairwise and three-way values of epistasis based on Walsh coefficients have the same order of magnitude as the main effects of the alleles. The magnitude of the epistatic effects has to do mainly with the degree of curvature. The effect is smaller in the nearly linear portions of the curve when fitness is ascending or when it has plateaued.

A more traditional way to estimate higher-order epistasis would be through least squares, an approach that automatically tends to maximize the main and second-order effects and to minimize higher-order effects. When epistasis is estimated by means of least squares for the alleles in Figure 1, for example, the second- and third-order epistatic effects are an order of

magnitude smaller than the main effects. A limitation of this approach is that the different orders of epistasis are not independent as they are when using Walsh coefficients.

No matter how higher-order epistasis is estimated, however, the error variance of the estimates is in need of careful investigation. The variance of an estimate of a k -way epistatic

coefficient may include sums or differences of up to $\binom{n}{k}$ fitness estimates, hence its variance can substantially exceed the average variance of any one fitness estimate.. To the extent that the fitness estimates may be correlated, the variance of the higher-order epistasis may be inflated further.

There is likely no universally best way to measure epistasis, as the best measure of epistasis depends on why it is being measured. For example, one approach may be best for predicting long-term evolutionary outcomes, while another may be best for assessing the forces that drive short-term allele-frequency change in a heterogeneous population. There is even a case to be made for focusing qualitatively on fitness ranks instead of their quantitative values [44–46]. Some features of fitness landscapes, such as number of local fitness peaks and number of paths to any given peak, lend themselves to this approach. A qualitative approach commends itself because fitness ranks can often be determined more reliably than precise magnitudes. Figure 2 shows a fitness graph with three ordered sites in which red represents mutant sites. The arrows are oriented with the head pointing to the allele associated with the higher fitness. Starting with the all-blue allele, there are two (and only two) accessible paths to the maximum all-red allele, which are indicated by the red arrows. When quantitatively only diminishing returns epistasis occurs, then the mutants contribute additively to fitness rank and second- and higher-order epistasis disappears. For more complex assignments of fitness rank, second- and higher-order epistasis remains and can be estimated. Analysis of fitness by rank is therefore one way to identify epistatic interactions more complex than those of diminishing returns. The whole question of which is the best measure of second and higher-order epistasis for any specified purpose is rich in possibilities for theoretical analysis.

Are inferences from adaptive landscapes of fitness also valid for other traits? And how do adaptive landscapes of fitness related to lower-level cellular and molecular traits, especially the biochemistry and biophysics of proteins? Fitness is the quintessential higher-order trait, and perhaps landscapes of quantitative traits that are closer to the molecular and cellular level are smoother than those of fitness. This is the case for enzyme thermodynamic stability. Wylie and Shakhnovich [34••] have analyzed a model in which mutations of small effect contribute additively to thermodynamic instability whereas fitness depends on the fraction of molecules present in their folded state. The resulting fitness–stability curve is concave, and mutants affecting protein stability additively show negative epistasis for fitness.

How many other quantitative traits are more nearly additive when measured on an appropriate scale? This is an open question, but it is of critical importance for evaluating risk in complex diseases affected by multiple risk factors. What is the cumulative risk in

genomes that include multiple risk factors for hypertension? Type 2 diabetes? Bipolar disorder?

How do adaptive landscapes of fitness change with changing environments? And for antibiotics and other drugs, how do adaptive landscapes compare across related perturbagens? Little data of this sort exist among the combinatorially complete datasets, and even limited data exist outside combinatorial completeness that would allow the key issue to be addressed. One relevant example concerns beneficial mutations in a single-stranded DNA bacteriophage, in which negative pairwise epistasis maintained the same pattern across temperature but intensified as temperature increased [33]. Another concerns the manner in which driver antibiotic molecules favor evolutionary divergence of extended-spectrum beta-lactamases [47].

An especially interesting class of environmental agents are small molecules that perturb cellular metabolism (*perturbagens*), such as antibiotics. To what extent do patterns of second- and higher-order epistasis change across a series of chemically related antibiotics that have the same target and act in the same way (e.g., as competitive inhibitors)? Comprehensive data are available only for combinations of β -lactamase mutants when tested against different β -lactam antibiotics [6,8,13] and combinations of malaria-parasite dihydrofolate reductase mutants against two antimalarial antifolates [7,26,27]. More limited data pertain to paired inhibitors in which one drug is effective against the wildtype allele but not against mutants while the other is effective against mutant alleles but not against wildtype [40••]. These few examples seem to suggest that the adaptive landscape can change quite drastically even for chemically closely related perturbagens, however this conclusion may be misleading because of experimental bias. In all cases studied so far, the chemically related perturbagens were chosen for clinical use or experimental study precisely because the various forms were known to act differently on wildtype and mutant alleles of the drug target. What is needed to assess the robustness of fitness landscapes are studies of chemically related perturbagens that have been chosen with no foreknowledge of their effects on target alleles. Such studies are likely to be informative from the standpoint of molecular evolution and could be a valuable tool for drug discovery and deployment.

To what extent do cognate amino replacements in orthologous proteins exhibit similar evolutionary landscapes? Or, to put the question in another way, do orthologous proteins evolve resistance to antibiotics and other drugs through the same or similar amino acid replacements? These questions have hardly been explored [28] but are of some general interest in revealing whether orthologous proteins can be expected to evolve in parallel pathways when subjected to similar selection pressures. By *cognate amino acid replacement* we mean a mutation yielding the identical amino acid at corresponding positions in two or more orthologous proteins. The scarcity of experimental studies of this issue may reflect the fact that it is easy to reduce the questions to absurdity. On the other hand if one studies orthologs that are too different in sequence, then their folding pathways, intrinsically disordered regions, and active-site contacts may be so dissimilar that parallel evolutionary paths could hardly be expected. On the other hand, if one studies orthologs that are virtually identical in sequence, then parallel evolutionary paths are almost assured. The interesting question is at what level of divergence orthologs are still similar enough to be

unambiguously aligned but different enough that cognate mutants might have different biochemical or biophysical properties. The broader question is the extent to which the adaptive landscape is affected by differences in amino acid sequence that do not directly participate in substrate binding or catalytic activity, but may play an essential role in protein folding and the proper orientation of residues in and around the active site. The answer to this question would help in knowing when key resistance residues in one pathogenic species could be used for surveillance to detect emerging resistance in related pathogens, as well as in making best use of evolutionary principles in protein engineering [48•].

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Key terms

Adaptive topography	In three dimensions, a graph depicting fitness as a function of genotype or genotype frequencies, which often serves as a metaphor for a more complex fitness surface in many dimensions.
Cognate amino acid replacements	Substitution of identical amino acids at corresponding in one or more correctly aligned orthologous proteins.
Combinatorially complete set	All possible combinations of a group of mutant sites in a gene, or of mutant alleles of different genes.
Concave fitness function	A fitness function whose slope decreases continuously as a function of a genetic, metabolic, or physiological variable.
Diminishing returns epistasis	Interaction between mutant sites in a gene or between mutant alleles of different genes in which the effect of a combination of mutants is smaller than would be expected from their individual effects.
Epistasis	A term overburdened by history with multiple meanings. Originally defined to refer to a genetic interaction in which the phenotype due to one genetic locus conceals that due to another genetic locus, the term became broadened to mean any kind of genetic interaction affecting phenotype; then it was appropriated by statistical genetics to mean the component of variance attributable to gene interaction in an analysis of variance; and more recently re-appropriated to mean a set of equations describing how different genotypes interact quantitatively in affecting phenotype. Usually the reader has to infer from context which meaning the writer intends. Particularly vexing is the use of the term in different senses in the same paper and sometimes even in the same sentence.
Fitness landscape	See adaptive topography .
Higher-order epistasis	Interactions among three or more mutant sites in a gene, or among three or more mutant alleles in different genes.
Magnitude epistasis	For a pair of mutant alleles in regard to fitness, a situation in which the phenotypes of both single mutants are intermediate between the fitnesses of the nonmutant and the double mutant but not equal to each other.
Negative epistasis	Genetic interaction such that the phenotype of a combination of mutants is diminished from what would be expected from their individual effects.
Perturbagen	A small molecule, such as a drug, that interferes with metabolic or physiological processes; by extension, any small environmental change with similar effects.

Positive epistasis	Genetic interaction such that the phenotype of a combination of mutants is augmented over what would be expected from their individual effects.
Reciprocal sign epistasis	For a pair of mutant alleles in regard to fitness, a situation in which the fitness of each single mutant is smaller than the fitnesses of the nonmutant and the double mutant.
Sign epistasis	For a pair of mutant alleles in regard to fitness, a situation in which the fitness of one of the single mutants is smaller than the fitnesses of the nonmutant and the double mutant, with that of the other single mutant being intermediate.

Highlights

- Fitness landscapes can help in understanding constraints on evolutionary change
- Combinatorially complete data sets reveal patterns of higher-order fitness interactions
- Actual fitness landscapes are much smoother than random fitness landscapes
- Reciprocal sign epistasis can occur but is not pervasive
- Fitness landscapes open great opportunities for further research

Fig. 1.

Mapping of the activity of a hypothetical enzyme onto fitness. The model assumes that fitness is proportion to flux through a metabolic pathway when enzyme activity is limiting to flux according to simple Michaelis-Menten enzyme kinetics, and the curve is normalized to a fitness of 1 when activity equals 25. The colored dots correspond to fitness for wildtype (red), any of three single mutants (blue), any pair of double mutants (green), and the triple mutant (orange).

Fig. 2. Qualitative analysis of a fitness landscape with three mutant sites or genes (circles). Wildtype is symbolized by blue, mutant by red. Red arrows indicate pathways accessible from the nonmutant genotype (all blue) and blue arrows represent pathways that are inaccessible from this state. The fitness maximum is realized by the triple mutant, and there are two accessible pathways to this state from the double mutant.