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RNA Folding: Conformational Statistics, Folding Kinetics, and Ion Electrostatics

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Abstract

RNA folding is a remarkably complex problem that involves ion-mediated electrostatic interaction, conformational entropy, base pairing and stacking, and noncanonical interactions. During the past decade, results from a variety of experimental and theoretical studies pointed to (a) the potential ion correlation effect in Mg^{2+} -RNA interactions, (b) the rugged energy landscapes and multistate RNA folding kinetics even for small RNA systems such as hairpins and pseudoknots, (c) the intraloop interactions and sequence-dependent loop free energy, and (d) the strong nonadditivity of chain entropy in RNA pseudoknot and other tertiary folds. Several related issues, which have not been thoroughly resolved, require combined approaches with thermodynamic and kinetic experiments, statistical mechanical modeling, and all-atom computer simulations.

Keywords

chain entropy; stability; conformational change; nonadditivity; ion correlation effect

INTRODUCTION

Over the past three decades, many high-resolution nuclear magnetic resonance (NMR) and X-ray crystallographic structures have been solved for RNAs ranging from tRNAs to the complete ribosome (60,65). On the basis of these structures, RNA biologists gained great insight into RNA mechanisms in gene regulation and biochemical catalysis. However, we are still far from predicting RNA functions from the sequence. Why? Because a static structure does not tell us how RNA undergoes structural changes in the biochemical process. In order to understand RNA functions, we would like to predict not only the native structure from the nucleotide sequence (23,56,82), but also the statistical distribution of the conformational ensemble, from which we can predict the folding stability and the rates and pathways for the structural changes. This review is focused primarily on the thermodynamics and kinetics of RNA folding.

Knowledge-based modeling is highly successful in predicting structures if there exist multiple homologous sequences with known structures (42,56,82). The method can become convoluted when applied to deciphering the alternative structures and structural switches. In contrast, first-principles statistical mechanical modeling predicts the structures and structural changes without relying on homologous structures. In addition, with the continuous improvement of the force field and the conformational sampling, computer simulations (51,79) have provided significant insight into RNA dynamics and stability for hairpins (37,83,104), pseudoknots

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DISCLOSURE STATEMENT

The author is not aware of any biases that might be perceived as affecting the objectivity of this review.

(110), and large RNA machinery such as ribosome (77). In this review, we address the recent advances in RNA folding thermodynamics, kinetics, and ion electrostatic effect with emphasis on the theoretical developments.

In simple terms, RNA folding is a process of navigating the huge conformational space of the polynucleotide chain. The process is driven by several interrelated factors: thermally driven chain fluctuation, ion-mediated electrostatics, base pairing and stacking, and other noncanonical interactions. Therefore, a predictive understanding of RNA folding requires a synthesis of several key components of the problem, including the characterization of RNA conformational space, the equilibrium distribution of the chain conformations, and the kinetics of folding and conformational changes. Of particular importance to RNA folding is the role of metal ions. In recent years, we have witnessed important advances in both theoretical and experimental fronts on RNA folding. Here I focus on several recent results on the above issues. These new advances, especially the results on the nonadditive, long-range, and correlated interactions in tertiary folds and ion effects, challenge the widespread speculation that the RNA folding problem is less difficult than the protein folding problem.

RNA CONFORMATIONAL STATISTICS AND ENTROPY

Each RNA nucleotide has eight degrees of freedom: six backbone torsions, one torsion between the ribose ring and the base, and two types of configurations ($C3'$ —*endo* and $C2'$ —*endo*) for the pucker of the ribose ring (Figure 1c). It would be a formidable task to model RNA folding using all eight parameters because of the large number of possible conformations. In search for a Ramachandran plot for RNA, Murthy et al. (63) performed *ab initio* computation for a small system with two nucleotide-5', 3'-diphosphates and one truncated dinucleotide. Their study demonstrated that steric interactions alone can account for well-separated regions in the conformational space. The result suggests that a denatured RNA has a much smaller conformational space (and entropy) than a completely flexible chain. The findings for the conformational statistics of the denatured state have significant implications for RNA folding stability (i.e., the free energy difference between the folded and the unfolded states), as well as for the folding kinetics, which involves searching for the folded structure from the unfolded conformational ensemble. For a folded RNA, the torsions are further restricted by the long-range (distant along the sequence but proximate in space) contacts and volume exclusion between the nucleotides.

An alternative approach to the investigation of the Ramachandran plot for RNA is based on the survey of the existing known RNA structures. The studies from several groups on this approach have led to two observations. (a) The RNA backbone is rotameric (61). The finding represents a significant development beyond the earlier studies by Olson (66) that led to the virtual bond model for nucleic acids. The model reduces the original six backbone torsions into two (virtual) bonds because the backbone C-O torsions (β and ϵ in Figure 1c) have a preferred *trans* (*t*) rotational isomeric state. (b) RNA virtual bonds manifest separated, preferred conformational regions (31). This finding of the discrete distributions of the virtual bonds is remarkable because it significantly reduces the conformational space for any virtual bond-based RNA models.

Motivated by the observation by Duarte & Pyle (31) on the discrete distributions of the virtual bonds, Cao & Chen (12–14) developed a virtual bond-based RNA folding model (Vfold). The model is based on the experimentally measured atomic coordinates for the helix conformation and the self-avoiding random walks of the virtual bonds in a diamond lattice for the loop conformations. Because the model has the ability to treat structural details such as intraloop base pairing, loop-helix structural interferences (volume exclusion) in multibranched loops

(102), and tertiary contacts, through conformational count it can predict the chain entropy for a given RNA structure such as a loop.

LOOP STABILITY AND RNA SECONDARY STRUCTURE FOLDING THERMODYNAMICS

Chastain & Tinoco (18) defined RNA secondary (tertiary) structures as non-cross-linked (cross-linked) helices and loops (Figure 1*a,b*). Such a definition has the advantage to directly connect the structure to the additivity principle of folding energetics. For a secondary structure, which is relatively extended, different base stacks and loops are weakly correlated and the total free energy of the structure is equal to the sum of the free energies of the base stacks and loops (additivity). For a tertiary structure, however, different helices and loops are brought into close contact and become strongly correlated. As a result, the free energy additivity that applies to secondary structure is doomed to fail (26).

A structure defined by the base pairs and flexible loops can assume many possible conformations. The statistical average over all the possible conformations gives the partition function Z : $Z = \sum_{\text{conformations}} e^{-\Delta E/k_B T}$, where T is the temperature, k_B (3.3×10^{-24} cal/mol·K) is the Boltzmann constant, and ΔE is the energy of the conformation. Z is central to the folding thermodynamics because it gives all the thermodynamic properties (free energy ΔG , enthalpy ΔH , and entropy ΔS).

The favorable stacking energy and the adverse conformational entropy are the two largest factors that determine the RNA folding stability (80). Different secondary structure models use the same set of empirical thermodynamic parameters (Turner rules) (56) for the helix. What distinguishes the different models is how to treat the loop free energy ΔG_{loop} . Most models (38,57,115) assume a purely entropic (i.e., $\Delta G_{\text{loop}} = -T\Delta S_{\text{loop}}$) and sequence-independent loop free energy. The complication of loop stability stems from the intraloop interactions such as non-canonical base pairing, mismatched (non-Watson-Crick) base stacks, single-strand base stacking, and other ion- and solvent-mediated interactions. The sequence-dependent energies of the intraloop interactions cause (a) the sequence dependence and (b) the enthalpic component of the loop free energy.

A statistical approach to the loop free energy requires the enumeration of different intraloop contacts. A key issue is how to evaluate the entropy for given intraloop contacts. No experiment can measure such a conditional entropy. The entropy can only come from an entropy theory such as Vfold. Cao & Chen applied their Vfold model to all the possible intraloop mismatched base stacks and achieved improved predictions for the folding thermodynamics and the structure for RNA secondary structures (12) and RNA/RNA complexes (3,13,27). Further improvements of the model should include the detailed information for the base configurations and other important intraloop interactions (such as noncanonical base pairing).

RNA PSEUDOKNOT: STRUCTURE AND FOLDING STABILITY

Pseudoknots (Figure 1*d,e*) play a critical role in many biochemical processes from regulation of viral gene expression to the catalysis of mRNA splicing and human telomerase RNA (hTR) (85). Central to the pseudoknot stability is the loop entropy (Figure 1*d,e*). Earlier pseudoknot algorithms were severely limited by the nearly complete lack of loop entropy parameters (28, 29, 74). Accurate calculation of loop entropy is challenging because of the loop-stem correlation through the volume exclusion effect. Abrahams et al. (1) introduced a uniform single value of $T\Delta S_{\text{loop}} = 4.2$ kcal/mol for all pseudoknot loops. Later, Gulyaev et al. (36) proposed a set of much-improved loop entropy parameters by introducing several fitting parameters to account for the loop-stem interference. The model with fitted parameters

correctly predicted that the known pseudoknots have lower free energies than the hairpins. More recently, with the Vfold model, which employs no fitting parameter, Cao & Chen (14) systematically computed the loop entropy parameters (Table 1) for different stem and loop size using rigorous polymer statistical mechanics. These parameters give reliable predictions for the folding thermodynamics (Figure 2) as well as the native structures (14).

Despite the promising progress, current pseudoknot theories are unable to treat many biologically significant pseudoknotted structures, such as pseudoknots with (a) a junction between the helix stems (Figure 1b), (b) internal or bulge loops in the helix stems, or (c) loop-stem or loop-loop base pair and base triple interactions (105). These structures are critical to the function of anti-HIV RNA aptamers (11), telomerase RNAs (96), and frameshifting RNAs (22). Three key issues focus on how to compute the chain entropy for these complex structures (47, 48), how to treat loop-stem and loop-loop tertiary interaction energies, and how to treat the possible coaxial stacking between the helices. The current theories can treat only H(airpin)-type pseudoknots with at most one nucleotide that connects the two helix stems, in which case the coaxially stack between the helices contributes a sequence-dependent free energy of $\Delta G_{\text{stack}} \sim 1 - 5$ kcal/mol at 37°C (106).

HAIRPIN AND PSEUDOKNOT FOLDING KINETICS

Hairpin is an elementary building block of RNA structure. The system is simple enough for exhaustive detailed studies yet sufficiently sophisticated to serve as a paradigm for more complex RNA folding kinetics. There have been extensive studies on DNA hairpin folding kinetics using laser temperature-jump (4,55) and fluorescence correlation spectroscopy (8, 43,44,52) techniques. In contrast, there are only very limited experiments on RNA hairpin (and pseudoknot) folding kinetics (54,64,69,111,113,114). The majority of RNA folding kinetics experiments address the folding of a large tertiary structure (76,88,99,101,109) after the formation of the secondary structure in the initial fast phase (μsec) of the measurements. Although RNA and DNA share remarkably similar biophysical properties in many aspects, without detailed measurements, assuming DNA and RNA hairpins to have the same folding kinetics remains unwarranted. In fact, DNA and RNA have different enthalpy and entropy parameters (56,78), which imply that they can have different folding thermodynamics and kinetics.

Recent experimental (54) and theoretical studies (111,113,114) revealed complex multistate, nonexponential folding kinetics even for small RNA hairpins, suggesting a complex bumpy energy landscape. These new results, especially the loop and stem sequence dependence of the hairpin folding kinetics, should dispel the common misconception about hairpin folding kinetics, namely, that folding is always rate-limited by the loop closure and the rate is determined by the loop size (68).

Tetraloop Hairpin Folding Kinetics

A tetraloop is stabilized by excess base pairing and stacking in the loop (103). Experimental measurements for tetraloop hairpin folding kinetics indicated that (a) changing a regular non-GNRA tetraloop to a GNRA tetraloop did not alter the folding rate (64), and (b) the stable (YNMG) UUCG tetraloop and the excessively less stable tetraloop UUUU have nearly the same folding rate (69) and hence the difference in stability between the two loops comes from the different unfolding rates. These experimental findings suggest that the rate-limiting step is not the (sequence-dependent) intraloop stabilization.

All-atom molecular dynamics simulation by Sorin et al. (83) revealed multiple pathways for the folding of a tetraloop RNA hairpin. The simulation showed two types of folding pathways. The first type is zipping (dominant pathway), in which the loop is closed by the marginally

stable base pair (with partial formation of hydrogen bonding), followed by subsequent zipping of the full helix stem. The rate-limiting step is the loop closure instead of intraloop stabilization, which is consistent with the experiments. The second folding pathway type is compaction, in which the chain collapses through nonspecific base pairing to form a heterogeneous structural ensemble, followed by (native-like or misfolded) helix growth from the nucleation centers. In their simulations, the initial collapsed state remained stable over the simulation timescale (μsec). Further simulation is required in order to show how the structure converges to the final, completely folded state.

RNA Hairpin Folding Kinetics: Theoretical Studies

A fundamental ingredient embodied in theoretical approaches to the folding kinetics is the rate constant $k_{i \rightarrow j} = k_0 e^{-\Delta G_{i \rightarrow j}^\ddagger / k_B T}$ for an elementary transition from state i to state j , where $\Delta G_{i \rightarrow j}^\ddagger$ is the activation barrier and k_0 is the fundamental rate constant, which is solvent dependent. Currently there are three types of rate models:

- Base stack model (111,113,114): An elementary kinetic move is the addition and breaking of a base stack, with $\Delta G_{i \rightarrow j}$ equal to the change in the entropic free energy $T\Delta S$ and the enthalpy ΔH , respectively.
- Base pair model (20,32): An elementary kinetic step is the formation or disruption of a base pair, with $\Delta G_{i \rightarrow j}$ equal to $\Delta G/2$ (ΔG is the free energy change from state i to state j) or equal j to ΔG for $\Delta G > 0$ and 0 otherwise.
- Helix stem model (41): A kinetic move is the creation or deletion of a helix stem, with rate constant determined by the helix free energy change (see the Base pair model, above).

The different rate models can lead to different folding pathways. The key factor that distinguishes the different rate models is whether the barrier is determined by $(\Delta H, \Delta S)$ or by ΔG . The $(\Delta H, \Delta S)$ values for different RNA base stacks show well-separated discrete hierarchies, whereas the ΔG values show no such large separation. For two typical base stacks, 5'AU-AU3' and 5'UC-GA3', the difference $\Delta(\Delta H_{\text{stack}}, \Delta S_{\text{stack}}) = (7.4 \text{ kcal/mol}, 20 \text{ cal/mol/K})$ is much larger than the difference $\Delta(\Delta G_{\text{stack}}) = 1.4 \text{ kcal/mol}$ (81). Because of this fact, different models can give different folding kinetics. For instance, in the base stack model, a kinetic trap can be formed by an ensemble of conformations that all contain a nonnative base stack with an outstanding ΔH_{stack} , whereas in the other two models, a trap can only be formed by a stable misfolded helix stem (with multiple stabilizing base stacks). The competition between the loop formation, stem elongation, and detrapping determines the complex sequence dependence of the folding kinetics (54).

For a nontetraloop hairpin, Zhang & Chen (111) predicted a non-Arrhenius kinetics characterized by the folding-transition temperature T_f and the glass-transition temperature T_g (Figure 3). There are three caveats for the predictions. First, the kinetic behavior varies between different sequences. Second, other mechanisms, such as kinetic traps, heat capacity changes (ΔC_p) in loop and base pair/stack formation, and the change of the single-strand base stacking, can also cause the non-Arrhenius behavior. Without further experimental studies, none of the possibilities can be excluded. Third, the single exponential kinetics at $T > T_g$ does not exclude the formation of kinetic intermediates. An ensemble of states, including the kinetic intermediates, can transiently form an effective single macrostate if they can quickly reach mutual local equilibrium. A single exponential kinetics only means the transition between the macrostates is a two-state process.

Experimental verification of the rate model is a challenge because the microscopic elementary processes are buried in the ensemble averages of the measured kinetics. Single-molecule

experiments, with careful extrapolation to the force-free case, may provide a discerning measure. All-atom simulations with reliable force field and sampling method are highly valuable for providing detailed atomistic configurations for the transition state. Alternatively, systematic theory-experiment tests for designed sequences can also provide critical assessment for the different rate models.

There is an important component missed in all the above theoretical models, namely, the sequence-dependent conformational statistics of the single-stranded coil and loop states. The importance of the unfolded state to hairpin folding kinetics has been suggested by several experimental studies. Experiments by Bonnet et al. (8) and Nagel et al. (64) indicated that a pyrimidine-rich loop (such U-loop) folds faster than a purine-rich loop (A-loop) because an A-rich single-stranded coil is prone to form single-stranded stacking, which must be disrupted prior to loop formation. To further examine how the loop composition affects folding kinetics, Proctor et al. (69) substituted a *syn*-G at position 4 in the UUCG tetraloop by a more bulky nucleotide analogy, 8-bromoguanosine, and found the substitution caused a fourfold increase in the folding rate. Thermodynamic measurements (69) suggested that the stronger steric constraint due to the bulky nucleotide analogy reduces the conformational space (and entropy) of the unfolded state, reducing the time for searching the loop conformation from the ensemble of the unfolded conformations.

Pseudoknot Folding Kinetics

Pseudoknot, which forms stable helix stems, is prone to form intermediate states (with a timescale of tens of microseconds). Depending on the sequence, the intermediate state often contains nonnative base pairs and thus must be disrupted (in milliseconds to minutes) before refolding (15,41,70). Several theoretical studies (15,41) indicated that pseudoknot folding involves parallel pathways: a fraction of population folds without being trapped to the misfolded state while the rest of population is first trapped and then refolds through slow detrapping. A recent study by Cao & Chen (15) suggested the dominant pathway shows biphasic kinetics through a misfolded hairpin intermediate. These results have significant implications for the cotranscriptional RNA folding (67) when the RNA chain elongation effect is considered (35,41) (but protein binding and ion effects are ignored). Simulations for several systems by Isambert & Siggia (41) and Gultyaev et al. (35) suggested that a fast RNA chain elongation would more likely cause kinetic trapping. For instance, kinetic Monte Carlo simulation for hepatitis delta virus ribozyme (HDV pseudoknot) predicted that an increase of RNA synthesis rate from 50 to 1000 nt/s causes the trapped population to increase from less than 10% to about 30% (41).

hTR pseudoknot is a catalytically essential region of human telomerase RNA (85,96). The hTR pseudoknot structure has been solved by Theimer et al. (95). Several studies for the structure-activity relationship pointed to the essential role of the pseudoknot structure in hTR activity (19,21,96,97).

Comolli et al. (21) proposed a molecular switch between hairpin and pseudoknot as an essential step for the telomerase activity (97). In contrast, Chen & Greider (19) proposed that only the static pseudoknot structure is required for the function, because their experiment showed that (a) a hairpin-destabilizing mutant retained telomerase activity and (b) destabilizing the pseudoknot caused reduction in telomerase activity. Recently, motivated by the controversy, Cao & Chen (15) applied the kinetic cluster approach (112) to examine the pseudoknot folding kinetics. Their results indicated that the folding of the mutant in the experiment of Chen & Greider (a) has a long-lived hairpin intermediate and (b) undergoes a hairpin-to-pseudoknot transition. The theoretical study suggested a possible kinetic control of the telomerase activity. Discerning the validity of these different models requires more detailed kinetic, biochemical, and functional experiments.

ELECTROSTATIC INTERACTIONS IN RNA FOLDING

RNA backbone is highly (negatively) charged. The formation of the compact tertiary structure requires the polyanionic chain to overcome the massive charge repulsion from the backbone. The divalent Mg^{2+} ions are unusually efficient to promote RNA tertiary structure folding. Physically, the distribution of the cations surrounding an RNA molecule is continuous and dynamic. However, it is useful to classify discrete ion types (Figure 4). A small number of the ions (16,17,25,58,59), which bind to specific sites of RNA, are classified as specific bound ions, while the majority of ions, which move diffusively without binding to any specific sites, are classified as (nonspecific) diffusive ions.

Central to the ion electrostatics of RNA folding is the Mg^{2+} ions. Several excellent articles (9,30,101,109) have extensively reviewed this important problem. In this review, we focus on the recent progress in several specific issues related to Mg^{2+} -mediated RNA folding (5,10,24,45,99).

First, RNA structure is an important determinant for ion-RNA interaction. A rigorous treatment for the ion electrostatics should be based on the complete conformational ensemble of RNA structure. To examine the effect of RNA conformational ensemble, Grilley et al. (34) performed a series of rigorous experiments to measure the Mg^{2+} -dependent stability of an rRNA segment and the BWYV pseudoknot. The experimental data pointed to the importance of considering the (ensemble of) (84) the intermediate states of RNA for the effect of Mg^{2+} on RNA stability. Despite the possible uncertainties associated with the validity of the Poisson-Boltzmann equation for Mg^{2+} -RNA interactions in the analysis, the results suggest that one must be cautious when using the traditional two-state approximation for ion-dependent RNA stability.

Second, ion charge and size (in addition to RNA structure) are also important determinants for ion-mediated RNA folding (2,46). Ion size is crucial not only because it determines the closest distance between an ion and the RNA but also because it affects ion-ion distance and hence the strength of Coulombic and excluded volume correlation. By measuring the folding stability of the *Tetrahymena* ribozyme in the solution of four different types of divalent ions (Mg^{2+} , Ca^{2+} , Sr^{2+} , Ba^{2+}), Koculi et al. (45) found a remarkable linear relationship between the increase of the folding stability of the *Tetrahymena* ribozyme and the increase of the (divalent) ion charge density (i.e., charge/volume of the ion).

Subsequent Brownian dynamics simulation by Koculi et al. (45) for the ion effect on *Tetrahymena* ribozyme folding led to two additional results. First, the distribution of the condensed ions around the RNA showed the liquid-like ion correlation. Second, for the *Tetrahymena* ribozyme, nonspecific electrostatic interaction alone (without specific metal ion coordination effect) can account for the collapsed state as well as the dependence (at least qualitatively) of the folding stability on ion charge density. Koculi et al. hypothesized that for a large RNA such as *Tetrahymena* ribozyme, the large number of nonspecifically bound ions outcompetes the specifically bound ions (16,25) for global stability. However, other experiments suggested that the contribution from the specific site-bound ions may vary significantly between different RNAs (34,84). These contrasting findings suggest the necessity to account for the full ensemble of not only the RNA structures but also the ion distributions (including the presence and absence of the possible buried ions) in the theory.

In a different line of approach, several theoretical (90–94) and experimental (49,76,89,108) groups focused on the mechanism of the unusually efficient Mg^{2+} -mediated driving force in RNA compaction (formation of compact structures lacking stable native tertiary contacts). The remarkable difference between the required ion concentrations (mM for Mg^{2+} and M for Na^+) cannot be simply explained by the effect of the ionic strength (30). Motivated by the desire to quantify the Mg^{2+} -mediated force, two experimental groups (5,71) performed a series

of remarkable experiments for a simple paradigm system: two short DNA helices immersed in a salt solution. The system is interesting for two reasons. First, helix assembly is the elementary step in the initial collapse transition. Second, it helps to quantitatively understand how the electrostatic force stabilizes the helix-helix packing in the observed RNA structural database (62).

For the system with two helices (each with 12 base pairs) tethered by a electrically neutral junction, Bai et al. (5) performed small-angle X-ray scattering (SAXS) experiments and observed (a) no attractive force that is strong enough to induce a collapsed state even in the presence of a 0.6 M (high) Mg^{2+} concentration, and (b) that the Mg^{2+} -induced compact state is an electrostatically relaxed (neutralized) random state.

In a separate study for DNA helices of 25 base pairs dispersed in the solution, Qiu et al. (71) observed an enhanced local clustering of DNA helices with increasing Mg^{2+} concentration. Quantitative analysis for the SAXS profile pointed to a short-range attractive force induced by a small amount of Mg^{2+} ions (~ 16.7 mM). Unlike the helices tethered by short loops (5), which are optimal for possible side-by-side helix attraction, the dispersed short helices (71) tend to form end-to-end helix stacking (attraction), and the attraction increases with decreasing helix length.

A central issue here concerns the strength of the Mg^{2+} -induced force, specifically, whether the force is strong enough to hold the two helices together against the random motion. Further experimental studies on the origin of the Mg^{2+} -induced attraction (71) and the effect of the different tethers, helix length, and the ion different concentration (5) would be highly valuable.

Ion-mediated attraction between polyelectrolytes has been an extensively studied problem (many excellent reviews have been published; see Reference 6). Several models, such as ion entropic driving force (73), ion-ion correlation effect (75), and solvent effects (72,87), have been proposed to explain the attraction. In the ion correlation mechanism, the correlation causes the ions to efficiently reach low-lying states whose energies are much lower than the mean-field energy. As the helices approach each other, the strong correlation (for multivalent ions) makes ions quickly reach low-energy (correlated) states and causes a net attraction.

In a more recent measurement for the Mg^{2+} -induced compaction in a tethered duplex system, researchers (Y. Bai, V. Chu, J. Lipfert, V. Pande, D. Herschlag & S. Doniach, manuscript submitted) found that the mean-field Poisson-Boltzmann equation, which ignores the ion correlation effect, would overestimate the required $[\text{Mg}^{2+}]$ for compaction more than 10 times higher than the experimentally measured value! This experimental result suggested that the traditional Poisson-Boltzmann equation, which ignores the ion correlation and the finite size of the ions, may not be appropriate for Mg^{2+} ions.

Motivated by the importance of the ion correlation effect and of the ensemble of ion distributions, Tan & Chen (90–94) developed the tightly bound ion (TBI) model. The essence of the theory is to provide a rigorous treatment for the strongly correlated ions (tightly bound ions). Later experiments by Stellwagen et al. (86) suggested that the experimentally observed bound cations around a 26-bp DNA helix may correspond to the tightly bound ions proposed in the TBI theory. The TBI model predicted an Mg^{2+} -induced compaction transition at $[\text{Mg}^{2+}] = 1 \sim 5$ mM, which is consistent with the experimental findings (49,76,108). In addition, the model made several new predictions. (a) Polynucleotide tether instead of neutral tether (5), smaller counterions, and multiple helices would make the compaction transition more cooperative. (b) The most compact state is somewhere between the random state and the fully collapsed state and occurs at $[\text{Mg}^{2+}] = 0.1$ M. A higher $[\text{Mg}^{2+}]$ (>0.1 M) makes the system less compact. The validation of these predictions requires further experimental tests.

SUMMARY AND CONCLUSIONS

RNA folding is remarkably complex. It is a result of the delicate balance between multiple factors: the chain entropy, ion-mediated electrostatic interactions and solvation effect, base pairing and stacking, and other non-canonical interactions. Recent experimental and theoretical studies on large ribozyme as well as small RNA systems (hairpin, pseudoknots, and two-helix assembly) are beginning to reveal the detailed folding mechanism that will lead us to a quantitative and predictive model for RNA folding. Currently, the greatest challenge lies in resolving several key issues such as the magnitude of the electrostatic (including ion correlation) and the nonelectrostatic (such as entropic) forces in RNA, the contribution of the specific versus nonspecific electrostatic effects, and the validity of the different rate models for the elementary steps. On the theoretical side, the challenge lies in the accurate calculation for the conformational entropy for RNA tertiary folds, for which the additivity principle fails, proper treatment of Mg^{2+} -induced correlation and solvation effect, and evaluation of the energetics for various noncanonical tertiary interactions. Finally, I would like to emphasize that this review is by no means complete. I refer readers to other review articles (98) on the issues that are not covered here, such as single-molecule experiments for force-induced RNA folding (7,33,40,50,53,100,107), knowledge-based approaches for structural prediction, and computer simulations on RNA folding.

SUMMARY POINTS

1. The rotameric nature of RNA backbone leads to reduced low-resolution models that enable reliable predictions for the chain entropy and folding thermodynamics.
2. Intraloop interactions can cause sequence-dependent loop free energy. Theory considering intraloop interactions can lead to improved predictions for RNA folding thermodynamics.
3. The folding stability of pseudoknot and other RNA tertiary structures are nonadditive. Accurate modeling for the loop-stem interference is the key for pseudoknot prediction.
4. The different rate constant models for the elementary steps in RNA folding can cause different folding pathways. It is critical to identify the correct rate model through well-designed discerning experiments.
5. The ion correlation effect may contribute to the unusually efficient role of Mg^{2+} in RNA tertiary structure folding.

FUTURE ISSUES

1. Is RNA hairpin and pseudoknot folding two-state or multistate? What is the transition state of folding? To resolve the issue requires accurate all-atom simulation, statistical mechanical modeling, and temperature-jump experiments.
2. There exist different rate models for the elementary steps in RNA folding, yet which rate model is valid? Single-molecule experiments would be able to draw a decisive conclusion for the validity of the different models.
3. How should the stability contribution from the site-bound ions (metal ion core) in RNA tertiary structures be properly estimated? This requires a predictive model for the electrostatic and solvation effects, as well as the ion correlation effect.
4. How can we predict the chain entropy for large complex RNA tertiary folds with multiple junctions, and loop-stem and loop-loop tertiary interactions?

5. How can we extract the (Turner rules–like) thermodynamic parameters for tertiary interactions from the melting experiments? This requires systematic thermodynamic experiments for a series of designed RNA tertiary motifs.
6. From the ion electrostatic model, the chain entropy model, and the secondary and tertiary energy parameters, how do we establish a unified predictive model for RNA folding?

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Glossary

Vfold	virtual bond folding model
hTR	human telomerase RNA
SAXS	small angle X-ray scattering
TBI	tightly bound ion model

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Figure 1.

(a) Graphical representation for an RNA structure, where vertices (i.e., nucleotide monomers) are connected by straight lines (i.e., backbone covalent bonds) and base pairs are denoted by curved links. (b) Graphical representation for a pseudoknot. (c) The virtual bonds (shown as the red and blue lines) for RNA backbone. (d) The three-dimensional structure and (e) base-pairing structure for a typical pseudoknot (gene 32 mRNA pseudoknot of bacteriophage T2; PDB ID: 2TPK). Loop 1 (L_1) and loop 2 (L_2) span across the major (narrow, deep) groove of helix 2 (S_2) and the minor (wide, shallow) groove of helix 1 (S_1), respectively. The structure in (d) is adopted from the PDB (PDB ID: 2TPK) (39).

Figure 2.

Predicting pseudoknot stability using the loop entropy parameters in Table 1 (14). For loop 1, length of stem 2 is 7 bp, length of loop 1 is 1 nt, so the entropy is read from Table 1 as $\Delta S_1(7,1)$. Similarly, for loop 2, stem 1 is 5 bp, loop 2 is 4 nt, so the loop entropy is $\Delta S_2(5,4)$. The total free energy of the pseudoknot is $\Delta G = \Delta G_1 + \Delta G_2 - T \Delta S_1(7,1) - T \Delta S_2(5,4) + \Delta G_{\text{assemble}} = (-6.6) \text{ kcal/mol} + (-11.2) \text{ kcal/mol} + (k_B T)(2.3) + (k_B T)(9.8) + 1.3 \text{ kcal/mol} = -9.0 \text{ kcal/mol}$, where $\Delta G_{\text{assemble}} = 1.3 \text{ kcal/mol}$ accounts for the multiple ways to connect the two loops (14) and $k_B T = 0.62 \text{ kcal/mol}$ at $T = 37^\circ\text{C}$. See Reference 14 for more examples.

Figure 3.

Temperature dependence of the reaction rate k (111). (a) $T > T_f > T_g$: The relaxation process is predominantly unfolding, with single exponential kinetics along an unzipping pathway. The apparent activation barrier $[= -d \ln(k)/d(1/T)]$ is positive, equal to the enthalpic cost of breaking the rate-limiting base stack(s). (b) $T_g > T > T_f$: The relaxation process is predominantly folding, with single exponential kinetics along a zipping pathway. The activation barrier is negative, equal to the stabilizing enthalpy of the rate-limiting base stack(s). (c) $T < T_g$: The relaxation process is predominantly folding, with multistate multiple exponential kinetics involving multiple pathways, including the zipping pathway and detrapping-refolding pathways. The activation barrier is positive, equal to the average enthalpic cost to detrapp the misfolded states.

Figure 4.

Two types of cations surrounding the P4-P6 RNA structure (17): specific binding and diffusive binding. A recent Mg^{2+} ion titration study suggested that two metal ions induce cooperative folding of the P4-P6 metal ion core (25).

Table 1
Pseudoknot loop entropy parameters^a

Stem size (bp) (S ₁)	Loop size (nt)											
	1	2	3	4	5	6	7	8	9	10	11	12
<i>L₁</i> (across the deep groove of S ₂)												
2	—	—	—	6.2	6.4	6.4	6.6	6.8	6.9	7.1	7.2	—
3	—	6.4*	6.4*	6.4	6.6	6.6	6.8	6.9	7.1	7.3	7.5	—
4	4.4*	4.4*	4.5	5.4	5.6	6.0	6.3	6.6	6.9	7.1	7.3	—
5	2.3	4.4	4.6	5.7	6.0	6.5	6.9	7.2	7.5	7.8	8.0	—
6	2.3	4.4	4.8	5.8	6.0	6.5	6.8	7.1	7.4	7.6	7.8	—
7	2.3	4.4	5.0	5.9	6.2	6.8	7.0	7.3	7.6	7.8	8.0	—
8	—	4.4	5.2	5.7	6.4	6.7	7.1	7.3	7.5	7.7	7.9	—
9	—	5.5*	5.5	6.4	6.7	7.2	7.5	7.9	8.1	8.3	8.5	—
10	—	6.9*	6.9*	6.9	7.5	7.7	8.1	8.3	8.6	8.8	8.9	—
11	—	—	—	—	8.7	8.8	8.9	9.1	9.2	9.3	9.3	—
12	—	—	—	—	9.8	9.2	9.5	9.6	9.7	9.8	9.8	—
<i>L₂</i> (across the shallow groove of S ₁)												
2	—	—	—	7.6	7.0	7.0	7.1	7.2	7.3	7.4	7.5	7.7
3	—	6.5*	6.5*	6.5	6.6	6.7	6.9	7.1	7.2	7.4	7.6	7.7
4	—	—	9.2*	9.2*	9.2	8.9	8.9	8.9	9.0	9.0	9.1	9.2
5	—	—	—	9.8*	9.8*	9.8	9.1	8.9	8.8	8.8	8.8	8.8
6	—	—	—	11.9*	11.9*	11.9	11.0	10.4	10.1	9.9	9.9	9.8
7	—	—	—	—	12.4*	12.4*	12.4	12.4	11.4	11.0	10.7	10.5
8	—	—	—	—	12.1*	12.1*	12.1	12.1	11.6	11.4	11.2	11.1
9	—	—	—	—	—	13.7*	13.7*	13.7*	13.7	12.6	12.0	11.5
10	—	—	—	—	—	13.7*	13.7*	13.7	12.7	12.2	11.8	11.5
11	—	—	—	—	—	—	—	—	15.9	14.1	13.0	12.4
12	—	—	—	—	—	—	—	—	18.7	15.8	14.2	13.2

^aThe upper and lower tables give $(-\Delta S_{\text{loop}}/kB)$ for loop 1 and loop 2, respectively; see Figure 1. The entries with an asterisk (*) denote the long stem and short loop structures that cannot be realized in the diamond lattice but may be viable for a realistic pseudoknot. For these restricted loops, we use the entropies of the minimal loop lengths for the same helix length. This table is adapted from Reference 14.