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Protein Backbone Dynamics through $^{13}\text{C}'$ – $^{13}\text{C}^\alpha$ Cross-Relaxation in NMR Spectroscopy

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Abstract

Internal dynamics of proteins are usually characterized by the analysis of ^{15}N relaxation rates that reflect the motions of NH^N vectors. It was suggested a decade ago that additional information on backbone motions can be obtained by measuring cross-relaxation rates associated with intra-residue $\text{C}'\text{C}^\alpha$ vectors. Here we propose a new approach to such measurements, based on the observation of the transfer between two-spin orders $2\text{N}_z\text{C}'_z$ and $2\text{N}_z\text{C}^\alpha_z$. This amounts to “anchoring” the C'_z and C^α_z operators to the N_z term from the amide of the next residue. In combination with symmetrical reconversion, this method greatly reduces various artifacts. The experiment is carried out on human ubiquitin at 284.1 K, where the correlation time is 7.1 ns. The motions of the $\text{C}'\text{C}^\alpha$ vector appear more restricted than those of the NH^N vector.

Introduction

The study of internal dynamics of proteins and nucleic acids by nuclear magnetic relaxation has been a very innovative and fruitful area of research over the past 15 years.^{1–3} In proteins, many probes have been used to characterize the motions of the backbone. Although most studies have focused on ^{15}N nuclei,^{1,4} a variety of methods enable the measurement of relaxation properties of $^{13}\text{C}^\alpha$ and $^{13}\text{C}'$ nuclei, where C' denotes the carbonyl carbon.^{5–7} Studies of $^{13}\text{C}^\alpha$ relaxation rates, which are comparable to those of amide ^{15}N , revealed similar dynamic properties for both nuclei.⁵ Relaxation studies of $^{13}\text{C}'$ complemented the information obtained by ^{15}N relaxation.^{6,7} Much effort has also been invested in the characterization of the dynamics of the $\text{C}'\text{C}^\alpha$ vector, either by measuring relaxation rates due to cross-correlated fluctuations between the C' chemical shielding anisotropy (CSA) and the $\text{C}'\text{C}^\alpha$ dipolar coupling⁸ or by investigating auto-correlated dipolar cross-relaxation, also known as the nuclear Overhauser effect (NOE), $\sigma(\text{C}'\text{C}^\alpha)$.^{9,10} Two approaches have been described to measure the dipolar cross-relaxation rate $\sigma(\text{C}'\text{C}^\alpha)$, by observing either the transient NOE or the steady-state NOE. The latter experiment, along with cross-correlation measurements, was used to supplement the characterization of protein backbone dynamics by ^{15}N relaxation.¹¹ The transient experiment has been extended to sample side-chain dynamics.¹² Several studies of the dynamics of the $\text{r}(\text{C}'\text{C}^\alpha)$ vector, employing various methods, have led to somewhat different interpretations.^{7, 11,13–15}

These results show that it is important to measure complementary relaxation rates to determine the amplitude and anisotropy of internal motions of peptide planes. The cross-relaxation rate

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$\sigma(C'C^\alpha)$ is particularly attractive for this purpose, since the $C'C^\alpha$ bond makes an angle of about 60° with respect to the NH^N bond. Furthermore, uncertainties associated with the magnitudes and orientations of CSA tensors have no effect. Unfortunately, the measurement of steady-state effects⁹ on C'_z due to saturation of $^{13}C^\alpha$ suffers from systematic errors caused by other carbon nuclei, such as $^{13}C^\beta$. The measurement of transient effects, as proposed by Cordier et al.,¹⁰ suffers from similar systematic errors, and the normalization of the transferred polarization is not fully satisfactory.

In this article, we present a new method to measure the dipolar cross-relaxation rate $\sigma(C'C^\alpha)$ that is much less prone to systematic errors. The measurement of the transient Overhauser effect between the two-spin orders $2N_zC'_z$ and $2N_zC_z^\alpha$ restricts the transfer to the one-bond cross-relaxation pathway. Moreover, symmetrical reconversion, a method that was initially developed in the context of cross-correlation experiments,¹⁶ allows one to normalize the transferred polarization.

Principle of the Experiment

The dipolar cross-relaxation rate $\sigma(C'C^\alpha)$ can be quantified either by monitoring the build-up of a transient polarization or by measuring a steady-state nuclear Overhauser effect upon saturation of one of the partners.¹⁷ Steady-state NOE methods are time-consuming because of the long saturation period required before each scan and the need for additional measurements of the C' longitudinal relaxation rate. The $^{13}C^\alpha$ nuclei have to be saturated without affecting other nuclei, so that a compromise has to be chosen between a saturation that is either too selective or too broad. If some C^α 's are not completely saturated, the corresponding $\sigma(C'C^\alpha)$ rates will be underestimated. If the saturation is too broad, other carbons such as C^β will be saturated, so that the $\sigma(C'C^\alpha)$ rates will be overestimated. Moreover, even if only the C^α 's are saturated perfectly, cross-relaxation with the C^α of the next residue, with a rate $\sigma(C_{i+1}^\alpha C_i')$ leads to an overestimation of the cross-relaxation rate $\sigma(C_i' C_i^\alpha)$ by about 6%. These problems can be overcome by selecting a suitable network in transient NOE experiments.¹⁸ Figure 1 presents the geometry of the system and shows the cross-relaxation pathway that must be isolated and those that must be suppressed.

The method of Cordier et al.¹⁰ – where the initial polarization of aliphatic protons is employed – fails to suppress the effects of cross-relaxation with C_{i+1}^α and C_i^β , unless an additional ^{13}C chemical shift evolution period is inserted before the relaxation time. Moreover, it is difficult to normalize the signal intensities, and the experiment is not applicable to deuterated proteins. By starting from the amide proton instead of the aliphatic protons, it is possible to reduce significantly the amount of polarization C_z^β at the beginning of the relaxation period: the upper value of $^2J(C'C^\beta)$ reported for ubiquitin¹⁹ (1.9 Hz) leads to a polarization transfer from C' to C^β of less than 1% during the refocused insensitive nuclei enhanced by polarization transfer (INEPT) sequence²⁰ designed to transfer polarization from C' to C^α . Combined with the low cross-relaxation rate, $\sigma(C_i' C_i^\beta)$ (about 5% of $\sigma(C_i' C_i^\alpha)$), this effect may be safely neglected.

The problem caused by cross-relaxation between C_i' and C_{i+1}^α still has to be solved. A way to discriminate between C_i^α and C_{i+1}^α would be to employ selective pulses. However, it would be very time-consuming to implement such an experiment if information is required for an entire protein. The approach we have chosen is to monitor the relaxation between the longitudinal two-spin orders, $2N_z^{i+1}C_z^{i,i}$ and $2N_z^{i+1}C_z^{\alpha,i}$. “Anchoring” the carbon operators to those of the amide nitrogen is an efficient way to design residue-specific experiments. Indeed, a perturbing cross-relaxation rate between C_i' and C_{i+1}^α leads to an undesired conversion of the two-spin order operator $2N_z^{i+1}C_z^{i,i}$ to $2N_z^{i+1}C_z^{\alpha,i+1}$, which is then transferred by evolution under scalar coupling

to $2N_z^{i+1}C_z'^{i+1}$. Since the scalar coupling $J(N_{i+1}C_{i+1}')$ is very small,¹⁹ the contribution of the latter operator to the observed signal will be negligible. This approach can be compared to those designed to suppress the observation of cross-relaxation from the amide protons.^{21,22} Since the INEPT transfer from N_{i+1} to C_i' does not require refocusing, one does not need to insert two intervals $(2J(N_{i+1}C_i'))^{-1}$ (~33 ms) where the C' single-quantum coherence evolves. This becomes important when transverse C' relaxation by CSA is fast.

Two other issues are crucial for the quantitation of the transient $C'C^\alpha$ NOEs. First, the buildup signal has to be normalized. Second, the difference between the auto-relaxation rates $\rho(2N_z^{i+1}C_z'^{i+1})$ and $\rho(2N_z^{i+1}C_z^{\alpha,i})$ has to be determined to extract an accurate cross-relaxation rate from normalized buildup curves. These two issues can be solved by one and the same approach. Recently, a method called symmetrical reconversion was introduced for the measurement of transverse cross-correlation rates.¹⁶ In this article, this idea will be adapted to the measurement of auto-correlated longitudinal cross-relaxation rates.

The principle of the method, depicted in Figure 2, is to record four different experiments that correspond to all four relaxation pathways in a system comprising two spin operators. If A_I and A_{IV} are the amplitudes of the signals in the two auto-relaxation experiments (e.g., the decay of the $2N_zC_z'$ and $2N_zC_z^\alpha$ two spin orders) and A_{II} and A_{III} the amplitudes recorded in the two cross-relaxation experiments (e.g., the transfer from $2N_zC_z'$ to $2N_zC_z^\alpha$ and vice versa), then

$$\sqrt{\frac{A_{II}A_{III}}{A_I A_{IV}}} = \tanh |\sigma_{CR} T|, \quad (1)$$

where T is the relaxation delay and ρ_{CR} the cross-relaxation rate which, as will be shown below, is an excellent approximation to the cross-relaxation rate between C_z' and C_z^α . This relationship is exact even if the efficiencies of the preparation and reconversion steps are unknown, provided the auto-relaxation rates ρ_P and ρ_Q of the two operators $P = 2N_zC_z'$ and $Q = 2N_zC_z^\alpha$ are identical.

Theory

In a system comprising two operators with different auto-relaxation rates, ρ_P and ρ_Q , the evolution of the operators P and Q is given by

$$\frac{d}{dt} \begin{Bmatrix} \langle P \rangle(t) \\ \langle Q \rangle(t) \end{Bmatrix} = - \begin{pmatrix} \rho_P & \sigma_{CR} \\ \sigma_{CR} & \rho_Q \end{pmatrix} \begin{Bmatrix} \langle P \rangle(t) \\ \langle Q \rangle(t) \end{Bmatrix} \quad (2)$$

This differential equation can be solved analytically:

$$\begin{Bmatrix} \langle P(T) \rangle \\ \langle Q(T) \rangle \end{Bmatrix} = \exp(-\rho_{AV} T) \begin{pmatrix} ch + \frac{\Delta_{QP}}{\Sigma} sh & -\frac{\sigma_{CR}}{\Sigma} sh \\ -\frac{\sigma_{CR}}{\Sigma} sh & ch - \frac{\Delta_{QP}}{\Sigma} sh \end{pmatrix} \begin{Bmatrix} \langle P(0) \rangle \\ \langle Q(0) \rangle \end{Bmatrix} \quad (3)$$

where $ch = \cosh(\Sigma T)$, $sh = \sinh(\Sigma T)$, $\rho_{AV} = (\rho_P + \rho_Q)/2$, $\Delta_{QP} = (\rho_Q - \rho_P)/2$, and $\Sigma = (\Delta_{QP}^2 + \sigma_{CR}^2)^{1/2}$. The ratio of signal amplitudes defined in eq 1 can thus be expressed as

$$\sqrt{\frac{A_{II}A_{III}}{A_I A_{IV}}} = \sqrt{\frac{\sigma_{CR}^2 sh^2}{\Sigma^2 ch^2 - \Delta_{QP}^2 sh^2}} \quad (4)$$

Note that there are only two unknown quantities, σ_{CR} and Δ_{QP} , on the right-hand side of this equation. When $\Sigma T \ll 1$ or $\Delta_{QP}^2 \ll \alpha_{CR}^2$, eq 4 simplifies to eq 1. Otherwise, Δ_{QP} can be extracted from the ratio of the signal intensities of experiments IV and I:

$$\frac{A_{IV}}{A_I} = C \frac{\Sigma ch - \Delta_{QP} sh}{\Sigma ch + \Delta_{QP} sh} \quad (5)$$

where the constant $C = 1$ in the (unlikely) event that the efficiencies of the preparation and reconversion of the operators P and Q in experiments I and IV are equal. If this is not the case, one must record signal amplitudes for at least two relaxation delays T to extract σ_{CR} by simultaneously fitting eqs 4 and 5. Note that for $\Sigma T \ll 1$, eq 5 does not depend on σ_{CR} .

The dipolar cross-relaxation rate is^{23,24}

$$\sigma(C'C^\alpha) = -\frac{d_{CC}^2}{4} [J(0) - 6J(2\omega_c)] \quad (6)$$

where $d_{CC} = (\mu_0/4\pi)\hbar\gamma_c^2 r_{CC}^{-3}$, μ_0 is the permeability of free space, $\hbar$ Planck's constant divided by 2π , γ_c the gyromagnetic ratio of ^{13}C nuclei, r_{CC} the bond length, ω_c the Larmor frequency for ^{13}C , and $J(\omega)$ the spectral density function for the rotational motion of the internuclear vector. In a macromolecule with axially symmetric global tumbling tensor and with the assumptions of the model-free approach,²⁵ $J(\omega)$ can be written as^{26,27}

$$J(\omega) = \frac{2}{5} \sum_{k=1}^3 A_k \left[S^2 \frac{\tau_k}{1 + \omega^2 \tau_k^2} + (1 - S^2) \frac{\tau'_k}{1 + \omega^2 \tau_k'^2} \right] \quad (7)$$

with $A_1 = (3 \cos^2 \theta - 1)^2/4$, $A_2 = 3 \sin^2 \theta \cos^2 \theta$, $A_3 = 3/4 \sin^2 \theta$, $\tau_1 = (6D_\perp)^{-1}$, $\tau_2 = (D_\parallel + 5D_\perp)^{-1}$, $\tau_3 = (4D_\parallel + 2D_\perp)^{-1}$, and $(\tau'_k)^{-1} = (\tau_k)^{-1} + (\tau_e)^{-1}$; S^2 is the local order parameter, τ_e is the effective correlation time for the fast local motion, $D_\parallel$ and $D_\perp$ are the rotational diffusion constants parallel and perpendicular to the symmetry axis of the diffusion tensor, and θ is the angle between this axis and the average orientation of the internuclear vector, $\mathbf{r}(C'C^\alpha)$.

In a large macromolecule with very fast local motions, one has approximately

$$\sigma(C'C^\alpha) \approx -\frac{d_{CC}^2}{10} S^2 \tau_c^{\text{local}} \quad (8)$$

where $\tau_c^{\text{local}} = \sum_{k=1}^3 A_k \tau_k$ can be computed from the structure and hydrodynamic properties of the macromolecule. In the case of isotropic rotational diffusion, τ_c^{local} is equal to the correlation time τ_c . The simple form of eq 8 makes $\sigma(C'C^\alpha)$ a convenient probe of the local order parameter S^2 .

The cross-relaxation rate σ_{CR} between the operators $2N_z^{i+1}C_z'^i$ and $2N_z^{i+1}C_z^{\alpha,i}$ comprises two terms which have opposite signs in macromolecules:²⁸

$$\sigma_{CR} = \sigma(C'C^\alpha) + \delta(\text{NC}'\text{NC}^\alpha) \quad (9)$$

where $\delta(\text{NC}'\text{NC}^\alpha)$ is the relaxation rate originating from the cross-correlation of the ^{15}N - ^{13}C ' and ^{15}N - $^{13}\text{C}^\alpha$ dipolar couplings. The expression for this rate is²⁸

$$\delta(\text{NC}'\text{NC}^\alpha) = \frac{3}{2}d(\text{NC}')d(\text{NC}^\alpha)J(\text{NC}'\text{NC}^\alpha)(\omega_N) \quad (10)$$

where $d(\text{NC}') = (\mu_0/4\pi)\text{H}\gamma_C\gamma_N r(\text{NC}')^{-3}$, $d(\text{NC}^\alpha) = (\mu_0/4\pi)\text{H}\gamma_C\gamma_N r(\text{NC}^\alpha)^{-3}$, γ_N is the gyromagnetic ratio of ^{15}N , and $r(\text{NC}')$ and $r(\text{NC}^\alpha)$ are the internuclear distances between the N nucleus and the C' and C $^\alpha$ nuclei, respectively.

For isotropic global diffusion and isotropic local motion, the spectral density function may be written as²⁹

$$J(\text{NC}'\text{NC}^\alpha)(\omega) = \frac{2}{5} \left[S^2(\text{NC}'\text{NC}^\alpha) \frac{\tau_c}{1+\omega^2\tau_c^2} + \left(\frac{3\cos^2\Theta(\text{NC}'\text{NC}^\alpha)-1}{2} - S^2(\text{NC}'\text{NC}^\alpha) \right) \frac{\tau_c}{1+\omega^2\tau_c^2} \right], \quad (11)$$

where $S^2(\text{NC}'\text{NC}^\alpha)$ is the cross-correlation order parameter and $\Theta(\text{NC}'\text{NC}^\alpha)$ is the angle between the $\mathbf{r}(\text{NC}')$ and $\mathbf{r}(\text{NC}^\alpha)$ internuclear vectors. In the absence of local motion, the order parameter is $S^2(\text{NC}'\text{NC}^\alpha) = [3 \cos^2[\Theta(\text{NC}'\text{NC}^\alpha)] - 1]/2$.²⁸

Figure 3 presents the structural parameters employed to calculate the values of cross-relaxation rates in the five-spin system under investigation. The total rate $\sigma_{\text{CR}} = \sigma(\text{C}'\text{C}^\alpha) + \delta(\text{NC}'\text{NC}^\alpha)$ differs from the desired rate $\sigma(\text{C}'\text{C}^\alpha)$ because of the perturbing term $\delta(\text{NC}'\text{NC}^\alpha)$. The ratio $r = \delta(\text{NC}'\text{NC}^\alpha)/\sigma(\text{C}'\text{C}^\alpha)$ was calculated assuming isotropic local and global motions, so that the order parameters of all processes are affected equally. For a global correlation time τ_c , the ratio r is shown in Figure 4. As expected from the absence of a zero-frequency term in eq 10, the contribution of $\delta(\text{NC}'\text{NC}^\alpha)$ diminishes with increasing size. Clearly, $|r| \ll 1$ in large macromolecules ($\tau_c > 10$ ns) but should not be neglected in small proteins. Note that the ratio r shows little dependence upon variations of isotropic local dynamics. The desired cross-relaxation rate can be obtained as $\sigma(\text{C}'\text{C}^\alpha) = \sigma_{\text{CR}}/(1 + r)$.

The apparent rate σ_{CR} can be contaminated by higher-order processes, which are due to multiple-step cross-relaxation and are proportional to T^n ($n \geq 2$) rather than linear in T . These spin-diffusion processes may lead to deviations from the ideal relationship of eq 1. The evolution of the 2^N populations in the system with $N = 5$ spins of Figure 3 was computed (in the base of all Zeeman operators and products thereof) with the interactions shown in Figure 3. Only the 5 strongest of the 10 possible dipole-dipole interactions were considered. The parameters employed for the CSA tensors are the averages obtained by Loth et al.²⁹ for H^{N} , C', and N. For $^{13}\text{C}^\alpha$ and $^{13}\text{C}^\beta$, we assumed the CSA to be $\delta\sigma = 30$ ppm and the symmetry axes of the tensors to lie along the $\mathbf{r}(\text{C}^\alpha\text{H}^\alpha)$ and $\mathbf{r}(\text{C}^\alpha\text{C}^\beta)$ vectors, respectively. The auto-relaxation rates were assumed to be $R(\text{C}'_z) = 0.8\text{s}^{-1}$, $R(\text{C}^\alpha_z) = 0.5\text{s}^{-1}$, $R(\text{C}^\beta_z) = 0.5\text{s}^{-1}$, $R(\text{H}^\text{N}_z) = 3\text{s}^{-1}$, and $R(\text{N}_z) = 1.5\text{s}^{-1}$. For the product of any longitudinal operators A and B (single- or multiple-spin orders), we assumed that $R(AB) = R(A) + R(B)$. Cross-relaxation rates were calculated for $S^2 = 1$ and isotropic global diffusion ($\tau_c = 7$ ns). As in the experiments, both $^{13}\text{C}^\alpha$ and $^{13}\text{C}'$ spins were inverted at $t = T/4$ and $t = 3T/4$, while the ^{15}N and ^1H spins were inverted at $t = T/2$. The calculations show that the deviations of the apparent rate (obtained from eq 1) from the relationship $\sigma_{\text{CR}} = \sigma(\text{C}'\text{C}^\alpha) + \delta(\text{NC}'\text{NC}^\alpha)$ are below 0.3%, even for $T = 800$ ms. The deviations are mostly due to the difference δ_{QP} of eq 3. These deviations could thus be taken into account by eq 4. Note that the small dipolar coupling between N and C $^\alpha$ can safely be neglected in the calculations for second- and higher-order contributions. In contrast, the cross-correlated relaxation rate $\delta(\text{NC}'\text{NC}^\alpha)$ contributes to first order to σ_{CR} and has been taken into account with the ratio r of Figure 4.

Experimental Section

All experiments were run on a Bruker Avance 600 spectrometer, with a static field of 14.1 T, equipped with either (i) a triple-resonance TXI cryoprobe with a z -axis gradient for the measurement of $\sigma(C^\alpha C')$ or (ii) a triple-resonance TBI room-temperature probe with three-axis gradients for the measurement of ^{15}N relaxation rates. A sample of uniformly triply labeled [^2H , ^{13}C , ^{15}N]ubiquitin at a concentration of 1.5 mM in a $\text{H}_2\text{O}:\text{D}_2\text{O}$ (90:10 v:v) buffer with 50 mM ammonium acetate (pH = 4.5) was used at a temperature of 284.1 K.

The pulse sequences used for the measurement of the cross-relaxation rate σ_{CR} are presented in detail in the Supporting Information. To improve both the amount of the proton polarization available at the beginning of each scan and the extent of water suppression,³⁰ a water flip-back scheme was implemented with a WATERGATE sequence³¹ prior to acquisition. All carbon pulses were selective, except the initial purge pulses and the C' pulses in the preparation and conversion of $2\text{N}_z C'_z$. The $\pi/2$ pulses were either Q5 Gaussian cascades³² or time-reversed Q5 pulses, depending on whether the operators are flipped toward or away from the transverse plane; all π pulses applied to C' were Q3 pulses,³² whereas all π pulses applied to C^α were REBURP pulses.³³

The ^{15}N chemical shift labeling is performed using a constant-time evolution period. This can be changed to a semi-constant time scheme for systems that require a higher resolution in the ^{15}N dimension. For each relaxation delay, the four experiments of symmetrical reconversion were interleaved, with 512 complex points in the ^1H dimension and 60 complex points in the ^{15}N dimension. Frequency-sign selection in the ω_1 dimension was performed with the States method.³⁴ Each free induction decay resulted from the sum of 64 scans. Every time point T required about 20 h of experimental time. The relaxation delays T were 400 (twice), 500, 600 (twice), 700, and 800 ms.

The rotational correlation time was determined with regular ^{15}N R_1 , R_2 and $^{15}\text{N}\{^1\text{H}\}$ steady-state NOE experiments³⁵ as well as cross-correlated CSA(^{15}N)/DD($^{15}\text{N}^1\text{H}$) longitudinal³⁶ η_z and transverse¹⁶ η_{xy} cross-relaxation rates. The relaxation delays employed were $T = 15$ (twice), 55, 105, 155, 205, 255 (twice), 305, 375, 505, and 655 ms for the R_1 experiments as well as $T = 2, 10, 20, 30$ (twice), 40, 44, 50, 60, and 74 ms for the R_2 experiments. The ^1H saturation period was 6 s for the $^{15}\text{N}\{^1\text{H}\}$ NOE experiment. The mixing times were $T = 100, 140, 180$, and 220 ms for longitudinal and $T = 60$ and 80 ms for transverse CSA/DD cross-correlated relaxation rates.

The processing of the spectra was performed with NMRPIPE.³⁷ The fit of peak intensities was performed with the nonlinear line shape analysis program nlinLS. Particular attention was paid to partially overlapping peaks. If a satisfying automated analysis could not be performed, the peaks were removed from further analysis. The symmetrical reconversion ratio of eq 1 was then used as input for the program curvefit.³⁸

A potential source of error can be the nonideal behavior of the band-selective inversion of C_z^α during the relaxation delay. First, an imperfect inversion may affect the apparent cross-relaxation between C' and C^α . If one uses symmetrical reconversion, the loss of C_z^α polarization due to incomplete inversion in the auto-relaxation experiment IV in Figure 2 is comparable to the product of the losses of intensity in the two cross-relaxation experiments II and III. Thus, this effect is expected to be negligible. Second, if C_z^β is partially inverted unwittingly, cross-relaxation in the three-spin system $\{C', C^\alpha, C^\beta\}$, with additional rates $\sigma(C^\alpha C^\beta)$ and $\sigma(C' C^\beta)$, has to be evaluated. Since all cross-relaxation rates are much smaller than the auto-relaxation rates $\rho(2\text{N}_z^{i+1} C_z^{i'})$ and $\rho(2\text{N}_z^{i+1} C_z^{\alpha,i})$, all relaxation delays T that yield sufficient signal intensity are

in the initial linear regime of cross-relaxation. Therefore, second-order spin diffusion effects should be small. In the Supporting Information, numerical calculations show that both sources of errors can, indeed, be neglected.

Results and Discussion

Three examples of experimental buildup curves and best fits are presented in Figure 5. The quality of the data and corresponding fits is satisfactory for quantitative analysis. A high cross-relaxation rate σ_{CR} can be observed for the $C'C^\alpha$ pair of glutamine Q31, which is located in the α helix of ubiquitin, thus demonstrating the local rigidity of the secondary structure. The lower cross-relaxation rate for leucine L8 shows the well-documented flexibility of the turn between the first and second β strands.^{11,26} Arginine R74 is located in the very flexible C-terminal tail, which is reflected by the very low value of σ_{CR} .

Figure 6 shows the corrected cross-relaxation rates $\sigma(C'C^\alpha) = \sigma_{CR}/(1 + r)$. The ratio $r = \delta(NC'NC^\alpha)/\sigma(C'C^\alpha)$ was extracted from Figure 4 (assuming $S^2 = 1$) using $\tau_c = 6.91$ ns. This estimate was obtained from the largest measured value of σ_{CR} with eq 8, assuming $S^2 = 1$. The isotropic correlation time obtained from ^{15}N relaxation is $\tau_c = 7.11$ ns. There is no significant difference in the values of r extracted using these two estimates of the isotropic correlation time. This shows that one does not need ^{15}N relaxation data to extract $\sigma(C^\alpha C')$ from σ_{CR} . However, one should be careful if the overall motion is highly anisotropic or the entire molecule is floppy.

The parameters describing the local motions of the $N_iH_i^N$ vectors can be combined with the NMR structure of human ubiquitin⁴² to predict the motions of the $C'_{i-1}C^\alpha_{i-1}$ vectors, assuming isotropic local motions of the entire peptide planes, so that S^2 and τ_c are the same for both $N_iN_i^N$ and $C'_{i-1}C^\alpha_{i-1}$ vectors. Overall, the negative rates $\sigma(C'C^\alpha)$ predicted in this fashion have a slightly smaller amplitude than the experimental rates: the experimental average over residues 2–72 gives $\langle\sigma(C'C^\alpha)_{exp}\rangle = -0.115 \pm 0.001$ s⁻¹. This lies between the rate $\langle\sigma(C'C^\alpha)_{pred}\rangle = -0.109$ s⁻¹ predicted if S^2 and τ_c from ^{15}N relaxation rates are used, and $\langle\sigma(C'C^\alpha)_{rigid}\rangle = -0.129$ s⁻¹ if one assumes that $S^2 = 1$. A few residues (e.g., T14, E16, G35, D39, L43, F45) show a significantly larger magnitude $|\sigma(C^\alpha C')|$ than predicted, but none of the rates is larger than predicted for the rigid case of $S^2 = 1$.

Figure 7 shows the correlation of experimental order parameters $S^2(C'C^\alpha) = \sigma(C'C^\alpha)_{exp}/\sigma(C'C^\alpha)_{rigid}$ with experimental order parameters $S^2(NH^N)$ derived from ^{15}N relaxation rates. The rates $\sigma(C'C^\alpha)_{rigid}$ were predicted using parameters of global anisotropic motion derived from ^{15}N relaxation rates, assuming $S^2 = 1$, i.e., without local motions. The ratio $S^2(C'C^\alpha) = \sigma(C'C^\alpha)_{exp}/\sigma(C'C^\alpha)_{rigid}$ corresponds to the one used in eq 7 for restricted local motions on fast time scales. To interpret these order parameters quantitatively, one needs to introduce a model for the local motions. One often describes anisotropic local motions of the peptide plane with the so-called axially symmetric three-dimensional Gaussian amplitude fluctuation (3D GAF) model,⁷ where motions around three orthogonal axes are characterized by the amplitudes $\sigma_\alpha = \sigma_\beta = \kappa\sigma_\gamma$ (σ_γ corresponds to fluctuations about the $C'_{i-1}C^\alpha_i$ vector).

Theoretical curves are shown in Figure 7 for the 3D GAF model for $\kappa = 0, 0.5, 1$, and 2 (red, light blue, dark blue, and purple curves). In principle, unless the local motions are isotropic ($\kappa = 1$), it is not possible to separate the two contributions to the experimental rate $\sigma_{CR} = \sigma(C'C^\alpha) + \delta(NC'NC^\alpha)$. Thus, one derives an apparent order parameter $S^2\{\sigma_{CR}\} = aS^2\{\sigma(C'C^\alpha)\} + bS^2\{\delta(NC'NC^\alpha)\}/(a + b)$. The order parameter $S^2\{\sigma_{CR}\}$ was calculated for very anisotropic local motions ($\kappa = 0$, i.e., $\sigma_\alpha = \sigma_\beta = 0$) and weights $a = 1$ and $b = -0.12$, which corresponds to a severe contamination, as can be seen in Figure 4. Results are displayed as the green diamonds which are almost exactly located on the red curve that represents $S^2\{\sigma(C'C^\alpha)\}$. The curves

show that the order parameters $S^2\{\sigma(C'C^\alpha)\}$ and $S^2\{\sigma_{CR}\}$ cannot be distinguished, even for a large local motional anisotropy ($\kappa = 0$) and an unusually large contribution of $\delta(NC'NC^\alpha)$. Thus, the ratio $r = \delta(NC'NC^\alpha)/\sigma(C'C^\alpha)$ is sufficiently insensitive to the degree of anisotropy of local motion expressed by the parameter $\kappa = \sigma_\alpha/\sigma_\gamma = \sigma_\beta/\sigma_\gamma$ in the GAF model, so that it is legitimate to extract $\sigma(C'C^\alpha)$ from $\sigma(C'C^\alpha) = \sigma_{CR}/(1 + r)$, and then to determine the order parameter $S^2\{\sigma(C'C^\alpha)\}$.

The dynamics of the four residues that belong to the C-terminal tail of ubiquitin and that exhibit large-amplitude motions cannot be described accurately by a simple model-free approach. The use of the extended model-free approach makes it difficult to compare the total order parameter⁴¹ to the 3D GAF-derived order parameters. Most of the remaining peptide planes show an order parameter $S^2(C'C^\alpha)$ that is larger than $S^2(NH^N)$. This indicates that the local motions cannot be accurately described by an isotropic model ($\kappa = 1$). In the axially symmetric 3D GAF model, the degree of anisotropy of the motions of the peptide plane is reflected by the ratio κ . Most experimental points lie between the curves corresponding to $\kappa = 0.5$ and $\kappa = 1$. None of the experimental points lies above the $\kappa = 0$ curve, which would be incompatible with the 3D GAF model. For comparison, the average value for κ obtained by Lienin et al.⁷ was 0.4 on ubiquitin at 300 K. However, this ratio, which suggests a more pronounced anisotropy than our results at 284.1 K, was critically dependent on the carbonyl CSA values employed. On the other hand, Wang et al.¹¹ found values for $S^2(C'C^\alpha)$ lower than $S^2(NH^N)$ using either cross-correlated relaxation between the C' CSA and the C'C $^\alpha$ dipolar coupling⁸ or C'C $^\alpha$ NOE measurements. However, recent results for ubiquitin using both ^{15}N relaxation and $^{13}C'$ relaxation⁴³ suggest that the NH N vectors sample a greater range of motions than the C'C $^\alpha$ vectors.

Residual dipolar couplings (RDC) are also sensitive to local dynamics. Ottiger and Bax¹³ have obtained effective bond lengths from RDC measurements in ubiquitin. The ratio between NH N and C'C $^\alpha$ bond lengths was found to be larger than the one usually assumed in relaxation studies. In this study, the local motions were considered to be isotropic. Bernado and Blackledge¹⁴ have shown that the longer apparent NH N bond length could be explained by a 3D GAF model for the motions of the peptide plane. However, RDCs are also sensitive to motions on slower time scales,^{44–46} making it difficult to extract the parameters of the fast motion sampled by liquid-state relaxation studies.

Conclusion

We have presented a new method for the accurate measurement of the one-bond dipolar auto-correlated cross-relaxation rate between $^{13}C'$ and $^{13}C^\alpha$ nuclei in proteins. This rate gives a direct measure of the mobility of the C'C $^\alpha$ vector, which complements the standard ^{15}N analysis. We refer to this method as COCA-NOE. The use of symmetrical reconversion and the anchoring of polarizations to the backbone ^{15}N nucleus of the next residue (by the observation of the transfer between two-spin orders $2N_zC'_z$ and $2N_zC^\alpha_z$) circumvent artifacts of earlier methods. We have introduced a self-contained way to correct the observed rates by taking into account a small cross-correlated relaxation contribution to the measured rate. Other possible sources of systematic error are estimated to be negligible. Comparison of order parameters $S^2(C'C^\alpha)$ extracted from our experiment with $S^2(NH^N)$ obtained from ^{15}N relaxation measurements shows that the local motion of the peptide plane is anisotropic and that the C'C $^\alpha$ vectors sample fewer motions than the NH N vector in ubiquitin.

Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

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Figure 1.

Representation of the system under investigation. The blue boxes highlight the $^{13}\text{C}'$ and $^{13}\text{C}^\alpha$ nuclei that carry the polarizations C'_z and C^α_z . These are partly interchanged by the cross-relaxation rate $\sigma(\text{C}'\text{C}^\alpha)$ indicated by a solid blue arrow. This rate must be determined accurately to obtain a measure of local motions. Dotted red arrows show competing cross-relaxation pathways between the carbonyl $^{13}\text{C}'$, the intra-residue side chain nuclei $^{13}\text{C}^\beta$ and $^{13}\text{C}^\gamma$, as well as the $^{13}\text{C}^\alpha$ of the next residue.

Figure 2.

Schematic representation of the four experiments required to measure the cross-relaxation rate $\sigma(C'C^\alpha)$. In experiments I and IV, the auto-relaxation of the operators $2N_zC'_z$ and $2N_zC^\alpha_z$ (represented by blue and red rectangles, respectively) is measured, while the cross-relaxation from $2N_zC'_z$ to $2N_zC^\alpha_z$ and vice versa, which occurs with the rate $\sigma(C'C^\alpha)$, is measured in experiments II and III.

Figure 3.

Interactions and parameters employed to calculate of the evolution of the 2^N populations in a system with $N = 5$ spins. (a) Schematic representation of the interactions considered, with ellipses and dashed lines corresponding to CSA and relevant dipole–dipole (DD) interactions respectively. (b) Effective bond distances (in picometers) and (c) angles subtended between DD interactions.

Figure 4.

Ratio $r = \delta(\text{NC}'\text{NC}^\alpha)/\sigma(\text{C}'\text{C}^\alpha)$ of the perturbing cross-correlation rate $\delta(\text{NC}'\text{NC}^\alpha)$ and the desired cross-relaxation rate $\sigma(\text{C}'\text{C}^\alpha)$, which together give the measured rate $\sigma_{\text{CR}} = \sigma(\text{C}'\text{C}^\alpha) + \delta(\text{NC}'\text{NC}^\alpha) = (1 + r)\sigma(\text{C}'\text{C}^\alpha)$, as a function of the overall tumbling correlation time τ_c .

Calculations were carried out with eqs 6, 7, 10, and 11, assuming isotropic overall tumbling. Three different models of isotropic local dynamics were considered: rigid residues with $S^2 = 1$ (solid blue line), typical residues with $S^2 = 0.85$ and $\tau_e = 50$ ps (dotted red line), and highly mobile residues with $S^2 = 0.5$ and $\tau_e = 100$ ps (dashed green line).

Figure 5.

Three typical buildup curves of the symmetrical reconversion ratio of eq 1, with their best-fit curves and the structure of ubiquitin. Filled red circles and the solid red line correspond to the C^αC' pair of glutamine Q31 observed through the NH^N pair of aspartate D32 ($\sigma_{\text{CR}} = (10.9 \pm 0.12) \times 10^{-2} \text{ s}^{-1}$). Blue crosses and the dashed blue line correspond to the C^αC' pair of leucine L8 observed through the signal of threonine T9 ($\sigma_{\text{CR}} = (9.07 \pm 0.09) \times 10^{-2} \text{ s}^{-1}$). Filled green squares and the dotted green line correspond to the C^αC' pair of arginine R74 observed through the signal of glycine G75 ($\sigma_{\text{CR}} = (2.33 \pm 0.02) \times 10^{-2} \text{ s}^{-1}$). The structure of ubiquitin³⁹ was generated with MOLMOL.⁴⁰

Figure 6.

Dipolar cross-relaxation rates $\sigma(C'C^\alpha)$ for 53 residues of human ubiquitin. Red symbols represent corrected rates $\sigma(C'C^\alpha) = \sigma_{CR}/(1 + r)$. The light blue line corresponds to rates $\sigma(C'C^\alpha)_{\text{rigid}}$ predicted using anisotropic global tumbling without local motions. The dark blue line incorporates the effects of isotropic local motions (residue-specific S^2 and τ_e) obtained from ^{15}N relaxation. For the last four residues, the extended model-free parameters were employed.

⁴¹ Error bars indicate the 68% confidence limits.

Figure 7.

Orange dots: correlation of experimental order parameters $S^2(C'C^\alpha) = \sigma(C'C^\alpha)_{\text{exp}}/\sigma(C'C^\alpha)_{\text{rigid}}$ with experimental order parameters $S^2(\text{NH}^N)$ derived from ^{15}N relaxation rates. The four points circled in red represent residues for which the extended model-free approach⁴¹ was used to fit ^{15}N relaxation data. The curves show the theoretical correlation for the three-dimensional Gaussian amplitude fluctuation (3D GAF) model with amplitudes $\sigma_\alpha = \sigma_\beta = \kappa\sigma_\gamma$ (where σ_γ corresponds to fluctuations about the $C_{i-1}^\alpha C_i^\alpha$ vectors) for $\kappa = 0, 0.5, 1$, and 2 (red, light blue, dark blue, and purple curves). The green diamonds (which are almost exactly on the red curve) represents $S^2\{\sigma_{\text{CR}}\} = aS^2\{\sigma(C'C^\alpha)\} + bS^2\{\delta(\text{NC}'\text{NC}^\alpha)\}/(a+b)$ for very anisotropic local motions ($\beta = 0$, i.e., $\sigma_\alpha = \sigma_\beta = 0$) for weights $a = 1$ and $b = -0.12$.