Modeling of the Mechanical Function of the Human Gastroesophageal Junction Using an Anatomically-Realistic Three-Dimensional Model

R. Yassi\textsuperscript{1}, L. K. Cheng\textsuperscript{1}, V. Rajagopal\textsuperscript{1}, M. P. Nash\textsuperscript{1,2}, J. A. Windsor\textsuperscript{3}, and A. J. Pullan\textsuperscript{1,2,4}

\textsuperscript{1} Auckland Bioengineering Institute, The University of Auckland, New Zealand \textsuperscript{2} Department of Engineering Science, The University of Auckland, New Zealand \textsuperscript{3} Department of Surgery, The University of Auckland, New Zealand \textsuperscript{4} Department of Surgery, Vanderbilt University, Nashville, United States of America

Abstract

The aim of this study was to combine the anatomy and physiology of the human gastroesophageal junction (the junction between the esophagus and the stomach) into a unified computer model. A three-dimensional computer model of the gastroesophageal junction was created using cross-sectional images from a human cadaver. The governing equations of finite deformation elasticity were incorporated into the three-dimensional model. The model was used to predict the intraluminal pressure values (pressure inside the junction) due to the muscle contraction of the gastroesophageal junction and the effects of the surrounding structures. The intraluminal pressure results obtained from the three-dimensional model were consistent with experimental values available in the literature. The model was also used to examine the independent roles of each muscle layer (circular and longitudinal) of the gastroesophageal junction by contracting them separately. Results showed that the intraluminal pressure values predicted by the model were primarily due to the contraction of the circular muscle layer. If the circular muscle layer was quiescent, the contraction of the longitudinal muscle layer resulted in an expansion of the junction.

In conclusion, the model provided reliable predictions of the intraluminal pressure values during the contraction of a normal gastroesophageal junction. The model also provided a framework to examine the role of each muscle layer during the contraction of the gastroesophageal junction.

Keywords

GEJ; mechanical behavior; muscle contraction; finite elasticity

1 Introduction

The gastroesophageal junction (GEJ) is a sophisticated region of the gastrointestinal tract where the narrow esophageal tube adjoins the stomach. In normal situations, the GEJ controls the
entry of food into the stomach, but does not allow the passive return of food due to the presence of a high-pressure zone at the GEJ. There is a lack of accord between the anatomical and functional descriptions of the GEJ by anatomists, physiologists, gastroenterologists, radiologists and surgeons (Castell, 1995; Christensen, 1987; Gray et al., 1979; Liebermann-Meffert and Brauer, 1995). While physiologists refer to the GEJ as a sphincter due to the presence of a high-pressure zone, anatomists dispute the use of the word sphincter due to the lack of thickening in the muscle layer (Bombeck et al., 1966; Castell, 1975; Castell, 1995; Christensen, 1987; Gray et al., 1979; Liebermann-Meffert and Brauer, 1995). Some studies, however, have shown a slight increase in the circular muscle layer around the GEJ (Bombeck et al., 1966; Liebermann-Meffert and Brauer, 1995; Mosher, 1930). This lack of understanding of the microstructure of the GEJ has limited the understanding of the correlation between the anatomy and physiology of the GEJ.

During esophageal manometry, a catheter is inserted transnasally into the patient to provide measurements of the intraluminal pressure of the GEJ during swallowing (Castell and Richter, 2004; Gregersen, 2003; Tytgat, 1991). This is the standard method for evaluating GEJ function. The recorded intraluminal pressure profile of the GEJ is typically divided into three main stages. The first is known as the resting or basal pressure, which is recorded during the resting state of the GEJ and has been found to vary between 10–40 mmHg (1.33–5.33 kPa) (Christensen, 1987; Kahrilas, 1997; Patti et al., 1997; Richter et al., 1987; Shafik et al., 2006; Stein et al., 1995). When a swallow commences, the GEJ relaxes and the pressure drops to the relaxation pressure, which ranges between 0–12 mmHg (0–1.6 kPa) (Shi et al., 1998). The peak pressure is the maximum pressure caused by the contraction of the GEJ to empty the food into the stomach and can range between 50–80 mmHg (6.67–10.67 kPa) (Christensen, 1987; Mittal and Balaban, 1997; Sugarbaker et al., 1993; Tytgat, 1991). As the esophagus passes through the diaphragm, the GEJ is encircled by muscular portions of the diaphragm known as the crural pillars, which contribute to the total measured intraluminal pressure of the GEJ (Delattre et al., 2000). If the GEJ fails to relax or contract, the pressure recorded during manometry can detect such abnormalities. However, the contributions of the surrounding anatomical structures and the physiological functions related to the GEJ are difficult to assess using the current diagnostic methods.

The purpose of this study was to construct an anatomically- and physiologically-realistic computer model of the GEJ to aid in the understanding of how the anatomy and physiology of the GEJ are integrated in health and disease states, and to investigate the contribution of surrounding structures towards the functionality of this region. To this end, an anatomically-realistic three-dimensional (3D) model of the GEJ was constructed from cross-sectional images of the region. The governing equations of finite deformation elasticity were incorporated into the model and solved using the finite element method to investigate normal physiological behavior of human GEJ. The model was then used to investigate the contribution of the different muscle layers of the GEJ (longitudinal and circular), and the contribution of the crura to the behavior of the GEJ.

2 Materials and Methods

2.1 Constructing a three-dimensional model of the GEJ

To obtain a realistic geometric representation of the GEJ, a 3D model was constructed using the two-dimensional (2D) cross-sectional photographic images obtained from the Visible Human Project1 (Spitzer et al., 1996). The inner and outer boundaries of the esophageal wall and the crura were manually segmented from the images (spaced 2 mm apart). These segmented images were then used to construct a three-dimensional model of the GEJ.

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data were aligned, assembled and then used to construct 3D meshes of the esophagus and the crura using the methods outlined by Bradley et al. (1997). The surfaces of the meshes were represented using smoothly continuous cubic Hermite basis functions. The wall of the esophageal model was divided into two layers of equal thickness (Castell, 1995; Christensen, 1987; Liebermann-Meffert and Brauer, 1995) to represent the outer longitudinal muscle (LM) layer and the inner circular muscle (CM) layer (Castell and Richter, 2004) with appropriate fiber orientations.

In a healthy human, the GEJ is closed at rest, at the onset of swallowing the GEJ relaxes and opens to allow the passage of food to the stomach. The diameter of the GEJ was visually examined on the images obtained from the Visible Human Project and it was found that the lumen of the GEJ was in an open state. Therefore, the visible human data presented in this study was assumed to provide the relaxed or the stress-free reference state. The pressure of the GEJ in the relaxed state was assumed to be 0 mmHg.

2.2 Constitutive relations

A number of experiments have been carried out to obtain the stress-strain relationship of the esophagus at the zero-stress state in animals (Fan et al., 2004; Gregersen et al., 2000; Gregersen et al., 1999; Lu and Gregersen, 2001; Zhao et al., 2007) and in humans (Takeda et al., 2002). In addition, recent work has been carried out to describe the mechanical properties of the esophageal wall (Egorov et al., 2002; Takeda et al., 2004; Vanags et al., 2003) using different loading conditions and methods. However, to the best of our knowledge, a constitutive relation has not yet been developed to describe the mechanical behavior of the human GEJ.

Initial work on modeling the passive mechanical behavior of the esophagus in 2D has been carried out using animal data (Liao et al., 2003; Yang et al., 2004; Yang et al., 2006). The constitutive relations developed in these studies neglected the variations of stress and strain throughout the wall, as well as the muscle’s resistance to shear. To model the 3D physiological behavior of the muscular layers of the GEJ, we used the transversely isotropic constitutive relation proposed by Guccione, et al. (1991) to model cardiac ventricular muscle. The Guccione relation is capable of modeling the mechanical behavior of a tissue in 3D and also includes the resistance to shear. The strain-energy density function of this constitutive relation takes an exponential form as follows:

\[ \overline{W} = \frac{C}{2} \left( e^{\theta} - 1 \right) \] (1)

where \( Q = 2c_1(E_{11} + E_{22} + E_{33}) + c_2E_{11}^2 + c_3(E_{22}^2 + E_{33}^2 + 2E_{23}^2) + 2c_4(E_{12}^2 + E_{13}^2) \) (2)

The properties of the smooth muscle (longitudinal and circular) in the GEJ were described by the five material parameters, \( C, c_1, c_2, c_3, \) and \( c_4 \), given in Equations (1) and (2). Trial simulations were carried out to examine the effect each material parameter had on the intraluminal pressure during muscle contraction of the GEJ. Using the conclusions drawn from these simulations, and by fitting the intraluminal pressure values predicted by the model to pressure values available from literature, the values of the parameters \( C, c_1, c_2, c_3, \) and \( c_4 \) were set to 1, 5, 195, 185, and 0.1 respectively.

2.3 Modeling active contraction of the esophagus

To model the active contraction of the muscle fibers in the GEJ, a technique previously developed to model the active contractile behavior of cardiac cells was used (Hunter et al.,
1997; Malvern, 1969; Nash, 1998; Nash and Hunter, 2000). In this study, we assumed that the muscle fibers only generated active force in the direction of the fibers’ main axis and that the transverse and shear strains had no effect on the active tension generated by the fibers. To model the active contraction in the muscle fibers, an extra term was added to the 3D passive stress tensor in Equation (3):

$$T^{MN} = \frac{1}{2} \left( \frac{\partial W}{\partial E_{MN}} + \frac{\partial W}{\partial E_{NM}} \right) - \rho C^{MN} + T J \frac{\partial X_M}{\partial x_1} \frac{\partial X_N}{\partial x_1}$$

(3)

where $J = \det F$. The extra term altered the $T^{11}$ component of the Cauchy stress tensor to include the active tension generated by the fiber, $T$. Further details can be obtained in Appendix A or from Hunter et al. (1998).

### 2.4 Modeling the intraluminal pressure

The intraluminal pressure recorded during manometry is due to the contraction of the GEJ against the manometer. A second mesh, referred to as the ‘cavity’ mesh, was created inside the GEJ lumen to calculate the intraluminal pressure values. Geometrically, the nodes of the outer wall of the cavity were identical to the nodes of the internal wall of the GEJ as illustrated with a cylindrical model in Figure 1. This method has previously been used to represent the blood in a model of cardiac mechanics (Nash, 1998). The cavity was assumed to be incompressible and all the elements of the cavity mesh have the same hydrostatic pressure value. This pressure was an additional solution degree of freedom (DOF), which was calculated using a single global constraint that equated the current volume of the cavity to the initial volume prior to contraction (Appendix B). As the mesh of the GEJ actively contracted, the size of the cavity mesh was expected to reduce in size. However, the cavity mesh was restricted to be of constant volume and therefore this leads to an increase in the cavity pressure, which was applied to the inner GEJ surface. To allow some movement in the radial direction of the GEJ mesh, one node of the cavity mesh (not shared with the GEJ mesh) was constrained to move approximately along the long axis of the GEJ. This additional constraint permitted contraction of the GEJ lumen while obeying the volume constraint of the cavity mesh. The displacement of the ‘free node’ in the axial direction was an additional solution DOF. The displacement of the free node was regulated to control the degree of cavity contraction, and hence the magnitude of the cavity pressure. To ensure the correct physiological movement of the GEJ towards the mouth (Winans, 1972), the displacements of the distal nodes connected to the stomach were fixed in all directions.

### 2.5 Mesh refinement and solution convergence

A portion of the 3D model of the esophagus was selected and used to model muscle contraction of the GEJ. The length of the GEJ has been found experimentally to range between 20–50 mm (Christensen, 1987; Kahrilas, 1997; Patti et al., 1997; Weinstock and Clouse, 1987; Winans, 1972). Some studies have shown that the proximal 20 mm of the GEJ is wrapped by the crura (Castell and Richter, 2004; Mittal and Balaban, 1997). The location of the crura in relation to the GEJ found in the literature was used to identify the GEJ in the 3D model. Therefore, the first mesh considered for simulations consisted of 80 tri-cubic Hermite elements, surrounded by the crura, representing a 34 mm long GEJ (blue region in Figure 2), 16 elements representing the lower esophagus and 32 elements representing the top part of the stomach (6305 total geometric degrees of freedom). The intraluminal pressure of the GEJ mesh was calculated as the global h-refinement was increased by sequentially dividing each element in half in each direction while maintaining regular element geometry. At each step a convergence analysis of the intraluminal pressure was performed.
An increased level of contraction was obtained with incremental increases of the $Ca_{actn}$ parameter, which is a spatially constant non-dimensional parameter used to represent the level of activation. The peak pressure was obtained when the $Ca_{actn}$ parameter reached the value of 1. At each loading step, convergence was achieved using 5–10 full Newton-Raphson iterations. Convergence was reached when the norm of residuals reached the tolerance of $1 \times 10^{-8}$.

Simulations of the GEJ model were carried out using a single 1.9 GHz processor of an IBM pSeries P595 computer (IBM, United States). Numerical simulations were all carried out using the CMISS\(^2\) software package.

### 2.6 Investigating the contribution of the crura

Both the GEJ and the crura contribute towards the intraluminal pressure of the GEJ measured during manometry. To investigate the contribution of the crura towards the physiological behavior of the GEJ, two simulations were carried out. In the first simulation, the muscle layers of the GEJ were actively contracted. In the second simulation, the GEJ was actively contracted whilst an external passive pressure of 37.5 mmHg (5 kPa) was applied to each of the elements of the LM layer surrounded by the crura. This load was estimated to account for the 44% contribution of the crura towards the final recorded pressure of the GEJ (Shafik et al., 2006). The external pressure was applied using incremental load steps each of 1.5 mmHg (0.2 kPa). Since this is a quasi-static problem, the external pressure and the $Ca_{actn}$ parameter were incremented simultaneously.

During manometry recordings, the resting pressure is usually reached at approximately 45% of the time taken to reach the peak pressure. In this study, we assumed that the increase in the $Ca_{actn}$ parameter varied linearly with respect to the time taken to reach the peak pressure. Therefore, the resting pressure was obtained when the $Ca_{actn}$ parameter reached a value of 0.45. In both cases, with and without crural contribution, the $Ca_{actn}$ parameter was increased in increments of 0.05 to ensure Newton convergence for nonlinear finite deformation elasticity mechanics. Intraluminal pressures of the GEJ due to muscle contraction with and without a crural contribution were calculated.

### 2.7 Examining the role of different muscle layers

Studies have speculated that the contribution of the GEJ to the intraluminal pressure is mainly due to the contraction of the innermost CM layer (Brasseur et al., 2007). In this study, we aimed to investigate the role of the CM layer towards the intraluminal pressure of the GEJ. The 3D model of the GEJ provided the flexibility to examine the respective role of each muscle layer in a way that is not feasible to perform experimentally on human subjects in-vivo. Within the GEJ model, each muscle layer was individually contracted and the effect on the intraluminal pressure was calculated.

### 3 Results

#### 3.1 Mesh refinement and solution convergence

As shown in Figure 3, the change in the intraluminal pressure decreased with an increase in the number of DOF. The mesh with 19877 DOF was chosen in this study to model the physiological behavior of the GEJ as the mesh predicted converged pressure values. The mesh consisted of a total of 672 nodes, 416 tri-cubic Hermite elements. Thirty two elements represented the lower esophagus, 320 elements the GEJ and 64 elements represented the top region of the stomach. The CPU time for each simulation was approximately 2 days.

\(^2\)http://www.cmiss.org/
3.2 Contribution of the crura

Intraluminal pressures of the GEJ due to muscle contraction with and without a crural contribution were calculated. Table 1 lists the pressure of the 3D model due to the contraction of the GEJ with and without the contribution of the crura. Results from the 3D model show that approximately 53% of the intraluminal pressure was due to the GEJ.

3.3 The role of muscle contraction

Results obtained from examining the role of each muscle layer are listed in Table 2 and show that the pressure values obtained from the 3D model are mainly due to the contraction of the CM layer. If the CM layer was quiescent, the contraction of the LM layer resulted in an expansion of the GEJ. This expansion is illustrated by the negative intraluminal pressure during the contraction of only the LM. However, with the presence of both layers, the contraction of the CM layer dominated the effect of the LM layer and resulted in an overall increase in pressure.

4 Discussion

A mathematical model that provides a realistic representation of a human GEJ would be beneficial to perform numerical studies in order to provide a better understanding of the functionality of the GEJ both in health and disease states. In order to accurately model the behavior of the different layers that contribute to the functionality of the GEJ, a more detailed understanding of the correlation between the physiology and anatomy is required. Such information includes the tissue properties of the different layers of the human GEJ, and a constitutive relation to model the behavior of these tissues, which is presently lacking. With the limited available data in the literature, the focus of our study was to construct a computer model that provides a prediction of the intraluminal pressure and can be validated with pressure recordings from manometry.

The intraluminal pressure results obtained from the 3D model constructed in this study showed a 53% contribution of the GEJ to the overall pressure, which was similar to the predicted value of 56% from experimental data available in the literature (Shafik et al., 2006). Results showed that the 3D model presented in this study, was capable of predicting realistic intraluminal pressure values when modeling the contraction of a normal GEJ.

To examine the role of each muscle layer, the muscle layers were each contracted individually while the other layer was quiescent. Results showed that the intraluminal pressure values predicted by the 3D model are mainly due to the contraction of the CM layer, and are consistent with the predictions of experimental data found in the literature (Edmundowicz and Clouse, 1991; Nicosia et al., 2001; Pouderoux et al., 1997). Results also showed that while the CM was quiescent, the contraction of the LM layer resulted in an expansion of the GEJ. Similar behavior has previously been reported by Nicosia, et al. (2001) during a 2.5 s period where the contraction of the LM layer preceded the contraction of the CM layer. The benefit of using the 3D model was the ability to show the role of the LM layer over a prolonged period of time and during quiescence of the CM layer.

One of the limitations with the model presented in this study was the uniform pressure magnitude in the circumferential and longitudinal directions due to the use of the cavity mesh. However, Stein et al., (1995) and Liu et al., (1997) have shown that the pressure recorded from the GEJ is axially asymmetrical due to the axial asymmetry of the muscles thickness of the GEJ. The ability to allow variation of pressure throughout the cavity mesh may result in a more realistic pressure profile that could be directly compared with experimental measurements.
Furthermore, to obtain a more realistic physiological model of the GEJ, a specific constitutive relation describing the properties of the smooth muscle layers of a human GEJ is needed. With the availability of a smooth muscle constitutive relation, the 3D model could be used to include the asymmetry of the GEJ and predict different intraluminal pressure values around the circumference of the GEJ as is reported in the literature. The dynamics of the peristaltic wave along the lower esophagus and the GEJ could also be incorporated by spatially varying the calcium activation parameter (Ca_\text{actn}). With the developments of the GEJ model, the contribution of surrounding structures that contribute to the functionality of the GEJ could also be included.

Although simulations are time consuming, with the rapid developments of computer hardware, and with the use of parallel processing, the development of the 3D computer model of the GEJ has several potential applications. The anatomical model could be adapted to provide a useful tool for health professional training and patient education. Also, the 3D model could be used to mimic the physiological behavior of a human GEJ. In addition to modeling normal physiological events, it is also possible to use the 3D model to study abnormal physiology, such as gastroesophageal reflux disease. Our long term goal is to construct 3D computer models on an individual-specific basis using CT or MR images from patients. Such patient-specific modeling may allow the ability to custom design aspects of an operation. In addition, results obtained from the model could potentially be used to guide clinical trials on an individual-specific basis.

**Supplementary Material**

Refer to Web version on PubMed Central for supplementary material.

**Acknowledgments**

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**References**


Figure 1.
A longitudinal cross-sectional view of a cylindrical model and a cavity mesh (lighter shade). The cavity mesh is visible through a transparent section of the cylindrical model. The displacements of the nodes of the cavity mesh were fixed in all directions with the exception of one node on the axis, which was constrained to move along the axial direction.
Figure 2.
Identifying the external length of the GEJ using the location of the crura. (a) The crural mesh with respect to the 3D esophageal mesh. (b) Enlarged view illustrating the location of the crura in relation to the GEJ. The location of the crura was used to identify the GEJ.
Figure 3.
The variation of intraluminal pressure as a function of the number of degrees of freedom of the GEJ computer model. The figure shows that the pressure value was converged when the mesh had 19877 degrees of freedom or more.
Table 1

The intraluminal pressure values predicted by the model during the contraction of the GEJ with and without the contribution of the crura.

<table>
<thead>
<tr>
<th></th>
<th>With crural contribution</th>
<th>GEJ only</th>
</tr>
</thead>
<tbody>
<tr>
<td>Basal pressure mmHg (kPa)</td>
<td>22 (2.95)</td>
<td>12 (1.54)</td>
</tr>
<tr>
<td>Experimental basal pressure mmHg (kPa)</td>
<td>10–40 (1.33–5.33)</td>
<td>6–22 (0.74 – 2.98)</td>
</tr>
<tr>
<td>Peak pressure mmHg (kPa)</td>
<td>52 (6.96)</td>
<td>28 (3.78)</td>
</tr>
<tr>
<td>Experimental peak pressure mmHg (kPa)</td>
<td>50–80 (6.67–10.67)</td>
<td>28–45 (3.74–5.98)</td>
</tr>
</tbody>
</table>

5 Values were taken from the following references (Christensen, 1987; Kahrilas, 1997; Patti et al., 1997; Richter et al., 1987; Shafik et al., 2006; Stein et al., 1995).

4 Values have been calculated by subtracting the 44% contribution of the crura from the values with crural contribution.

3 Values were taken from the following references (Christensen, 1987; Mittal and Balaban, 1997; Sugarbaker et al., 1993; Tytgat, 1991).
Table 2

The intraluminal pressure values predicted by the model with the contraction of each individual muscle layer, and both layers of the GEJ. CM (circular muscle), LM (longitudinal muscle).

<table>
<thead>
<tr>
<th></th>
<th>LM only</th>
<th>CM only</th>
<th>Both layers</th>
</tr>
</thead>
<tbody>
<tr>
<td>Basal pressure mmHg (kPa)</td>
<td>-3 (-0.49)</td>
<td>15 (2.04)</td>
<td>12 (1.54)</td>
</tr>
<tr>
<td>Peak pressure mmHg (kPa)</td>
<td>-7 (-0.97)</td>
<td>38 (5.11)</td>
<td>28 (3.78)</td>
</tr>
</tbody>
</table>