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Conformational selection or induced-fit? A critical appraisal of the kinetic mechanism†

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Abstract

For almost five decades, two competing mechanisms of ligand recognition – conformational selection and induced-fit – have dominated our interpretation of ligand binding in biological macromolecules. When binding/dissociation events are fast compared to conformational transitions, the rate of approach to equilibrium, k_{obs} , becomes diagnostic of conformational selection or induced-fit based on whether it decreases or increases with the ligand concentration, [L]. However, this simple conclusion based on the rapid-equilibrium approximation is not valid in general. Here we show that conformational selection is associated with a rich repertoire of kinetic properties, with k_{obs} decreasing or increasing with [L] depending on the relative magnitude of the rate of ligand dissociation, k_{off} , and the rate of conformational isomerization, k_r . We prove that, even for the simplest two-step mechanism of ligand binding, a decrease of k_{obs} with [L] is unequivocal evidence of conformational selection, but an increase of k_{obs} with [L] is not unequivocal evidence of induced-fit. Ligand binding to glucokinase, thrombin and its precursor prethrombin-2 are used as relevant examples. We conclude that conformational selection as a mechanism for ligand binding to its target may be far more common than currently believed.

The specific encounter between a ligand and a host target is fundamental to the chemistry of all biological activities. Understanding the molecular mechanism of how ligands recognize their targets and how those interactions are regulated remains a central issue to biochemistry and biophysics and a critical prerequisite for our ability to rationally design effective drugs and new therapeutics (1). In its simplest incarnation, binding of ligand L to its biological target E can be cast in terms of the single step reaction scheme (2) where k_{on} ($M^{-1}s^{-1}$) is the second-order rate constant for ligand binding and k_{off} (s^{-1}) is the first-order rate of dissociation of the E:L complex into the parent species E and L. The strength of the interaction is quantified by the equilibrium association constant K_a (M^{-1}) defined as the ratio k_{on}/k_{off} , or equivalently by the equilibrium dissociation constant K_d (M) defined as the inverse of K_a or k_{off}/k_{on} . Scheme 1 provides an important starting point for any discussion of ligand binding, but offers little insight into the mechanism of recognition. Basically, the scheme assumes that the binding interaction is a rigid body collision between the ligand and its target, with no conformational change involved. In this case, the system approaches equilibrium according to an observed rate constant, k_{obs} , that increases linearly with [L]. The set of differential equations associated with Scheme 1 is in fact

$$\begin{pmatrix} d[E]/dt \\ d[E:L]/dt \end{pmatrix} = \begin{pmatrix} -k_{on}[L] & k_{off} \\ k_{on}[L] & -k_{off} \end{pmatrix} \begin{pmatrix} [E] \\ [E:L] \end{pmatrix} \quad (1)$$

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and the non-zero eigenvalue of the 2×2 matrix above gives the k_{obs} measured experimentally as

$$-\lambda_1 = k_{\text{obs}} = k_{\text{off}} + k_{\text{on}}[\text{L}] \quad (2)$$

A plot of k_{obs} vs $[\text{L}]$ is linear with intercept k_{off} and slope k_{on} , from which the value of the equilibrium association constant K_a or K_d can be easily derived.

Scheme 1 needs extension in the more realistic scenario of a binding interaction that involves conformational transitions. In this case, the rate of approach to equilibrium is no longer a linear function of $[\text{L}]$. Two limiting schemes become of interest as special cases of a more general scheme that links ligand binding to conformational transitions (3, 4), as shown in Figure 1. In the first case (Scheme 2), the target exists in distinct conformations in equilibrium and the ligand selects the one with optimal fit, i.e., The species E^* is added to reflect a pre-existing equilibrium between two forms, E^* and E , of which only E can interact with the ligand L . The rate constants k_r and k_{-r} refer to the transitions from E^* to E and backward, with the ratio $r = k_{-r}/k_r$ quantifying the population of E^* relative to E . This is the simplest form of the celebrated Monod-Wyman-Changeux model of allosteric transitions (5). In the second case (Scheme 3), the conformation of the target changes after ligand binding to provide an optimal fit, i.e., In this case, the rate constants k_r and k_{-r} refer to the transition from $\text{E}^*:\text{L}$ to $\text{E}:\text{L}$ and backward, with the ratio $r = k_{-r}/k_r$ quantifying the population of $\text{E}^*:\text{L}$ relative to $\text{E}:\text{L}$. Scheme 3 is the simplest form of the alternative Koshland-Nemethy-Filmer model of allosteric transitions (6) based on the induced-fit hypothesis (7). Schemes 2 and 3 have long been considered as mutually exclusive and distinguishing between them continues to dominate discussions in several systems of interest to biology and chemistry (4, 8–10).

Under the “rapid equilibrium approximation”, binding and dissociation steps in Schemes 2 and 3 are assumed to be fast compared to conformational changes (11, 12) and the dependence of k_{obs} on $[\text{L}]$ becomes diagnostic of the mechanism involved (Figure 1). In the case of Scheme 2, the k_{obs} *decreases* hyperbolically with $[\text{L}]$ according to the equation

$$k_{\text{obs}} = k_r + k_{-r} \frac{1}{1 + K_d[\text{L}]} = k_r + k_{-r} \frac{K_d}{K_d + [\text{L}]} \quad (3)$$

A plot of k_{obs} vs $[\text{L}]$ is an inverse hyperbola with asymptotic values of $k_{-r} + k_r$ for $[\text{L}] = 0$ and k_r for $[\text{L}] = \infty$. The mid-point between these values defines the equilibrium constant K_d . The dependence of k_{obs} on $[\text{L}]$ reflects the *decrease* in the number of species from two (E^* and E) to one (EL) as $[\text{L}]$ increases, with the rate of approach to equilibrium shifting from the reversible E^*-E interconversion at low $[\text{L}]$, with a value $k_{-r} + k_r$ to the irreversible E^* to E conversion at high $[\text{L}]$ (rate k_r). In the case of Scheme 3, the k_{obs} *increases* hyperbolically with $[\text{L}]$ according to the equation

$$k_{\text{obs}} = k_{-r} + k_r \frac{K_a[\text{L}]}{1 + K_a[\text{L}]} = k_{-r} + k_r \frac{[\text{L}]}{K_d + [\text{L}]} \quad (4)$$

A plot of k_{obs} vs $[\text{L}]$ is a rectangular hyperbola with asymptotic values of k_{-r} for $[\text{L}] = 0$ and $k_{-r} + k_r$ for $[\text{L}] = \infty$, and again the mid-point between these values defines the equilibrium constant K_d . In this case the dependence of k_{obs} on $[\text{L}]$ reflects the *increase* in the number of species from one (E^*) to two (E^*L and EL) as $[\text{L}]$ increases, with the rate of approach to equilibrium shifting from the irreversible EL to E^*L conversion at low $[\text{L}]$, with a value k_{-r} to the reversible $\text{E}^*\text{L}-\text{EL}$ interconversion at high $[\text{L}]$ (rate $k_{-r} + k_r$). The widely used rapid equilibrium approximation has fueled the notion that conformational selection (Scheme 2) and induced-fit (Scheme 3) can easily be distinguished from the kinetics of approach to

equilibrium (11). In turn, the preponderance of experimental systems found to obey eq 4 relative to eq 3 has been cited as evidence that induced-fit is the dominant mechanism of recognition in ligand binding to proteins (11, 13). In this study we analyze the kinetics of approach to equilibrium for Schemes 2 and 3 without simplifying assumptions on the rate constants and show how information on the mechanism of recognition can be extracted from the plot of k_{obs} vs $[L]$. Our analysis calls for caution in the use of the rapid equilibrium approximation in the analysis of experimental data.

Materials and Methods

Prethrombin-2 and thrombin were expressed in *E. coli* and purified from inclusion bodies, essentially as described (14, 15). Both proteins were expressed with the S195A substitution, which renders the protein catalytically inert while leaving its binding properties intact (16, 17). Stopped-flow fluorescence measurements were conducted on an Applied Photophysics SX20 spectrometer using 1:1 mixing in a total volume of 60 μL . For Na^+ , K^+ , FPR and VPR the intrinsic fluorescence of thrombin was monitored with an excitation wavelength of 283 nm and a cutoff filter of 305 nm. The active site inhibitor p-aminobenzamidine (PABA) has a strong fluorescence signal at 380 nm when excited at 330 nm and shows extraordinary sensitivity to its binding environment in the active site of trypsin-like proteases (18, 19), thus these experiments were conducted by exciting at 330 nm with a 375 nm cutoff filter, as described previously (19). Final thrombin concentrations were 50 nM (Na^+ binding), 75 nM (VPR and FPR binding), 100 nM (K^+ binding) and 1 μM (PABA binding). All thrombin binding experiments were conducted in the presence of 5 mM Tris, pH 8.0 at 15 $^{\circ}\text{C}$, 0.1 % PEG8000, with ionic strength maintained constant at 400 mM with choline chloride. Prethrombin-2 (75 nM) used essentially the same buffer with pH 8.0 at the temperature of interest. Individual kinetic traces were determined by averaging a minimum of four traces each from three independent ligand titrations. Traces were fit to a single exponential equation, with the quality of the fit determined by evaluation of the residuals. The k_{obs} values, taken from the single exponential fits, were plotted against the ligand concentration $[L]$ and these plots were used for all subsequent fitting to various kinetic schemes. Best-fit parameter values were derived by non-linear least squares with Mathematica.

Results

Consider Scheme 2 and the set of differential equations associated with it

$$\begin{pmatrix} d[E^*]/dt \\ d[E]/dt \\ d[E:L]/dt \end{pmatrix} = \begin{pmatrix} -k_r & k_{-r} & 0 \\ k_r & -k_{-r} - k_{\text{on}}[L] & k_{\text{off}} \\ 0 & k_{\text{on}}[L] & -k_{\text{off}} \end{pmatrix} \begin{pmatrix} [E^*] \\ [E] \\ [E:L] \end{pmatrix} \quad (5)$$

The two non-zero eigenvalues of the 3×3 matrix of kinetic rate constants are

$$-\lambda_{1,2} = \frac{k_{-r} + k_r + k_{\text{off}} + k_{\text{on}}[L] \pm \sqrt{(k_{\text{off}} + k_{\text{on}}[L] - k_{-r} - k_r)^2 + 4k_{-r}k_{\text{on}}[L]}}{2} \quad (6)$$

In the general case, when no assumption is made on the relative rates of binding and conformational transition, the kinetics of approach to equilibrium depend on two exponentials, each associated with an observed rate constant defined by the solutions of eq 5. The larger eigenvalue, $-\lambda_1$, defines a k_{obs} that becomes increasingly fast as $[L]$ increases. Detection of the contribution of this eigenvalue to the kinetics of approach to equilibrium may be difficult with standard transient kinetics and may require the use of ultra-rapid techniques like continuous flow and T-jump. The smaller eigenvalue, $-\lambda_2$, typically defines the evolution of the system over a time scale accessible to rapid kinetics technique like

stopped-flow. It is this eigenvalue that directly relates to the k_{obs} accessible to experimental measurements. Elementary rearrangements of eq 6 show that under the rapid equilibrium approximation, $k_{\text{off}} + k_{\text{on}}[L] \gg k_{-r} + k_r$, the larger eigenvalue $-\lambda_1$ is simply $k_{\text{off}} + k_{\text{on}}[L]$ and the smaller eigenvalue $-\lambda_2$ is given by eq 3 and decreases hyperbolically with $[L]$. We are interested in the behavior of eq 6 in the general case.

Consider how eq 6 depends on $[L]$ and especially its limiting values for $[L]=0$ and $[L]=\infty$ (Table 1). As $[L]$ increases, $-\lambda_1$ grows linearly as $k_{\text{on}}[L]$ but $-\lambda_2$ approaches the asymptotic value of k_r . The limit for $[L]=0$ depends on the difference $k_{\text{off}} - k_{-r} - k_r$. When the difference is positive ($k_{\text{off}} > k_{-r} + k_r$), then $-\lambda_1 = k_{\text{off}}$ and $-\lambda_2 = k_{-r} + k_r$. If the difference is negative ($k_{-r} + k_r > k_{\text{off}}$), then $-\lambda_1 = k_{-r} + k_r$ and $-\lambda_2 = k_{\text{off}}$. Basically, for $[L]=0$, $-\lambda_1$ and $-\lambda_2$ respectively assume the larger and smaller value between k_{off} and the sum $k_{-r} + k_r$. When k_{off} exceeds the sum $k_{-r} + k_r$, the situation is analogous to the rapid equilibrium approximation where $-\lambda_1 = k_{\text{off}} + k_{\text{on}}[L]$ and $-\lambda_2$ is given by eq 3. However, when $k_{-r} + k_r$ exceeds k_{off} , the kinetics become dependent on the relative magnitude of k_{off} and k_r . When $k_{\text{off}} > k_r$ the value of $-\lambda_2 = k_{\text{obs}}$ decreases with $[L]$. Although this situation is analogous to the case $k_{\text{off}} > k_{-r} + k_r$, there is an important distinction insofar as the asymptotic value for $[L]=0$ does not give $k_{-r} + k_r$ as in the rapid equilibrium approximation but k_{off} . Hence, when $k_{-r} + k_r > k_{\text{off}} > k_r$, Scheme 2 produces a dependence of k_{obs} vs $[L]$ that can be mistaken with that observed under the rapid equilibrium approximation (Figure 2), with the asymptotic value of k_{obs} for $[L]=0$ becoming incorrectly assigned as the sum $k_{-r} + k_r$ instead of k_{off} . It also follows from inspection of eq 6 that the value of $-\lambda_2 = k_{\text{obs}}$ does not change with $[L]$ when $k_{\text{off}} = k_r$ (Figure 2). The lack of dependence of k_{obs} on $[L]$ was originally reported in the first rapid kinetics study of Na^+ binding to thrombin (20) and interpreted in terms of an extended version of Scheme 2. It is now clear that Scheme 2 used in its general form easily accounts for a value of k_{obs} that is independent of $[L]$ and no extension is necessary. Finally, when $k_{\text{off}} < k_r$ the value of $-\lambda_2 = k_{\text{obs}}$ actually increases with $[L]$ and mimics the dependence observed in the case of induced-fit (Figures 1 and 2). In the general case, conformational selection (Scheme 2) produces a gamut of kinetic properties that include those uniquely pertaining to induced-fit (Scheme 3) under the assumption of rapid equilibrium.

Unlike Scheme 2, Scheme 3 always produces eigenvalues that increase with $[L]$. Scheme 3 is associated with the set of differential equations

$$\begin{pmatrix} d[E^*]/dt \\ d[E^*:L]/dt \\ d[E:L]/dt \end{pmatrix} = \begin{pmatrix} -k_{\text{on}}[L] & k_{\text{off}} & 0 \\ k_{\text{on}}[L] & -k_r - k_{\text{off}} & k_{-r} \\ 0 & k_r & -k_{-r} \end{pmatrix} \begin{pmatrix} [E^*] \\ [E^*:L] \\ [E:L] \end{pmatrix} \quad (7)$$

The two non-zero eigenvalues associated with the 3×3 matrix of kinetic rate constants are

$$-\lambda_{1,2} = \frac{k_{-r} + k_r + k_{\text{off}} + k_{\text{on}}[L] \pm \sqrt{(k_{\text{off}} + k_{\text{on}}[L] - k_{-r} - k_r)^2 + 4k_r k_{\text{off}}}}{2} \quad (8)$$

There is a basic similarity between eqs 6 and 8, that only differ in the last term under the square root expression. However, this difference results in two eigenvalues that always increase with $[L]$. Unlike Scheme 2, there is no finite value of the rate constants in Scheme 3 that makes $-\lambda_2$ independent of $[L]$. As $[L]$ increases, $-\lambda_1$ grows linearly as $k_{\text{on}}[L]$ as in the case of Scheme 2, but $-\lambda_2$ approaches the asymptotic value of $k_{-r} + k_r$. The limit for $[L]=0$ does not depend on the relative values of k_{off} and the sum $k_{-r} + k_r$ (Table 1) as in Scheme 2 and is always less than the value reached for $[L]=\infty$. This implies that Scheme 3 always produces values of k_{obs} that increase with $[L]$, as opposed to Scheme 2 that produces values of k_{obs} that decrease, increase or are independent of $[L]$ depending on the relative values of k_{off} and k_r .

A plot of k_{obs} decreasing with $[L]$ or independent of $[L]$ is unambiguous proof of conformational selection (Scheme 2), but a plot of k_{obs} increasing with $[L]$ may also be associated with conformational selection (Figure 2) and cannot be considered unambiguous proof of induced-fit (Scheme 3). Glucokinase illustrates this scenario directly. The enzyme was originally assumed to bind glucose at a single site according to induced-fit (21) based on the analysis of rapid kinetics data where both the larger and smaller eigenvalues were resolved experimentally (Figure 3). The larger eigenvalue produces a k_{obs} that increases linearly with $[L]$ and the smaller eigenvalue shows a hyperbolic increase with $[L]$ as expected of Scheme 3 under the rapid equilibrium approximation. However, the data in Figure 3 cannot be considered unequivocal evidence of induced-fit because they fit accurately to Scheme 2 without the rapid equilibrium approximation with values of the rate constants $k_{-f}=7.16 \text{ s}^{-1}$, $k_f=0.8 \text{ s}^{-1}$, $k_{\text{off}}=0.34 \text{ s}^{-1}$ and $k_{\text{on}}=540 \text{ M}^{-1}\text{s}^{-1}$. It comes as no surprise, then, that more recent kinetic measurements of glucose binding to glucokinase support conformational selection over induced-fit (22) and it is now accepted that glucokinase exists in alternative conformations in equilibrium prior to the binding of any ligands (23). This conclusion is strongly supported by recent X-ray structures of glucokinase that reveal how ligand binding does not result in conformational changes of the enzyme but only in stabilization of the E form (24).

Figure 4 shows the values of k_{obs} as a function of $[L]$ for the case of different ligands binding to the clotting protease thrombin (25). The active site inhibitor PABA shows an inverse hyperbolic dependence of k_{obs} vs $[L]$ conforming to conformational selection according to Scheme 2. Under the rapid equilibrium approximation for PABA binding, analysis of the data in Figure 2 gives values of $k_f=74 \text{ s}^{-1}$ and $k_{-f}=344 \text{ s}^{-1}$ for the E*-E interconversion, along with a value of $K_d=53 \text{ }\mu\text{M}$ for the equilibrium association constant, that translates into a value of $K_{d,\text{app}}=K_d(1+r)=300 \text{ }\mu\text{M}$ in agreement with equilibrium titration measurements (18). The kinetic features of PABA binding to thrombin show evidence of the E*-E equilibrium in the free form of the enzyme. As for glucokinase, this conclusion is directly supported by X-ray structural data (19). Thrombin crystallizes in the free form in two alternative conformations, one (E form) with the active site open and accessible to substrates and inhibitors like PABA, and the other (E* form) with the active site occluded by a collapse of the 215–217 segment that precludes binding of substrates or inhibitors like PABA. The E* and E forms have been detected crystallographically in the same protein construct for several thrombin mutants (19), as well in numerous other members of the trypsin family (26). Indeed, conformational selection is the dominant mechanism of ligand recognition in this large family of biologically important enzymes (10).

Because the E*-E equilibrium exists in solution independent of any binding event, its presence should be detected with exactly the same kinetic signatures regardless of the ligand under study. Specifically, different ligands influenced directly by the E*-E equilibrium should produce the same dependence of k_{obs} on $[L]$ as seen for PABA (Figure 4), with identical asymptotic values for $[L]=0$ and $[L]=\infty$. A key property of thrombin is its ability to bind monovalent cations like Na^+ and K^+ to a site near the primary specificity pocket that is obliterated by the repositioning of an Arg side chain when the enzyme switches from the E to the E* form (25). Consistent with the scenario supported by structural data, binding of K^+ produces a dependence of k_{obs} on $[L]$ that closely resembles that observed for PABA (Figure 4), thereby supporting the conclusion that the asymptotic values of k_{obs} for $[L]=0$ and $[L]=\infty$ reflect the properties of the E*-E interconversion. However, binding of Na^+ deviates from K^+ and PABA, especially in the asymptotic value of k_{obs} for $[L]=0$ that defines the value of k_f+k_{-f} (Table 1). Why do K^+ and Na^+ produce different asymptotic values of k_{obs} for $[L]=0$ if they bind to the same site (27, 28) and according to the same kinetic mechanism? A fourth ligand, the chromogenic substrate VPR binding to the active site like PABA, produces a dependence of k_{obs} on $[L]$ that departs even more drastically

from the profile seen for PABA and K^+ (Figure 4). In this case, the value of k_{obs} actually increases with $[L]$. The properties of Scheme 2 in the general case rationalize the seemingly disparate behavior observed in the binding of different ligands to thrombin (Figure 4). Binding of PABA, Na^+ and K^+ is consistent with the E^* -E equilibrium, with only E enabling binding at the active site and the cation binding site, as indicated by structural biology (19). For all ligands, the value of k_{obs} levels off around 70 s^{-1} at high $[L]$ and increases to 400 s^{-1} for $[L]=0$ for PABA and K^+ , and 130 s^{-1} for Na^+ . When k_{obs} decreases with $[L]$, the value for $[L]=0$ always measures whichever is smaller between k_{off} and the sum $k_{-r}+k_r$ (Table 1). Hence, the value of 130 s^{-1} measured for Na^+ binding at $[L]=0$ should not be assigned to $k_{-r}+k_r$ but to k_{off} for Na^+ dissociation, and the value of 400 s^{-1} measured for PABA and K^+ binding is most likely the sum $k_{-r}+k_r$. These values enable assignment of $k_r=70\text{ s}^{-1}$ and $k_{-r}=340\text{ s}^{-1}$ (Table 2), making the E^* form 5-fold more populated than E under the experimental conditions of the rapid kinetics measurements. Assignment of the asymptotic value of k_{obs} at $[L]=0$ for Na^+ binding as the sum $k_{-r}+k_r$ would give values of $k_r=60\text{ s}^{-1}$ and $k_{-r}=67\text{ s}^{-1}$, thereby making E^* and E equally populated. This is the conclusion drawn in previous studies where the value of k_{obs} for $[L]=0$ was interpreted as k_r+k_{-r} under the assumption of rapid equilibrium for Na^+ binding (19, 29, 30). The analysis presented here demonstrates that previous studies have underestimated the contribution of E^* and supports the need for measurements involving different ligands, under the same solution conditions, to fully explore the range of k_{obs} values in the limits $[L]=0$ and $[L]=\infty$ when the larger eigenvalue is not accessible to experimental measurements. Once the values of k_r and k_{-r} are assigned from measurements of PABA and K^+ binding, all other rate constants in eq 6 can be assigned for Na^+ (Table 2). The value of $k_{on}=3.4\cdot 10^4\text{ M}^{-1}\text{ s}^{-1}$ is in agreement with that determined from continuous flow ultra-rapid kinetics (31) and the value of $K_{d,app}=K_d(1+r)=27\text{ mM}$ agrees with equilibrium titrations of Na^+ binding (32, 33). In the case of the chromogenic substrate VPR, the value of k_{obs} at high $[L]$ levels off around 70 s^{-1} , again in keeping with the rate for the E^* to E transition k_r , but the dependence of k_{obs} is drastically different and shows an increase with $[L]$. This behavior could be easily interpreted in terms of an induced-fit under the rapid equilibrium approximation. On the other hand, Scheme 2 offers an alternative explanation in terms of conformational selection with k_{off} much smaller than k_r , resulting in values of $k_{on}=1.7\cdot 10^7\text{ M}^{-1}\text{ s}^{-1}$ and $K_{d,app}=K_d(1+r)=0.75\text{ }\mu\text{M}$ consistent with previous kinetic (34) and equilibrium (17) measurements. Binding of four different ligands (PABA, K^+ , Na^+ and VPR) to thrombin support the same mechanism of conformational selection, even though the kinetic signatures differ drastically in the four cases.

Screening multiple ligands is a specific example of the more general strategy of altering the relative rates of k_r and k_{off} to differentiate between potential mechanisms and detect signatures of conformational selection. Perturbations that alter the values of k_{off} relative to k_r for the same ligand produce similar results. We demonstrate this principle with prethrombin-2 (15), an inactive zymogen precursor of thrombin, binding to the chromogenic substrate FPR at different temperatures. Because temperature may affect the values of k_{off} and k_r to different extent, it may be ideally suited to detect drastic changes in the dependence of k_{obs} vs $[L]$. At $15\text{ }^\circ\text{C}$, FPR binding displays the same hyperbolically increasing dependence of k_{obs} on $[L]$ seen with VPR in thrombin, with asymptotes of 45 s^{-1} at $[L]=0$ and 156 s^{-1} at $[L]=\infty$. Both the $[L]=0$ and the $[L]=\infty$ asymptotes, reflecting k_{off} and k_r respectively, increase with temperature but to different extent. At $25\text{ }^\circ\text{C}$, the asymptotes increase to 142 s^{-1} and 255 s^{-1} in the limits of $[L]=0$ and $[L]=\infty$. However, at $35\text{ }^\circ\text{C}$, k_{off} becomes at least 550 s^{-1} and faster than k_r (365 s^{-1}) causing the dependence of k_{obs} on $[L]$ to invert and decrease hyperbolically with $[L]$ (Figure 4). Under the rapid equilibrium approximation, this type of behavior could only be explained by the mechanism of binding switching from induced-fit at or below $25\text{ }^\circ\text{C}$ to conformational selection at $35\text{ }^\circ\text{C}$, a very unrealistic scenario. On the other hand, Scheme 2 in the general case explains the

binding of FPR to prethrombin-2 with a single mechanism, conformational selection, with the dependence of k_{obs} on $[L]$ changing drastically based on the relative values of k_r and k_{off} at different temperatures, in keeping with the simulations reported in Figure 2. Hence, conformational selection not only applies to the mature enzyme thrombin, but also to its inactive precursor prethrombin-2, thereby confirming kinetically well established results from structural biology for thrombin (15) and trypsin-like proteases in general (10, 26).

Discussion

A previous study by Galletto et al. (35) merged the mechanisms in Schemes 2 and 3 to produce a three-step scheme of ligand binding where a pre-existing equilibrium is followed by ligand-induced conformational changes. Because of the algebraic complexity of the expressions involved, the properties of such scheme were analyzed under separation of time scales. Important conclusions were reached about the dependence of k_{obs} on $[L]$ and how the extended scheme would account for kinetic properties often associated with induced-fit. A more recent study by Hammes et al. (4) offered a description of Schemes 2 and 3 in terms of fluxes along selected pathways of a more general scheme encompassing conformational transitions and ligand binding (Figure 1). A continuum version of that scheme has been discussed by Zhou (9). Again, a richer repertoire of kinetic properties was identified for conformational selection. Our study reveals the kinetic properties of Schemes 2 and 3 and derives mathematical expressions to extract rate constants from the analysis of experimental data. Conformational selection is shown to produce kinetic properties such as an increase of k_{obs} with $[L]$ that overlap with those of induced-fit, even though no such mechanism is present in Scheme 2. On the other hand, induced-fit (Scheme 3) is unable of kinetic properties pertaining uniquely to conformational selection, i.e., a k_{obs} decreasing with $[L]$ or independent of $[L]$.

When the rapid equilibrium approximation is invoked, both Scheme 2 and 3 depend on three independent parameters (eqs 3 and 4) that can be resolved from a plot of k_{obs} vs $[L]$. If the approximation is not used, both schemes depend on four independent rate constants but the plot of k_{obs} vs $[L]$ only contains information on three independent variables, i.e., the asymptotic values at $[L]=0$ and $[L]=\infty$ and the mid-point of the transition. In this case, it is not possible to unequivocally resolve all the independent rate constants k_r , k_{-r} , k_{on} and k_{off} . The value of k_r for Scheme 2 is always defined by k_{obs} for large $[L]$, but the value at $[L]=0$ is the smaller between k_r+k_{-r} and k_{off} . The mid-point of the transition is not necessarily related to K_d . The situation is even more complex in the case of Scheme 3 where the value of k_{obs} for $[L]$ large is k_r+k_{-r} , but the value for $[L]=0$ depends on three rate constants (Table 1) and again the mid-point of the transition does not depend only on K_d . Determination of all four independent rate constants is always possible when both the larger and smaller eigenvalues are accessed experimentally, as shown in the case of glucokinase (Figure 3). However, this approach may not be feasible in general. Use of different ligands binding with different rate constants becomes essential, as shown in the present study for thrombin. Although the approach in the general case may fail to provide the exact magnitude of the rate constants involved in the scheme, it is nonetheless instrumental in avoiding potentially incorrect conclusions based on the rapid equilibrium approximation. Particularly important is the need to assign the mechanism of binding when k_{obs} increases with $[L]$, which cannot be linked unambiguously to induced-fit as shown by our analysis and previous work (4, 35). In a recent review, Tummino and Copeland pointed out that induced-fit is by far the most common mechanism of recognition documented experimentally, with conformational selection being confined to a handful of cases (11). This conclusion was based on the results of kinetics analyzed under the rapid equilibrium approximation. Conformational selection can explain an increase of k_{obs} with $[L]$ commonly assigned to induced-fit, but induced-fit can never account for a decrease of k_{obs} with $[L]$ that unequivocally identifies

conformational selection. We therefore suspect that the preponderance of induced-fit as a mechanism of ligand binding needs to be critically reconsidered. Indeed, several proteins like alkaline phosphatase (36), chymotrypsin (12, 37), thrombin (20, 29), meizothrombin-desF1 (38), glucokinase (22), trypsin (39), the immunoglobulin IgE (40), clotting proteases factor Xa and activated protein C (30) obey conformational selection, and so does DNA in its B to Z transition (41). Structural biology offers unequivocal evidence of multiple conformations in pre-existing equilibrium for maltose-binding protein (42), trypsin-like proteases in general (10, 26) and RNA (43).

Our work offers a clear explanation for the apparent infrequency of conformational selection (11). There is a lower limit on the equilibrium dissociation constant K_d where the characteristic inverse hyperbola of conformational selection will be detectable. As discussed earlier, the strength of a ligand binding interaction is controlled by the interplay between k_{on} and k_{off} rates, with the diffusion limit setting the upper bound for k_{on} at around $6.5 \cdot 10^8 \text{ M}^{-1}\text{s}^{-1}$ (44). Because k_{on} is limited and k_{off} must exceed k_r for conformational selection to be detected, only ligands binding with

$$K_d > \frac{k_r}{k_{on}} \quad (9)$$

would produce a plot of k_{obs} that decreases hyperbolically with [L]. If the value of k_r is in the range of 100 s^{-1} , conformational selection can only be detected for values of $K_d > 150 \text{ nM}$, provided the ligand binds at the diffusion-limited rate. Thus, not only is sampling multiple ligands important to establishing the kinetic mechanism of binding, but experiments should be designed to sample conditions where ligand binding is relatively weak.

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Abbreviations used

FPR	H-D-Phe-Pro-Arg-p-nitroanilide
PABA	p-aminobenzamidine
PEG	polyethyleneglycol
VPR	H-D-Val-Pro-Arg-p-nitroanilide

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Figure 1. Conformational selection and induced-fit

The two alternative mechanisms of ligand recognition in Schemes 2 (left) and 3 (right) show the different role of conformational transitions in the binding process. The two schemes are special cases of a general scheme (middle) linking conformational changes to ligand binding. Conformational selection (derived from the pathway at the bottom left in the general scheme) postulates a pre-existing equilibrium between the E^* and E forms, of which only E binds the ligand. Under the rapid equilibrium approximation, the rate of approach to equilibrium, k_{obs} , is an inverse hyperbolic function of the ligand concentration from which the values of k_r and k_{-r} for the E^* - E interconversion can be derived directly, along with the value of K_d for ligand binding. In this mechanism, the value of k_{obs} decreases with increasing ligand concentration. The induced-fit model (derived from the pathway at the top right in the general scheme) postulates a conformational transition between E^*L and EL that optimizes binding. Under the rapid equilibrium approximation, the rate of approach to equilibrium, k_{obs} , is an hyperbolic function of the ligand concentration from which the values of k_r and k_{-r} for the E^*L - EL interconversion can be derived directly, along with the value of K_d for ligand binding. In this mechanism, the value of k_{obs} increases with increasing ligand concentration. Hence, under the rapid equilibrium approximation, the

dependence of k_{obs} on the ligand concentration $[L]$ is diagnostic of the mechanism of binding.

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Figure 2. Dependence of k_{obs} on $[L]$ for conformational selection

The eigenvalues $-\lambda_1$ (A) and $-\lambda_2$ (B) were simulated according to eq 6 in the text, with rate constants $k_f=50 \text{ s}^{-1}$, $k_r=150 \text{ s}^{-1}$, and $k_{\text{on}}=10^6 \text{ M}^{-1} \text{ s}^{-1}$ fixed and k_{off} varied between 300 s^{-1} (solid line), 100 s^{-1} (dashed line), 50 s^{-1} (dashed-dotted line) and 10 s^{-1} (dotted line). When $k_{\text{off}} > k_f + k_r$ (solid line) the asymptotes of the curves in (A) and (B) are equivalent to those of eq 2 and eq 3, respectively, under the rapid equilibrium approximation. However, when $k_f + k_r > k_{\text{off}} > k_f$ (dashed line) the values of $-\lambda_1$ and $-\lambda_2$ in the limit of $[L]=0$ switch, with $k_f + k_r$ defining the lower limit of $-\lambda_1$ and k_{off} defining the lower limit of $-\lambda_2$ (Table 1). When $k_{\text{off}} > k_f$ (solid line and dashed line) the inverse hyperbola traditionally associated with conformational selection is retained and the curve will look essentially the same as predicted from eq 3. Importantly, when $k_f > k_{\text{off}}$ (dotted line) the value of $-\lambda_2$ actually increases with ligand concentration, mimicking the behavior observed under the induced-fit mechanism (see Figure 1). The transition between the opposite dependences of k_{obs} vs $[L]$ is observed for $k_f = k_{\text{off}}$ (dashed-dotted line) where k_{obs} is finite but independent of the ligand concentration.

Figure 3. Rapid kinetics of glucose binding to glucokinase

Data were taken from ref (21) and analyzed as in the original report according to the induced-fit mechanism (grey discontinuous lines) under the rapid equilibrium approximation (eqs 2 and 3 in the text) with best-fit parameter values: $k_{\text{on}}=530\pm30\text{ M}^{-1}\text{s}^{-1}$, $k_{\text{off}}=7.9\pm0.6\text{ s}^{-1}$, $k_{\text{r}}=0.45\pm0.03\text{ s}^{-1}$ and $k_{\text{-r}}=0.29\pm0.03\text{ s}^{-1}$. These values are practically identical to those published by Heredia et al. (21). However, the same data can be fit according to the conformational selection mechanism (black lines) in the general case (eqs 5 and 6 in the text) with best-fit parameter values: $k_{\text{on}}=540\pm30\text{ M}^{-1}\text{s}^{-1}$, $k_{\text{off}}=0.34\pm0.03\text{ s}^{-1}$, $k_{\text{r}}=0.80\pm0.06\text{ s}^{-1}$ and $k_{\text{-r}}=7.2\pm0.3\text{ s}^{-1}$. Although the fits are equivalent in the two cases, they produce a very different description of the glucokinase-glucose interaction. The value of $K_{\text{d,app}}$ (Table 2) is similar in the two cases (9.1 vs 6.3 mM), but the values of K_{d} reflecting the intrinsic binding affinity of glucose for glucokinase are 15 mM in the case of induced-fit and 0.63 mM in the case of conformational selection. Induced-fit predicts a weak binding interaction of glucose to glucokinase that is modestly strengthened by conformational rearrangements of the initial complex. On the other hand, conformational selection predicts tighter binding of glucose to the E form of glucokinase with the resulting apparent affinity weakened by the significant population of E*.

Figure 4. Rapid kinetics of ligand binding to thrombin

(A) Rate of approach to equilibrium, k_{obs} , determined from stopped-flow fluorescence measurements of PABA (red), KCl (magenta), NaCl (cyan), and VPR (orange) binding to thrombin, under experimental conditions of 5 mM Tris, 0.1% PEG8000, pH 8.0, at 15 °C. The KCl and NaCl concentrations were changed by keeping the ionic strength constant at 400 mM with choline chloride, which was also used in the buffers for PABA and VPR. Continuous lines were drawn according to eq 3 (PABA and K⁺) or eq 6 (Na⁺ and VPR), as described in methods, with best-fit parameter values listed in Table 2. In all cases, the asymptotic value of k_{obs} for large [L], k_r , levels off around 70 s⁻¹. On the other hand, the value of k_{obs} for [L]=0 changes for different ligands and measures the sum k_r+k_{-r} (PABA and K⁺) or the value of k_{off} for ligand dissociation that exceeds (Na⁺) or remains below (VPR) k_r . To facilitate comparison, the values of [L] for each ligand are expressed as a percentage of the maximum concentration used. (B) Rate of approach to equilibrium, k_{obs} , determined from stopped-flow fluorescence measurements of FPR binding to prethrombin-2 at 15 °C (red), 25 °C (cyan), and 35 °C (magenta), under experimental conditions of 5 mM Tris, 400 mM choline chloride, 0.1% PEG8000, pH 8.0. The contrast in the dependence of k_{obs} on [L] between 15–25 °C (increase) and 35 °C (decrease) is easily explained by a temperature change in k_{off} that exceeds that of k_r (see also the simulation in Figure 2). Use of Scheme 2 in the general case, however, prevents resolution of the four independent parameters in eq 6 at each temperature, although it provides an excellent fit of the data (continuous lines) when the values of k_{on} is arbitrarily fixed to 10⁷ M⁻¹s⁻¹.

SCHEME 1.

SCHEME 2.

SCHEME 3.

Table 1

Kinetic signatures of conformational selection and induced-fit in the general case

	Conformational selection (Scheme 2)		Induced-fit (Scheme 3)
$-\lambda_{1,2}$	$\frac{k_{-r}+k_r+k_{\text{off}}+k_{\text{on}}[\text{L}] \pm \sqrt{(k_{\text{off}}+k_{\text{on}}[\text{L}] - k_{-r} - k_r)^2 + 4k_{-r}k_{\text{on}}[\text{L}]}}{2}$		$\frac{k_{-r}+k_r+k_{\text{off}}+k_{\text{on}}[\text{L}] \pm \sqrt{(k_{\text{off}}+k_{\text{on}}[\text{L}] - k_{-r} - k_r)^2 + 4k_rk_{\text{off}}}}{2}$
	$k_{\text{off}} > k_{-r} + k_r$	$k_{\text{off}} < k_{-r} + k_r$	
$-\lambda_1 ([\text{L}]=0)$	k_{off}	$k_{-r} + k_r$	$\frac{k_{-r}+k_r+k_{\text{off}} + \sqrt{(k_{\text{off}} - k_{-r} - k_r)^2 + 4k_rk_{\text{off}}}}{2}$
$-\lambda_1 ([\text{L}]=\infty)$	$k_{\text{on}}[\text{L}]$	$k_{\text{on}}[\text{L}]$	$k_{\text{on}}[\text{L}]$
$-\lambda_2 ([\text{L}]=0)$	$k_{-r} + k_r$	k_{off}	$\frac{k_{-r}+k_r+k_{\text{off}} - \sqrt{(k_{\text{off}} - k_{-r} - k_r)^2 + 4k_rk_{\text{off}}}}{2} < k_{-r} + k_r$
$-\lambda_2 ([\text{L}]=\infty)$	k_r	k_r	$k_{-r} + k_r$
$k_{\text{obs}} = -\lambda_2$	Always decreases with [L]	Decreases ($k_{\text{off}} > k_r$) or increases ($k_{\text{off}} < k_r$) with [L]	Always increases with [L]
$K_{d,\text{app}}^*$	$\frac{[\text{E}^*] + [\text{E}]}{[\text{EL}]} = \frac{k_{\text{off}}}{k_{\text{on}}} \left(\frac{k_r + k_{-r}}{k_r} \right) = K_d(1+r)$		$\frac{[\text{E}]}{[\text{E}^*:\text{L}] + [\text{E}:\text{L}]} = \frac{k_{\text{off}}}{k_{\text{on}}} \left(\frac{k_r}{k_r + k_{-r}} \right) = K_d \left(\frac{1}{1+r} \right)$

* $K_{d,\text{app}}$ is the only parameter accessible to experimental measurements of the system at equilibrium (29). Its value depends on the intrinsic K_d and the ratio $r = k_{-r}/k_r$ for both Schemes 2 and 3. Because two independent parameters, K_d and r , cannot be resolved from the single independent parameter, $K_{d,\text{app}}$, measurements of ligand binding at equilibrium cannot be used to distinguish between conformational selection or induced-fit.

Table 2

Kinetic parameters for ligand binding to thrombin

Ligand	k_{on} ($M^{-1}s^{-1}$)	k_{off} (s^{-1})	k_r (s^{-1})	k_{-r} (s^{-1})	K_d (M)	r	K_{dapp} (M)
PABA	N.D.	N.D.	70 $\pm$ 10	340 $\pm$ 10	5.2 $\pm$ 0.8 10^{-6}	4.9 $\pm$ 0.6	2.9 $\pm$ 0.4 10^{-4}
Na ⁺	3.2 $\pm$ 0.3 10^4	130 $\pm$ 20	60 $\pm$ 10	340 $\pm$ 10	4.1 $\pm$ 0.4 10^{-3}	5.7 $\pm$ 0.7	27 $\pm$ 4 10^{-3}
K ⁺	N.D.	N.D.	60 $\pm$ 10	340 $\pm$ 10	19 $\pm$ 2 10^{-3}	5.7 $\pm$ 0.7	130 $\pm$ 10 10^{-3}
VPR	1.7 $\pm$ 0.1 10^7	2.4 $\pm$ 0.2	80 $\pm$ 10	340 $\pm$ 10	1.4 $\pm$ 0.1 10^{-7}	4.3 $\pm$ 0.7	7.5 $\pm$ 0.8 10^{-7}