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Mechanism of Magnetic Relaxation Switching Sensing

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Abstract

Magnetic relaxation switching (MRSw) assays that employ target-induced aggregation (or disaggregation) of magnetic nanoparticles (MNPs) can be used to detect a wide range of biomolecules. The precise working mechanisms, however, remain poorly understood, often leading to confounding interpretation. We herein present a systematic and comprehensive characterization of MRSw sensing. By using different types of MNPs with varying physical properties, we analyzed the nature and transverse relaxation modes for MRSw detection. The study found that clustered MNPs are universally in a diffusion-limited fractal state (dimension of ~2.4). Importantly, a new model for transverse relaxation was constructed, that accurately recapitulates observed MRSw phenomena, and predicts the MRSw detection sensitivities and dynamic ranges.

Keywords

Magnetic Relaxation Switching; Magnetic Nanoparticles; NMR; Biosensors

The advance of nanoparticles has significantly accelerated the development of new, highly sensitive biosensors that have broad applications in basic biomedical research, drug discovery, and clinical diagnostics.¹⁻³ With their size scale often similar to those of biological molecules, nanoparticles can efficiently bind to target biomarkers, generating distinctive and amplified analytical signals.⁴ Magnetic nanoparticles (MNPs) in particular offer an attractive sensing mechanism.^{5, 6} Owing to the intrinsically low magnetic susceptibility of biological media, MNPs can achieve high “contrast” even in complex biological specimens with little interference from biological background.

We have previously developed a MNP-based sensing methodology for water-soluble biomarkers.^{7, 8} The approach is based on the phenomenon of magnetic relaxation switching (MRSw) as a sensing mechanism; when MNPs cross-link upon the recognition and binding of biological targets, these clustered particles change the transverse (R_2) relaxation of water protons, which can be detected by nuclear magnetic resonance (NMR; **Scheme 1**). Alternatively, the assay can be performed in reverse mode, where enzymatic cleavage or

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Supporting Information Available

Additional data from MRSw assays using DNA molecules and mathematical models describing MRSw assays for different types of MNPs are summarized in the Supporting Information. This material is available free of charge *via* the internet at <http://pubs.acs.org>.

competitive binding of molecular targets disassembles preformed clusters. The assay is ideally suited for detecting small biological targets; the formation of MNP clusters is most efficient when size of the detection targets is smaller than that of MNPs, and the assay does not require extensive purification to separate the bound from the free MNPs. Moreover, since the signal is generated from the entire sample volume, the assay benefits from faster binding kinetics than that of surface structure-based devices. Many different types of targets, including small molecules, nucleic acids, and proteins, have thus been detected by MRSw.^{7, 9-12} To date, however, the precise working mechanisms of MRSw have not been fully characterized. This results in limited understanding of MRSw detection capacities, which is further confounded by conflicting literature reports on R_2 changes upon MNP clustering.¹²⁻¹⁴ Specifically, most prior reports were limited by studying only one type of MNPs (*e.g.*, with a fixed core size) or a single transverse relaxation mode (*i.e.*, motional averaging) regardless of the MNP-cluster size.¹³⁻¹⁵

We herein report on a systematic and comprehensive characterization of the MRSw assay. A panel of MNPs with different physical properties were synthesized and utilized for comparative analyses. We specifically focused on 1) characterizing the nature of MNP clustering; 2) elucidating the different transverse relaxation modes with such clustered MNPs; and 3) establishing the relationship between MNP's material properties and its MRSw detection sensitivities. Our study found that clustered MNPs are universally in a quasi-solid, fractal state (dimension of ~ 2.4). Accordingly, a new model for transverse relaxation was constructed, that describes the observed MRSw phenomena. Most importantly, the study led to an analytical MRSw model that could predict the detection sensitivities and dynamic ranges for a given type of MNPs. These findings will aid in not only interpreting existing experiment data but also designing new MNPs and assay protocols to further improve MRSw sensitivities.

RESULTS

Preparation of MNPs with different relaxation properties

We first synthesized a panel of MNPs with different size and composition (**Fig. 1a**; see Methods for details). Small MNPs (CLIO; cross-linked iron oxide) were synthesized through chemical coprecipitation of ferric (Fe^{3+}) and ferrous (Fe^{2+}) chloride with the addition of a base solution (NaOH).¹⁶ The magnetic core measured ~ 8 nm in diameter and was covered with a thick layer of 10 kDa dextran, cross-linked with epichlorohydrin. The resulting particles had a hydrodynamic diameter of ~ 35 nm. Additional ferrite MNPs (Fe_3O_4) were synthesized *via* thermal decomposition of metal-complexes (iron (III) acetylacetonate [$\text{Fe}(\text{acac})_3$] at high temperature (300°C). The core size of these particles was increased from 12 to 16 and then 22 nm, through a seed-mediated growth approach.¹⁷ In a similar manner, Mn-doped ferrite (MnFe_2O_4) particles, which have higher magnetization than Fe_3O_4 , were also prepared by thermally decomposing $\text{Fe}(\text{acac})_3$ in the presence of manganese complexes ($\text{Mn}(\text{acac})_2$).¹⁸ To further improve the magnetization, elemental iron (Fe) was selected as a core material of new nanoparticles. Initially, Fe-MNPs were synthesized by thermally decomposing iron (0) pentacarbonyl [$\text{Fe}(\text{CO})_5$]. To prevent oxidation, Fe-MNPs were then encased with an artificially grown ferrite shell ($\text{Fe@MnFe}_2\text{O}_4$).¹⁹ All prepared MNPs were rendered water-soluble by coating the particle surface with small molecules (2,3-dimercaptosuccinic acid) with the exception for CLIO which had a hydrophilic dextran coating.

For each type of MNPs, we measured its transverse relaxivity (r_2), the capacity of the particles to accelerate the R_2 relaxation of water protons (Methods). With different diameter (d_s ; 8 – 22 nm) and magnetization (M), the prepared MNPs assumed a wide range of r_2 values (**Fig. 1b**). All MNPs, however, were in the motional averaging regime of R_2

relaxation, where the diffusional motion of water protons was fast enough to average out the effects of MNPs. Consequently, the observed r_2 values could be fitted to $r_2 \sim d_s^2 \cdot M^2$, as predicted by the outer-sphere model (dotted lines, Fig. 1b).²⁰

Characterization of MNP clusters and relaxation mechanism

Prepared particles were used to characterize the effect of different MNP types on MRSw assay. As a model mechanism for particle-clustering, we used avidin-biotin interaction. MNPs were biotinylated by forming amide bonds between carboxylic acids in MNPs and amine groups in biotin (Methods). On average, 40 biotin molecules were found to be immobilized per particle. For MRSw assay, a varying amount of avidin was introduced to the biotinylated-MNP solution; control samples were prepared in the same way, but with the addition of PBS (phosphate buffered saline) solution (Methods). Following a 15-min incubation at $T = 300$ K, the samples were subjected to R_2 -measurements using a miniaturized NMR system previously reported.^{7, 21} The corresponding size of MNP clusters was measured *via* dynamic light scattering (DLS).

Two distinct MRSw modes were observed (Fig. 2). With small particles (CLIO), the R_2 values initially rose and then decreased with increasing avidin concentration ($[Av]$; Fig. 2a). In contrast, larger MNPs showed an initial decrease and plateau of R_2 values with increasing $[Av]$ (Figs. 2b-d). For all types of MNPs, a strong correlation between R_2 and cluster size (d_c) was observed, which led to the development of a new physical model of MRSw phenomena. (1) For small MNPs, the clustered particles remain in the motional averaging (MA) mode of relaxation; these clusters are still small enough that the effect of their magnetic fields is averaged out by the diffusional motion of water molecules.²² In the MA mode, the R_2 values concomitantly increase with the particle size. With a core size of 8 nm and water-permeable coating, the clustered CLIO falls into this regime, showing a close match between R_2 and d_c . Further addition of avidin, however, leads to a decrease of both R_2 and d_c , as excess avidin coats MNPs (prozone effect) to hinder inter-particle clustering.²³ (2) Larger MNPs assume a different relaxation mode upon clustering, namely the static dephasing (SD), as their cluster size exceeds the traveling distance of diffusing water molecules. These clusters appear as randomly-distributed, stationary objects.²⁴ In the conventional SD model, where MNPs are assumed to be a solid sphere with a constant magnetization (M), the R_2 values are independent of the particle size but only proportional to M . For the MRSw, however, the observed R_2 values declined with the cluster size d_c , indicating that the effective M decreased in the corresponding clusters.

The observed new R_2 -dependence on the cluster size was further analyzed in the framework of the diffusion-limited aggregation model.²⁵⁻²⁷ Clusters of nanoparticles are known to have a fractal structure; the number of particles (n) per cluster is given as $n \sim (d_c)^f$, where f is the fractal dimension. Accordingly, we hypothesize that the magnetization M_c of the MNP clusters scales as $M_c = M_s \cdot (d_c/d_s)^{f-3}$, where M_s and d_s are the magnetization and the diameter of a single MNP, respectively (see Supporting Information for details). By denoting R_{2c} and R_{2s} as the relaxation rates for clusters and individual MNPs respectively, we then obtain the following power law for the normalized relaxation rate and particle size. For the MA mode, R_2 is proportional to $d^2 \cdot M^2$, hence $(R_{2c}/R_{2s})_{MA} \sim (d_c M_c)^2 / (d_s M_s)^2 \sim (d_c/d_s)^{2f-4}$ (Fig. 3a). Likewise $(R_{2c}/R_{2s})_{SD} \sim (d_c/d_s)^{f-3}$ for the SD mode, since R_2 is proportional to M (Fig. 3b). When the observed MRSw data was replotted in these normalized units, it indeed showed the power law behavior. The dimension (f) determined for each MNP type had a universal value ($f \sim 2.4$), revealing the generic fractal nature of MNP clusters. Similar results were also observed when MRSw assays were performed using DNA molecules as a crosslinker (Fig. S1). Clusters of small MNPs (8 nm Fe_3O_4) were found to be in the MA mode, whereas larger MNPs (16 nm $MnFe_2O_4$) fell into the SD mode

upon clustering; the fractal dimension of MNP clusters for both modes was around 2.4. This value is in good agreement with those ($f = 2.1 - 2.5$) measured by other methods for nanoscale clusters.²⁷⁻²⁹

Analytical model for MRSw assays: detection sensitivities and dynamic ranges

To evaluate the utility of MRSw for molecular sensing, we next investigated the detection limit and dynamic range for each MNP type. For a given MNP concentration, an avidin-dose response curve was obtained (Figs. 4a, b). The lower and upper bounds of $[Av]$ for detection were defined from 5 – 95% of the overall R_2 responses. The detection limit was found to improve with decreasing MNP concentrations, presumably due to a favorable stoichiometric ratio between MNPs and avidin molecules; the R_2 changes are maximized since all MNPs could be transformed into clusters under these conditions. Lowering MNP concentrations, on the other hand, reduced the dynamic ranges, as the R_2 of MNP solutions became closer to that of the background (e.g., water). These opposing behaviors led to the following consequences: 1) MNPs with higher r_2 achieve lower detection limit by producing larger R_2 changes even at low particle concentrations; 2) each MNP type has an absolute lower detection limit, set by the diminishing dynamic ranges. The experimental data further confirmed this hypothesis. The detection limit scaled inversely with particle r_2 ; the lowest detection limit was ~ 1 pM with 22 nm Fe_3O_4 ($r_2 = 1.2 \times 10^{-15} \text{ L}\cdot\text{s}^{-1}$), whereas 8 nm ferrite ($r_2 = 7.0 \times 10^{-16} \text{ L}\cdot\text{s}^{-1}$) had the limit of ~ 2 nM.

The observed detection limits and dynamic ranges were further formulated into a general analytical model, based on the developed MRSw modes (MA, SD) for different MNPs (see Supporting Information for details). The model correlated well with experimental observation (Fig. 4c); the detection limit was found to scale as $1/r_2$, and the dynamic range was proportional to k/α , where k and α are the average numbers of individual MNPs and avidin molecules per cluster, respectively. For the case of DNA molecules, their lower binding affinity led to the formation of smaller MNPs clusters, resulting in smaller k . The overall detection sensitivity and dynamic ranges were thus reduced.

The developed model can further estimate effective MRSw responses for a given MNP type and concentration (Fig. 4c), which can facilitate assay determination and optimization for intended detection targets. Importantly, we could accurately predict the MRSw mode and the absolute detection limit as a function of particle relaxivity r_2 (Fig. 4d). The transition from MA to SD for MNP clusters happened at $r_2 \sim 10^{-15} \text{ L}\cdot\text{s}^{-1}$ (Supporting Information), and higher r_2 lowered the absolute detection limit, all of which agreed well with experimental data.

DISCUSSION

We have performed a systematic investigation on MRSw phenomena using a panel of MNPs with different size and magnetization (Table 1). The study showed that cluster size of MNPs governs the transverse relaxation mode, namely motional averaging (MA) and static dephasing (SD), and thereby elucidated and unified contradicting R_2 changes in previous reports. The study also identified the universal fractal nature ($f = 2.4$) of MNP clusters, which led to new formulation for MA and SD relaxation modes. Based on these understanding, we developed an analytical MRSw model that can be used to estimate the detection limit and dynamic range for a given MNP type. The model further indicates that the detection sensitivity can be enhanced by 1) using MNPs with high r_2 relaxivity, 2) optimizing the stoichiometric ratio between MNPs and molecular targets, and 3) forming denser and larger MNP clusters, which could be achieved by maximizing binding sites per MNP.³⁰ Indeed, among the panel of tested nanoparticles, MNPs with the highest r_2 (22 nm

Fe₃O₄) achieved the lowest detection limit (~1 pM, avidin); by lowering MNP concentration and thereby reducing particle-to-target ratio, the detection sensitivities were also improved.

The model conversely reveals a practical limitation in sensitivity improvement. First, with the detection limit scaling as $1/r_2$, the benefit of increasing r_2 can be easily offset by technical difficulties in MNP synthesis. Preparing single MNPs with higher r_2 is a difficult task, which is often challenged by the availability of suitable magnetic materials and the colloidal stability of resulting particles. Second, because the detection limit is weakly dependent on f , only limited improvement in sensitivity can be achieved through densely packing MNPs. For instance, maximally packed clusters ($f = 2.7$) could be formed by switching from monodisperse to polydisperse particles.³¹ The overall sensitivity improvement, however, is expected to be less than two-fold. Third, due to the intrinsic R_2 of background (e.g., 0.5 s^{-1} for water), there exists a lower bound on MNP concentration to generate discernible R_2 changes (e.g., 5% above the background), which will in turn set the minimum amount of molecular targets detectable. Together, these factors place a practical detection limit in empirical MRSw assays (~100 fM) with MNPs (see Supporting Information for details).

CONCLUSIONS

To further improve MRSw sensitivity, we thus propose the following approaches. First, the assay could incorporate additional target-based amplification strategies. For instance, by employing DNA tags for molecular targeting and performing polymerase chain reaction for their amplification, both the detection sensitivity and specificity of the sensing platform could be considerably enhanced.³² Second, magnetic microspheres, which are developed for magnetic separation, could be adapted for MRSw.^{11, 33, 34} By embedding a large number of small magnetic cores, these particles assume larger r_2 relaxivities than MNPs, and can offer higher detection sensitivity. However, judicious screening and optimization of particles should precede, as magnetic microspheres could display R_2 -drift due to magnetic aggregation during relaxation measurements.¹⁹ Combined with the advantages of MRSw (i.e., negligible interference from biological background, no need for washing steps, and fast assay kinetics), these improved platforms would be a powerful analytic tool for molecular detection.

METHODS

Synthesis and characterization of magnetic nanoparticles

All MNPs were prepared as previously reported. Briefly, amine-terminated cross-linked iron oxide (CLIO) nanoparticles were generated by aqueous co-precipitation and coated with dextran.³⁵

Ferrite nanoparticles (Fe₃O₄ and MnFe₂O₄) were synthesized *via* thermal decomposition and enlarged through a seed-mediated growth process.¹⁸ Iron (III) acetylacetonate [99.9%, Fe(acac)₃], manganese (II) acetylacetonate [Mn(acac)₃], oleylamine (70%), 1-octadecene (95%, ODE), 1,2-hexadecanediol (90%), chloroform (99%), sulfosuccinimidyl-(4-N-maleimidomethyl)cyclohexane-1-carboxylate (99%, sulfo-SMCC), 2,3-dimercaptosuccinic acid (98%, DMSA) and dimethyl sulfoxide (99.9%, DMSO) were purchased (Sigma–Aldrich) and used without further modification. Isopropanol (99.5%), hexane (98.5%), ethanol (99.5%), and NaHCO₃ were purchased (Fisher Scientific) and used as received.

We first synthesized 10-nm MnFe₂O₄ MNPs. Fe(acac)₃ (4 mmol, 1.4 g), Mn(acac)₂ (2 mmol, 0.5 g), 1,2-hexadecanediol (10 mmol, 2.9 g), oleic acid (6 mmol, 1.9 mL), oleylamine (6 mmol, 2.8 mL), and 1-octadecene (20 mL) were mixed by stirring under N₂ flow (1 h).

The mixture was then heated and kept at 200 °C for 2 h. Subsequently, the temperature was ramped to 280 °C to initiate particle formation. After reflux, the mixture was cooled to room temperature, and isopropanol (80 mL) was added. Particles were collected *via* centrifugation ($1,811 \times g$, 15 min) and then dispersed in hexane. To make 12-nm particles *via* the seed-mediated growth, 10-nm MnFe_2O_4 MNPs (100 mg) were dispersed in hexane (10 mL) along with the same amount of metal acetylacetonates, 1,2-hexadecanediol, oleic acid, oleylamine, and 1-octadecene as described above. The mixture was heated and kept at 100 °C for 1 h under N_2 flow. The mixture was then heated and kept at 200 °C for 2 h. Finally, the temperature was increased to 300 °C, and the mixture was refluxed for 2 h. After cooling down to room temperature, the particles were collected by the same washing and isolation procedure. 16-nm MnFe_2O_4 MNPs were synthesized in a similar manner using 12-nm particles as a seed.

$\text{Fe@MnFe}_2\text{O}_4$ were prepared through annealing of manganese and iron-oleate complexes on Fe nanoparticles.¹⁹ Fe-only MNPs were first synthesized. 20 mL ODE and 0.3 mL oleylamine (0.64 mmol) were mixed and the mixture was heated (60 °C) under vacuum (1 h) and recharged with N_2 gas. The mixture was then heated to 260 °C. When the temperature became stable, $\text{Fe}(\text{CO})_5$ (1.4 mL, 10 mmol) was injected. The solution was kept at 260 °C and under N_2 flow for 1 h, after which it was cooled to room temperature. While the Fe MNPs were formed, manganese and iron-oleate complex was separately prepared. $\text{Mn}_2(\text{CO})_{10}$ (156 mg, 0.8 mmol), oleylamine (2.3 mL, 7.26 mmol) and 10 mL ODE were mixed and the mixture was heated to 60 °C under vacuum (1 h) and recharged with N_2 . The mixture was heated to 120 °C and $\text{Fe}(\text{CO})_5$ (0.21 mL, 1.61 mmol) was subsequently injected. The solution, containing metal-oleate complexes, was cooled to room temperature and transferred to the Fe MNP solution using double-ended needles. The mixture of Fe MNPs and metal-oleate complexes was stirred (0.5 h) at room temperature. The reactor temperature was then ramped (5 °C/min) to the optimal annealing temperature (300 °C) for the ferrite-shell formation. When the temperature stabilized, the mixture was stirred for 1 h. The solution was then cooled to room temperature and 150 mL isopropanol solution (ODE/isopropanol = 0.2 v/v) was added. MNPs were collected *via* centrifugation ($1,811 \times g$, 15 min) and dispersed in 10 mL hexane.

The shape, structure, and composition were further characterized using a transmission electron microscope (TEM; JEOL 2100, JOEL USA), an X-ray powder diffractometer (XRD; RU300, Rigaku), and an inductively-coupled plasma atomic emission spectrometer (ICP-AES; Activa-S, HORIBA Jobin Yvon), respectively. The magnetic properties were analyzed using a vibrating sample magnetometer (EV-5, ADE Magnetics). The r_2 relaxivity of MNPs was obtained by measuring R_2 of samples with varying MNP concentrations using a commercial relaxometer (0.47 T; Minispec mq20, Bruker). After the magnetic measurements, samples were dissolved in acid (HCl 10%), and the amounts of metals (Fe, Mn) were quantified by ICP-AES.

Surface modification and biotinylation

Amine-terminated CLIO nanoparticles were biotinylated in the presence of 20-fold molar excess of sulfo-NHS-biotin (Pierce Biotechnology), in PBS containing 0.1M sodium bicarbonate for 3 h at room temperature. Following conjugation, unbound biotin molecules were removed using Sephadex G50 columns (GE Healthcare).

All other MNPs prepared in the organic phase were transferred into the aqueous phase prior to biotinylation. Briefly, the prepared MNPs were suspended in 10 mL chloroform, and treated with 50 μL triethylamine and dimercaptosuccinic acid (DMSA; 50 mg in 10 mL DMSO). The mixture was incubated for 6 h at 40 °C until it gradually turned heterogeneous, and precipitated down by centrifugation (3,000 rpm, 10 mins). The precipitate was washed

with ethanol to remove excess DMSA, and dispersed in 10 mL ethanol. DMSA treatment was then repeated to improve nanoparticle aqueous stability. The precipitated MNPs were finally dispersed in 10 mL water and had terminal sulfhydryl and carboxylic acid groups. The number of sulfhydryl group per nanoparticle was ~50 as determined by Ellman's reagent (Pierce Biotechnology). To conjugate DMSA-treated MNPs with (+)biotin-hydrazide (Aldrich), amide bonds were formed using carboxylic acids in MNPs and amine groups in biotin through NHS/EDC chemical reactions. The DMSA-treated MNPs (25 mg) were dispersed in 10 mL water, followed by the addition of NHS (3.5 mg), EDC (5 mg), and biotin (1 mg). The mixture was shaken for 3 h at room temperature. The conjugated MNPs was precipitated down (1811 g, 20 min) and washed three times with water. The number of biotins per particle, quantified using the EZ Biotin Quantitation Kit (Pierce Biotechnology), was ~40.

MRSw assays

Avidin (ImmunoPure Avidin #21121; Pierce Biotechnology) was first dissolved in PBS, and serially diluted. MRSw samples were prepared by adding 100 μ L of avidin solution, containing varying avidin doses, into biotinylated MNP solutions (100 μ L). After 15 minutes of incubation at 37 °C, T_2 values of all samples were measured from 1 μ L aliquots using a miniaturized nuclear magnetic resonance (NMR) system. Independently, the size of MNP clusters was measured *via* dynamic light scattering (Zetasizer Nano-ZS, Malvern). These experiments were then repeated using samples with different MNP concentrations. For the relaxation measurements, we used Carr-Purcell-Meiboom-Gill pulse sequences with the following parameters: echo time (TE), 4 msec; repetition time (TR), 6 sec; the number of 180° pulses per scan, 500; the number of scans, 8.

Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

Acknowledgments

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Scheme 1. Magnetic relaxation switching (MRSw) assay

Dispersed magnetic nanoparticles (MNPs; left) form clusters upon binding with target molecules (right). Depending on the cluster size, the transverse relaxation of samples can assume two separate modes, motional averaging and static dephasing, resulting in opposite changes in its relaxation rate (R_2).

Figure 1. Panel of MNPs with different transverse relaxivities

(a) To study the effect of particle relaxivity (r_2) on MRSw assays, different types of MNPs with varying size and magnetization were synthesized. The transmission electron micrographs confirmed the narrow size distribution of the prepared MNPs. Clockwise from the top left are: 16 nm Fe_3O_4 , 22 nm Fe_3O_4 , 16 nm Fe-core and MnFe_2O_4 shell ($\text{Fe@MnFe}_2\text{O}_4$), 16 nm MnFe_2O_4 MNPs. (b) The measured transverse relaxivity (r_2) showed good agreement with those predicted by an outer-sphere model (dashed lines). These MNPs thus were in the motional averaging regime in their non-clustered state. M_s , saturation magnetization; CLIO, cross-linked iron oxide nanoparticle.

Figure 2. Different MRSw behaviors for a panel of MNPs

Two distinct relationships between R_2 and cluster size (d_c) were observed. With small MNPs (*e.g.*, 8 nm core MNP; CLIO), the R_2 values were commensurate with the cluster size (a), which indicated that the clusters remained in the motional averaging (MA) regime. For all other MNP types, R_2 values decreased with the cluster size (b – d), as the clusters entered a different relaxation mode (static dephasing; SD).

Figure 3. Characterization of MNP clustering

The normalized R_2 and d showed different power law behaviors than that expected from a conventional MA or SD model, which could be attributed to the fractal nature of MNP clusters. From the observed data, the dimension constant (f) was obtained. Clusters, both in MA (a) and SD (b) mode of relaxation, assumed a universal f value ($= 2.4$), which is close to the theoretical maximum (2.7). Gray areas indicate 95% prediction level from the fit.

Figure 4. Analytical modeling of MRSw assays

(a, b) The detection threshold and dynamic range of each MNP type were determined. For both MA and SD modes, the detection sensitivity improved with decreasing MNP concentrations. With lower MNP numbers, however, the detection dynamic range became narrower with the R_2 of MNP solution approaching that of background. These effects set the detection limit for each MNP type. (c) An analytical MRSw model (for MA and SD modes) was constructed, that can estimate the detection limit and the dynamic range for a given MNP type and concentration. The model showed good correlation with the observed data (dotted lines with triangles). (d) The r_2 relaxivity of MNPs determines the relaxation mode of clusters, with the transition from MA to SD occurring around $r_2 \sim 10^{-15} \text{ L}\cdot\text{s}^{-1}$. The MRSw model also revealed that the detection limit is proportional to $1/r_2$ (solid lines), which agreed well with the experiment data (filled circles). Notably, the sensitivity enhancement becomes progressively slower with r_2 increases, which places practical limits on further sensitivity improvement. The practical detection limit ($\sim 100 \text{ fM}$) was calculated assuming the use of hypothetical, highly magnetic Fe-MNPs ($d_s = 22 \text{ nm}$). Nevertheless, these limits could be overcome by designing new assays employing target amplification strategies and magnetic microspheres.

Table 1

Physical properties of magnetic nanoparticles and the summary of MRSw assays.

Magnetic nanoparticles			MRSw assay	
Composition	Core size (nm)	Hydrodynamic diameter (nm)	r_2 relaxivity ($\times 10^{-15} \text{ s}^{-1} \text{ L}$)	Detection limit (pM) [†]
Fe ₂ O ₃ /Fe ₃ O ₄	8	35	0.7	2000
Fe ₃ O ₄	16	19	23	20
MnFe ₂ O ₄	16	19	60	2.6
Fe ₃ O ₄	22	25	123	1.0
Fe@FeO	16	19	1.8	500
Fe@MnFe ₂ O ₄	16	19	68	1.5

MA, motional averaging; SD, static dephasing.

[†] Based on avidin detection using biotinylated magnetic nanoparticles.